

Testing the quantum nature of gravity with levitated mirrors

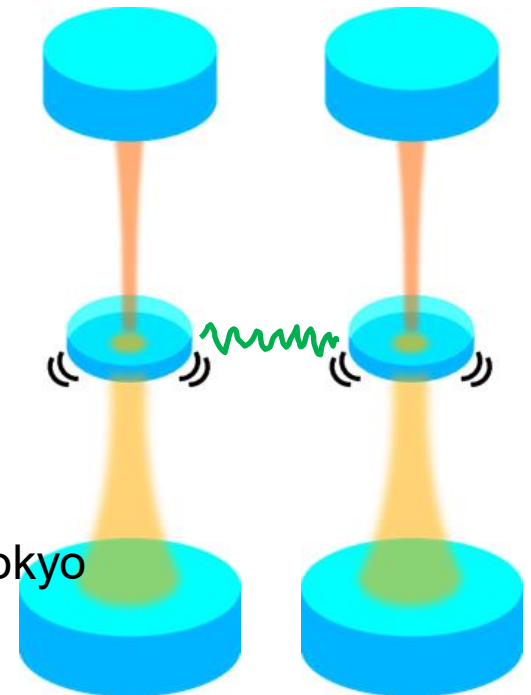


Yuta Michimura

RESCEU, University of Tokyo

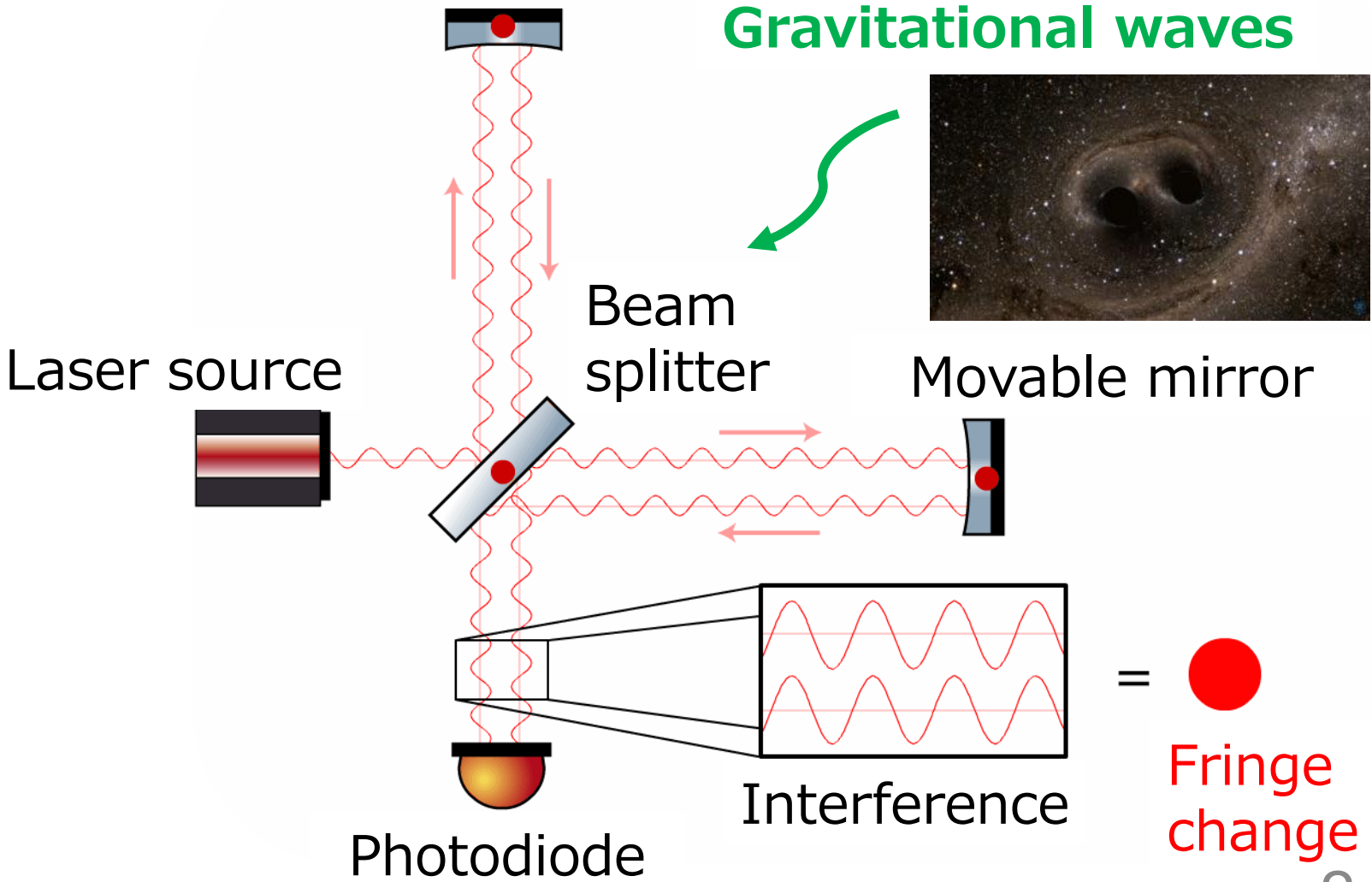
Kavli IPMU, WPI, UTIAS, University of Tokyo

michimura@resceu.s.u-tokyo.ac.jp



Laser Interferometric GW Detectors

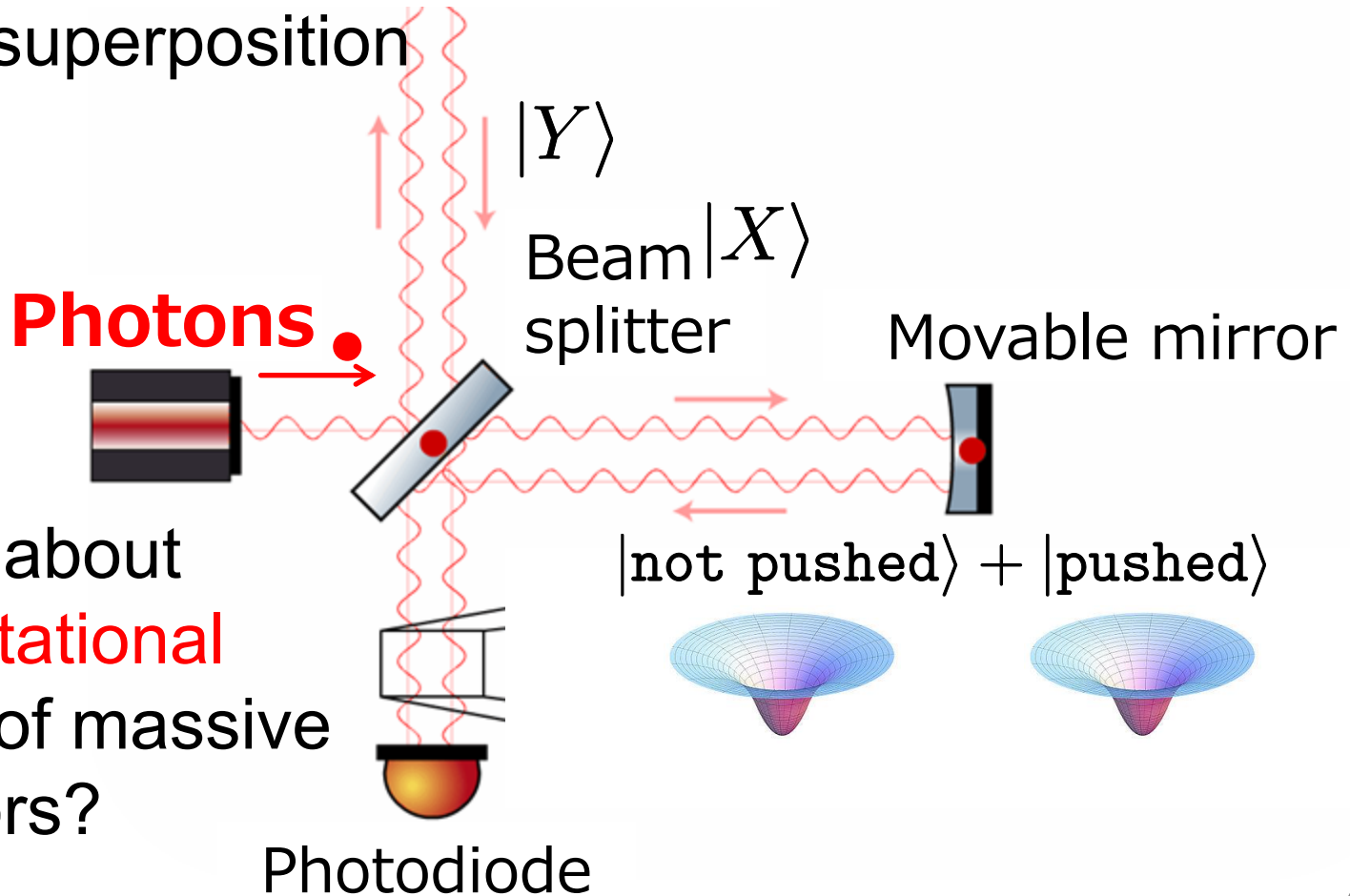
- measures differential arm length change



= ●
Fringe
change

As a Probe of Quantum

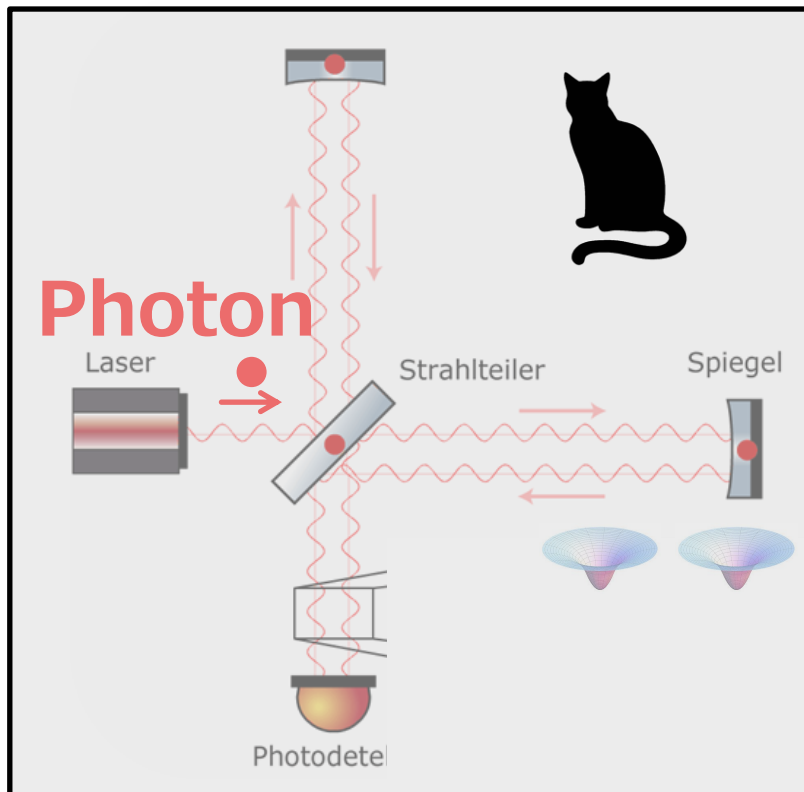
- Photon going to X or Y arm is in **superposition**
- Mirrors **pushed or not pushed** by radiation pressure is in superposition



- How about **gravitational field** of massive mirrors?

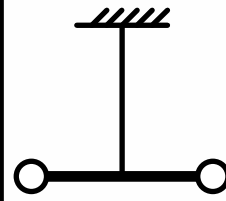
Schrödinger's KAGRA

- If you put **KAGRA in a box** and bring a torsion pendulum close to one of its mirrors, will the torsion pendulum oscillate due to the mirror's gravity, not oscillate at all, or **oscillate half???**



$$\nabla^2 \Phi = 4\pi G \langle \text{Mass distribution} \rangle$$

Expectation value



Semiclassical Gravity
(e.g. Schrödinger-Newton model)

Very strange model, but not experimentally falsified completely.

Various Gravity Models

TABLE I. Summary of collapse, Schrödinger-Newton, and classical gravity models that rely on auxiliary observers. We propose a unified model in which classical gravity depends on the outcomes of auxiliary observers as well as the results of experiments performed by the experimentalist.

Class	Model	Auxiliary observers introduced?	Auxiliary outcomes used to generate ϕ ?	Experimental measurement outcomes used to generate ϕ ?	Features
Collapse models	Diosi-Penrose [18,43]	Measure \mathbf{g} everywhere	No	No	Gravity not implemented
	CSL [20,44]	Measure smeared matter distribution	No	No	
Schrödinger-Newton	Preselection [4,7] S-N	No	No	No	Violates Page-Geilker
	Postselection S-N [7]	No	No	Yes	Future measurement choices influence past.
	Causal-conditional S-N [8,9,11,12]	No	No	Obtain conditional expectation of positions then generate gravity via classical feedback	Preserves causality
Classical gravity with auxiliary observers	N-H extension of S-N [45]	Measure \mathbf{g} everywhere	Yes	No	Classical gravity via Diosi-Penrose measurements
	KTM Model [21,22]	Measure position of each mass	Uses instant outputs of position channels	No	Instant outputs are very noisy
	Oppenheim's model [23]	Yes	Yes	No	More general and includes NH and KTM
	Unified model	Measure position of each mass	Yes	Yes	Can incorporate all above models

This model is falsified by D. N. Page, C. D. Geilker, [PRL 47, 979 \(1981\)](#)



Violates causality



Preserves causality

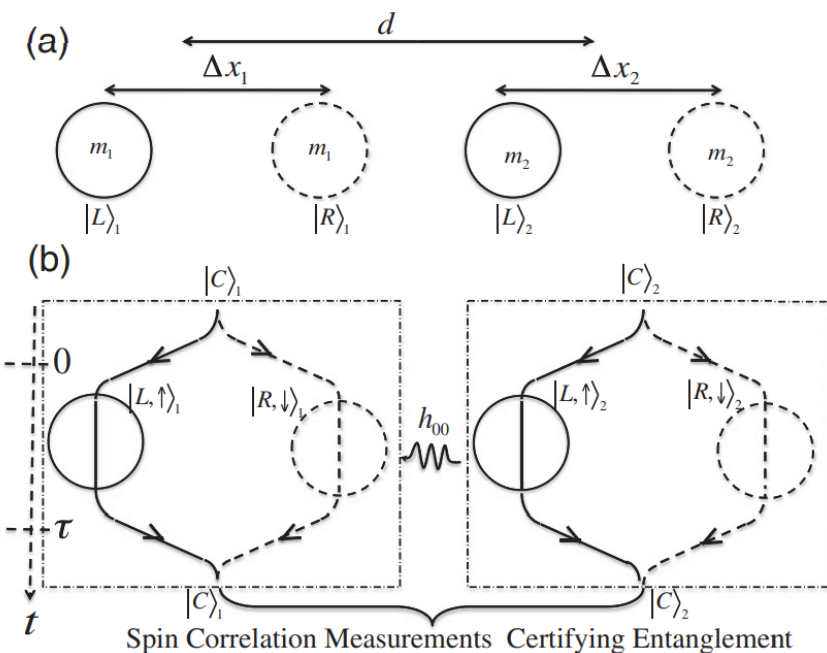


D. Miki, Y. Kaku, Y. Liu, Y. Ma, Y. Chen, [PRD 111, 104084 \(2025\)](#)

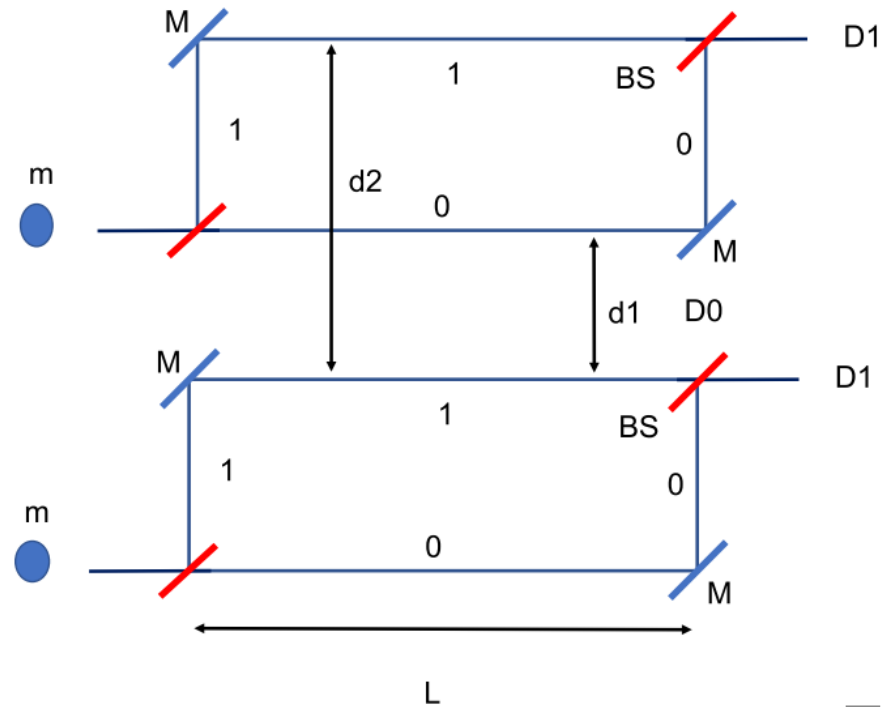
BMV Proposals

- Quantum nature of gravity can be tested by testing **gravity-induced entanglement** with **adjacent matter interferometers**

S. Bose+,
[Phys. Rev. Lett. 119, 240401 \(2017\)](#)



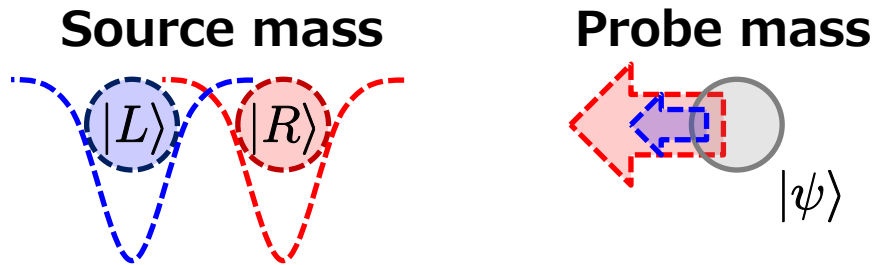
C. Marletto & V. Vedral,
[Phys. Rev. Lett. 119, 240402 \(2017\)](#)



Key Idea of BMV Proposals

- If gravity is quantum

$$\Phi(\hat{x}, \hat{X}) = -\frac{GM}{|\hat{x} - \hat{X}|}$$



Newtonian potential
act as an **operator**

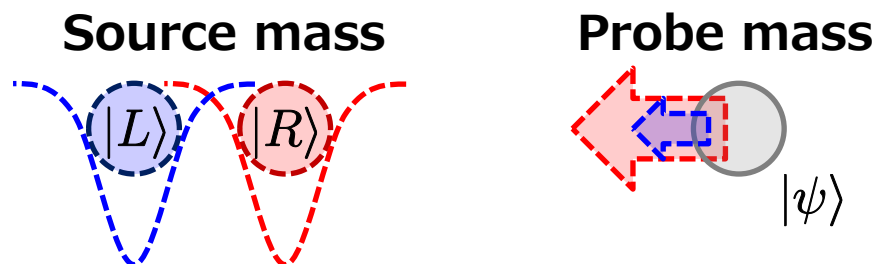
$$\begin{aligned} & e^{\frac{i}{\hbar}m\Phi(\hat{X})t} \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle) \otimes |\psi\rangle \\ &= \frac{1}{\sqrt{2}} (|L\rangle \otimes e^{i\phi_L} |\psi\rangle + |R\rangle \otimes e^{i\phi_R} |\psi\rangle) \end{aligned}$$

**Gravity induced
entanglement**

Key Idea of BMV Proposals

- If gravity is quantum

$$\Phi(\hat{x}, \hat{X}) = -\frac{GM}{|\hat{x} - \hat{X}|}$$



Newtonian potential
act as an **operator**

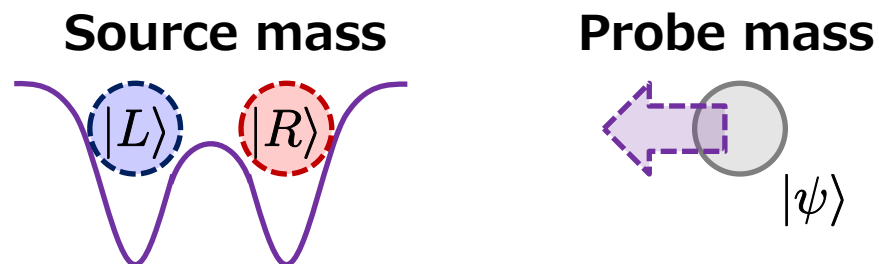
$$e^{\frac{i}{\hbar}m\Phi(\hat{X})t} \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle) \otimes |\psi\rangle$$

$$= \frac{1}{\sqrt{2}} (|L\rangle \otimes e^{i\phi_L} |\psi\rangle + |R\rangle \otimes e^{i\phi_R} |\psi\rangle)$$

**Gravity induced
entanglement**

- If gravity is classical

$$\Phi(\hat{x}) = -\left\langle \frac{GM}{|\hat{x} - \hat{X}|} \right\rangle$$



Newtonian potential
act as a **c-number**

$$e^{\frac{i}{\hbar}m\Phi t} \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle) \otimes |\psi\rangle$$

$$= \frac{1}{\sqrt{2}} (|L\rangle + |R\rangle) \otimes e^{\frac{i}{\hbar}m\Phi t} |\psi\rangle$$

Remains separable

What is the Best Oscillator?

- We computed the amount of entanglement for **arbitrary quadratic potential**

- Hamiltonian

$$H = \sum_{i=1,2} \left(\frac{p_i^2}{2m} + \frac{1}{2} k_i x_i^2 \right) + \frac{Gm^2}{d^3} (x_1 - x_2)^2$$

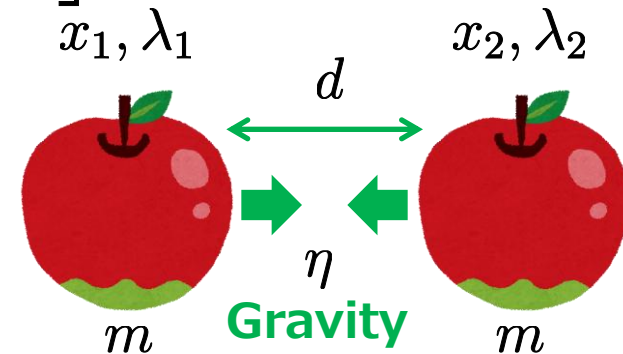
$$= \frac{\omega}{2} \left[\sum_{i=1,2} (P_i^2 + \lambda_i X_i^2) + \eta (X_1 - X_2)^2 \right]$$

Sign of potential
 +1 for harmonic
 0 for free-falling
 -1 for inverted

Strength of gravitational
 coupling

$$\eta = \frac{2Gm}{\omega^2 d^3}$$

Distance between
 masses



Inverted Oscillators are the Best

- Logarithmic negativity when $\lambda \equiv \lambda_1 = \lambda_2$

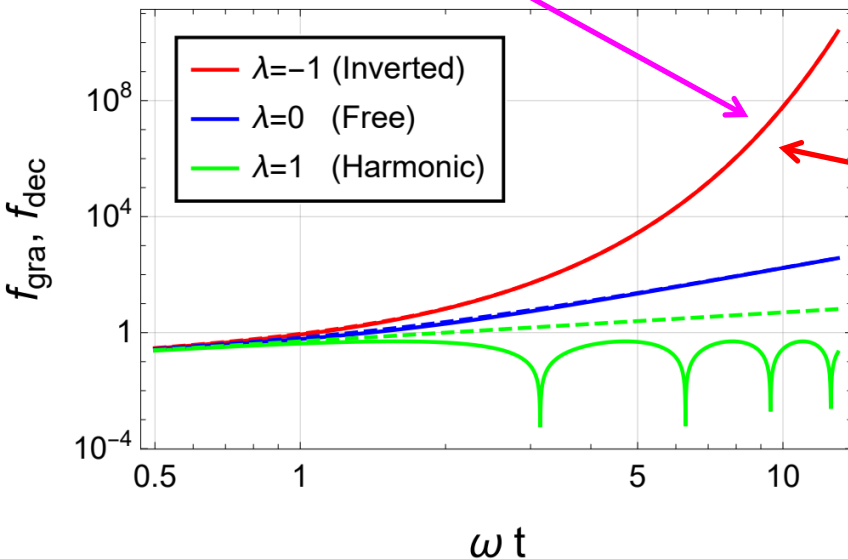
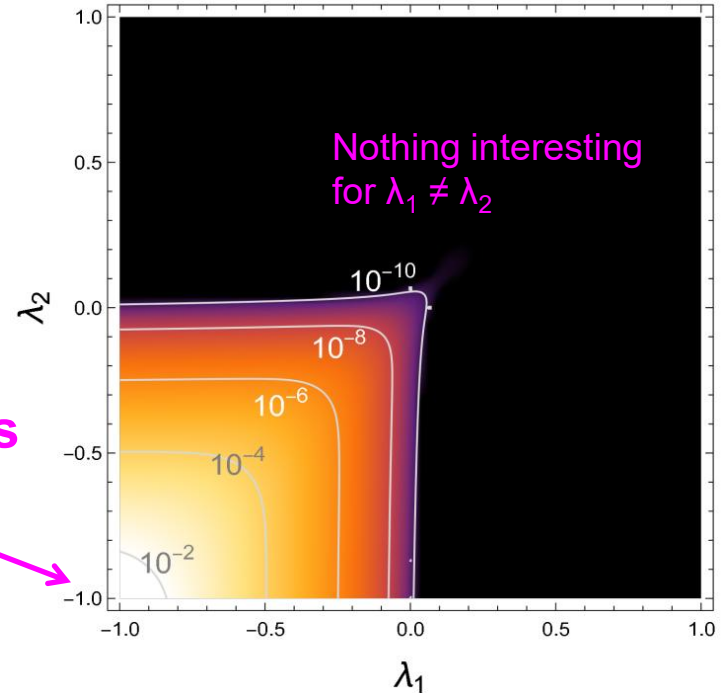
$$E_N \simeq 3[\eta f_{\text{gra}}(t) - \mu f_{\text{dec}}(t)]$$

Strength of gravitational coupling

Amount of decoherence

Exponential growth of entanglement

Inverted oscillators are the best



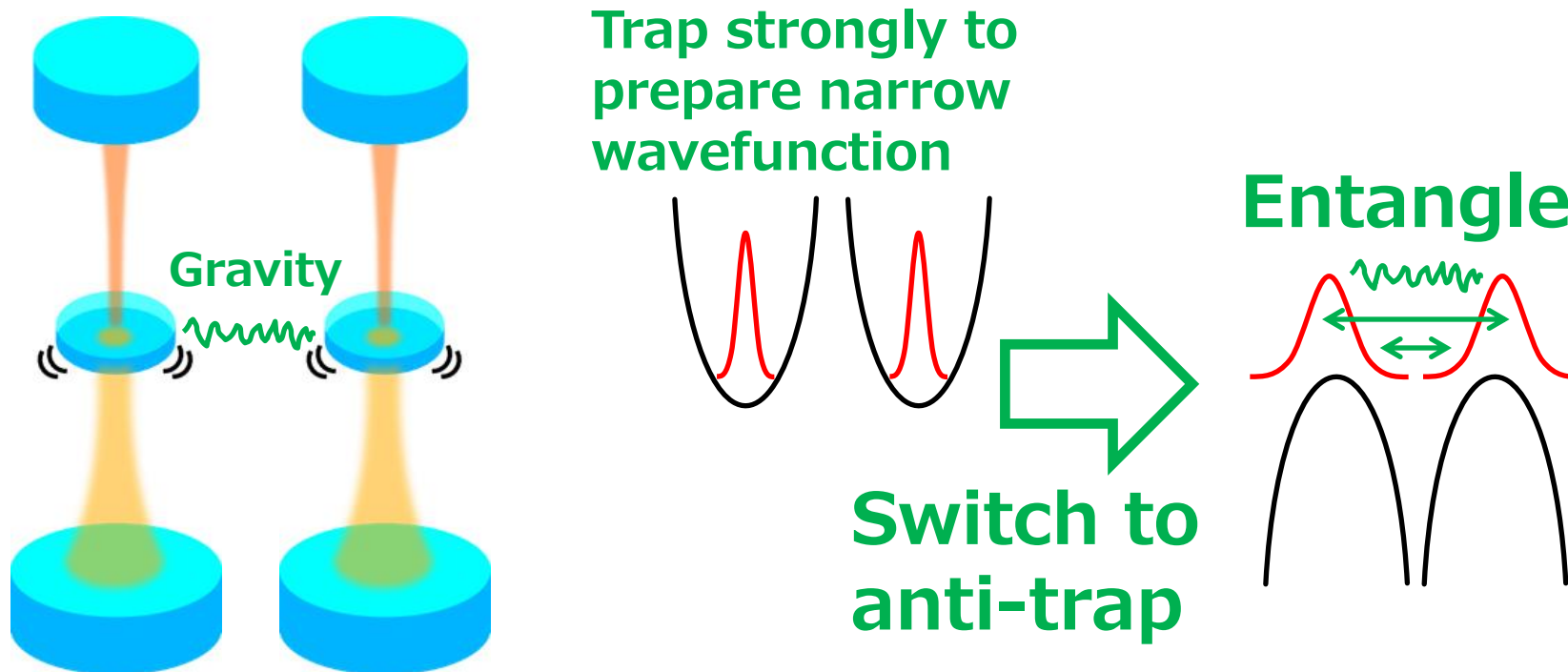
$$f_{\text{gra}}(t) \simeq f_{\text{dec}}(t) \simeq \frac{1}{8} e^{2\omega t}$$

$$f_{\text{gra}}(t) \simeq f_{\text{dec}}(t) \simeq \frac{1}{8} (\omega t)^3$$

$$f_{\text{gra}}(t) \simeq \frac{1}{2} |\sin(\omega t)|, \quad f_{\text{dec}}(t) \simeq \frac{1}{2} \omega t$$

Realization with Levitated Mirrors

- Switching between trap and anti-trap is easy with **optically levitated mirrors**
- Entanglement can be tested in horizontal motion
- Can be done similar with other systems



Example Setup

- To prepare 1 kHz anti-spring for 0.1 mg mirror

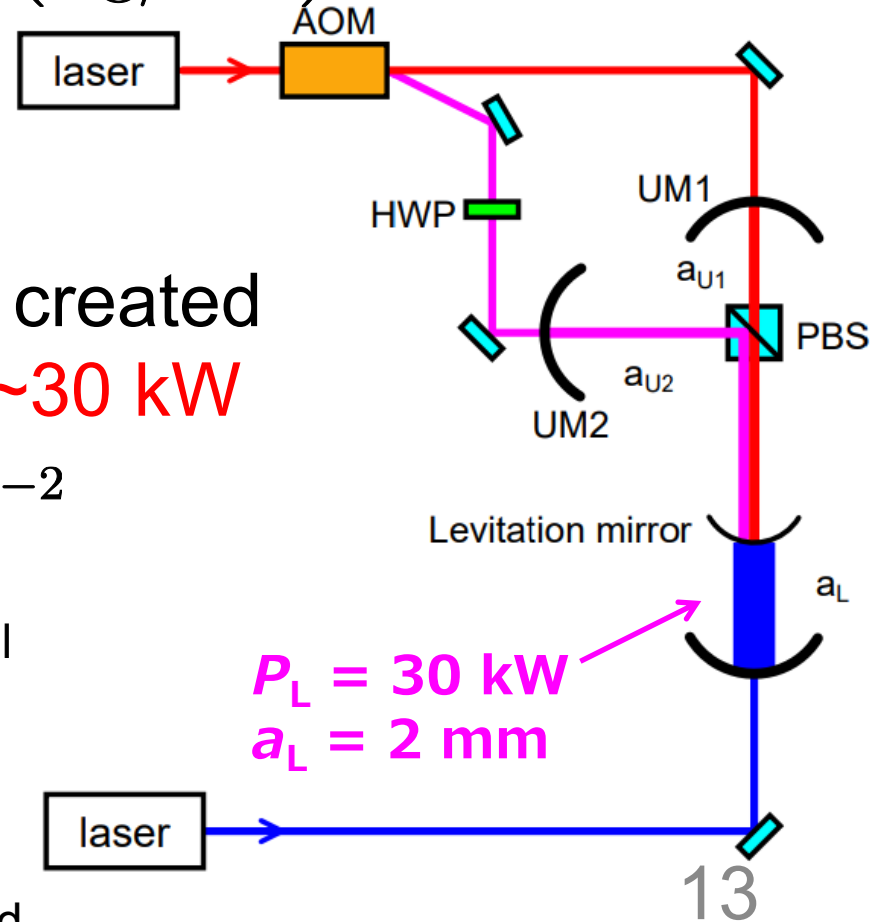
$$\mu \ll \eta = 2.7 \times 10^{-13} \omega_{\text{kHz}} \left(\frac{m/d^3}{2 \text{ g/cm}^3} \right)$$

- Requires $T < \sim 1 \text{ K}$ and $P < \sim 10^{-17} \text{ Pa}$ (as usual)
- $\sim 1 \text{ kHz}$ anti-spring can be created with intra-cavity power of $\sim 30 \text{ kW}$
- Time to generate $E_N = 10^{-2}$

$$\tau_{\text{ent}} = 4.2 \omega_{\text{kHz}}^{-1/3} \text{ sec} \quad \text{for free-fall}$$

300 times faster

$$\tau_{\text{ent}} = 1.3 \times 10^{-2} \omega_{\text{kHz}}^{-1/3} \text{ sec} \quad \text{for inverted}$$



Fabricating Mirrors for Levitation

- To support the mass:

$$mg = \frac{2P_{\text{circ}}}{c}$$

Roughly 1.5 kW of power is required to levitate 1 mg mirror

- Mirror needs to be **curved**, **high reflectivity** and **low absorption**. Our target now is:

φ 3 mm, 0.1 mm thick (~1.6 mg for fused silica)

Curvature RoC = **~30 mm convex**

Reflectivity $R > 99.95 \%$

Absorption $A < \sim 0.5$ ppm (LIGO, Virgo, KAGRA level)

- Experiment in ANU suggest higher absorption makes the system unstable (**photothermal effects**)

C. Gu+, [New J. Phys. 25, 123051 \(2023\)](#)

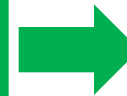
How to Make Tiny Mirrors

2014 Approach (Company in Japan)

(1) Make 3 mm dia. lens



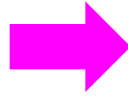
(2) Coat



2020- Approach

(2018-2024 ANR-JST CREST,
2025-2027 France- Japan JSPS Bilateral program)

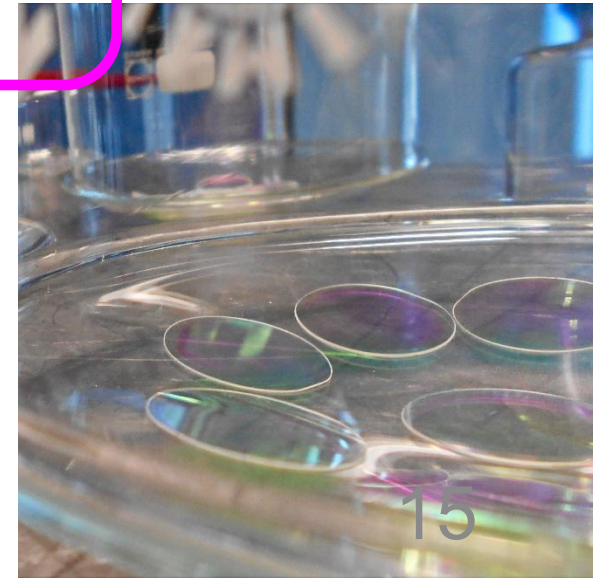
(1) Make 1 inch dia.
0.1 mm thick disk



(2) Coat (bend due to stress)



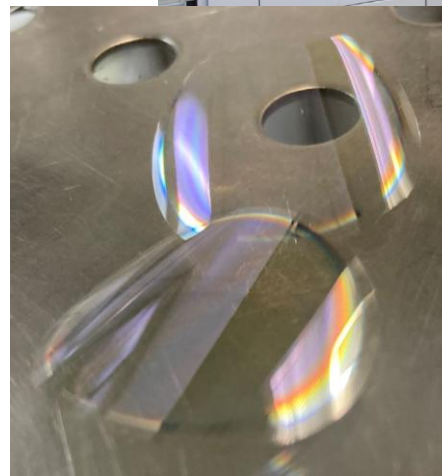
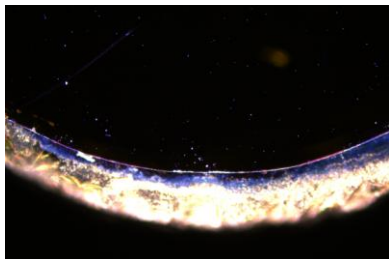
(3) Cut into 3 mm dia.



Fabrication Status in LMA

- HR coating with amplitude transmittance $T=10$ ppm (6.2 μm thick)
- Cut into $\phi 3$ mm is tough
- Curvature was not enough $O(10$ cm)
- Now trying thinner substrate (25 μm) with laser cutting

1/4 thick, 1/16 curvature



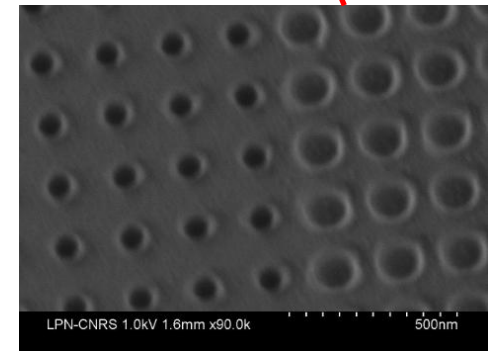
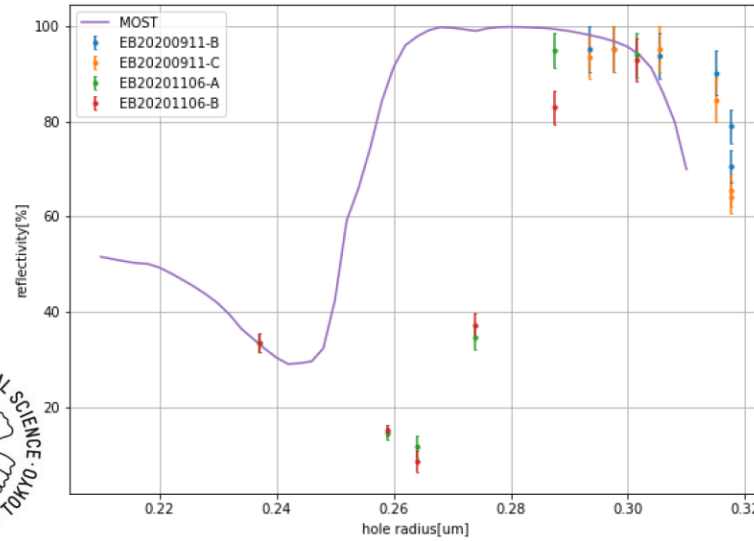
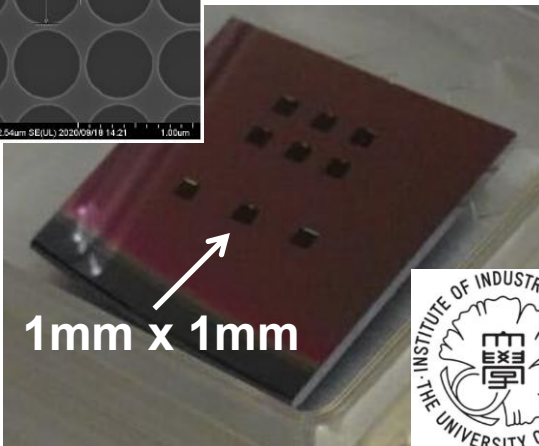
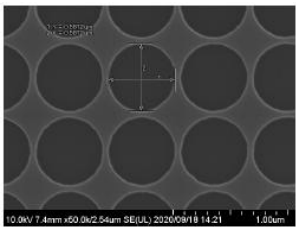
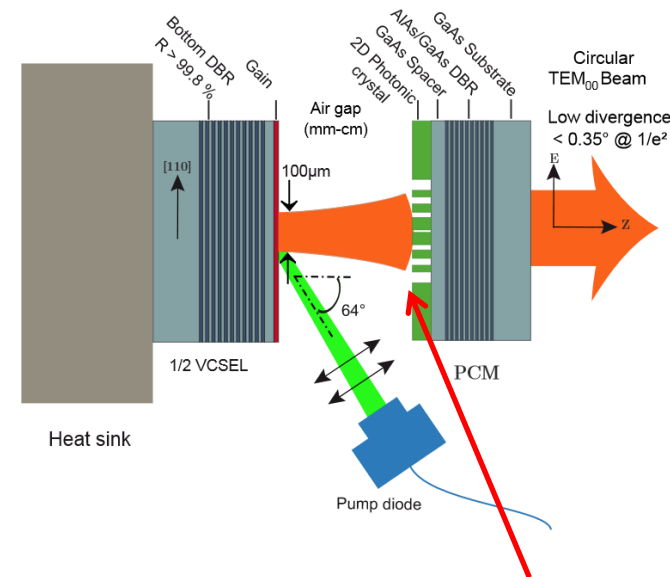
Metasurface Approach

- **Effective curvature** possible by modulating the filling factor

M. S. Seghilani+,
[Optics Express 22, 5962 \(2014\)](#)

- Tried with Si with different filling factor

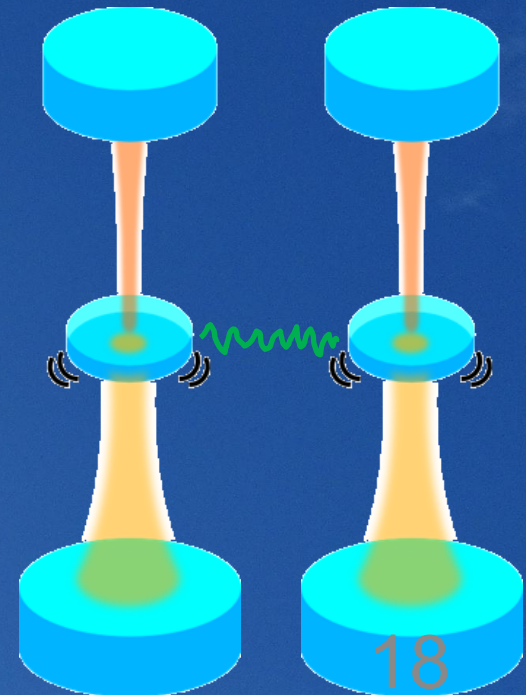
So far achieved 95(5) % reflectivity



Summary

- Quantum nature of gravity can be tested with **gravity induced entanglement**
- Entanglement generation can be accelerated with **inverted oscillators**
- **Mirror fabrication** is underway to realize optical levitation of mirrors for the first time

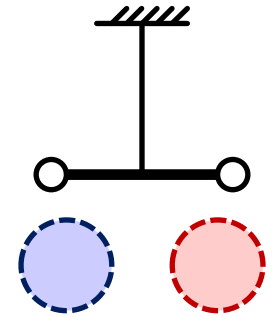
T. Fujita, Y. Kaku, A. Matsumura, YM,
CQG 42, 165003 (2025)



Bonus Slides

Page-Geilker Experiment

- Source mass was moved according to γ -ray emission from Cobalt 60
→ Torsion **correlated** with γ -ray emission



VOLUME 47, NUMBER 14

PHYSICAL REVIEW LETTERS

5 OCTOBER 1981

Indirect Evidence for Quantum Gravity

Don N. Page

Department of Physics, The Pennsylvania State University, University Park, Pennsylvania 16802

and

C. D. Geilker

Department of Physics, William Jewell College, Liberty, Missouri 64068

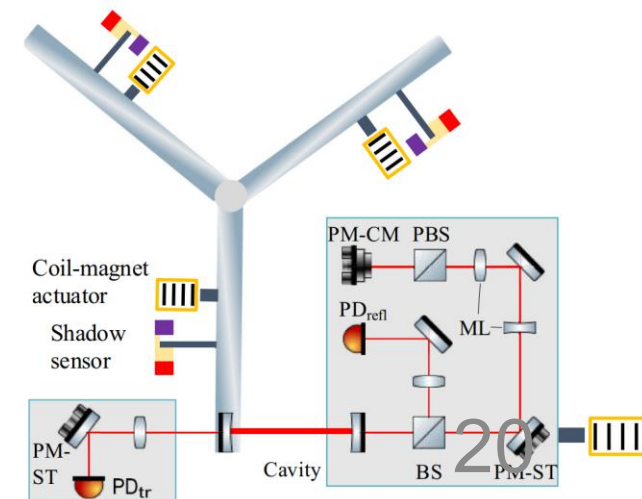
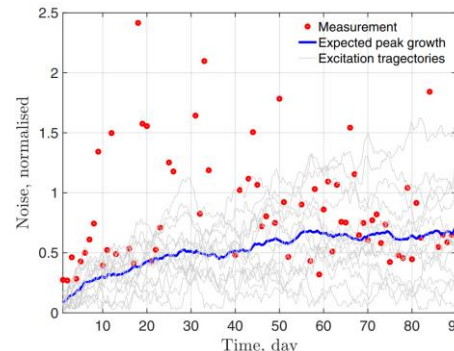
(Received 9 June 1981)

D. N. Page, C. D. Geilker,
[PRL 47, 979 \(1981\)](#)

An experiment gave results inconsistent with the simplest alternative to quantum gravity, the semiclassical Einstein equations. This evidence supports (but does not prove) the hypothesis that a consistent theory of gravity coupled to quantized matter should also have the gravitational field quantized.

- Preselection Schrodinger-Newton also tested more recently
(resonant frequency shift from self-gravity and the growth in the resonant peak)

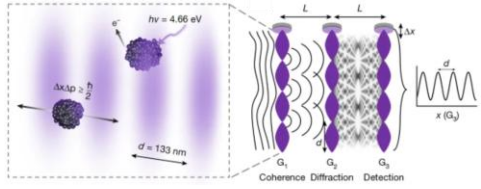
T. Yan+,
[PRD 111, 082007 \(2025\)](#)



Quantum and Gravity Experiments

Quantum →

← **Gravity**



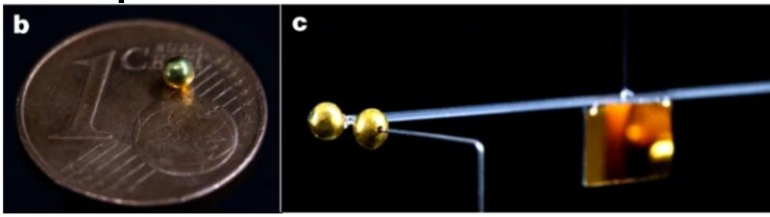
sodium nanoparticles,
 $3e-19$ g
[Pedalino+ \(2026\)](#)
Interference



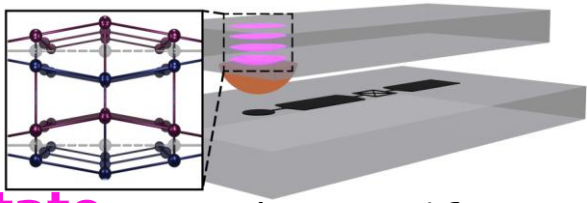
cantilever, 50 ng
[Cripe+ \(2019\)](#)

Backaction

Planck mass
 $22 \mu\text{g}$



torsion pendulum, 90 mg
[Westphal+ \(2021\)](#)



Cat state acoustic wave, 16 μg
[Bild+ \(2023\)](#)

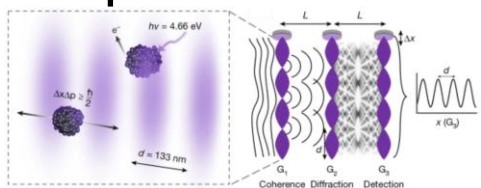
Quantum and Gravity Experiments

Quantum

Quantum regime of gravity

Gravity

Mass



sodium nanoparticles,
3e-19 g

[Pedalino+ \(2026\)](#)

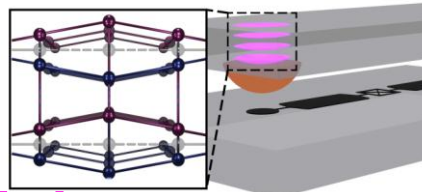
Interference



cantilever, 50 ng

[Cripe+ \(2019\)](#)

Backaction

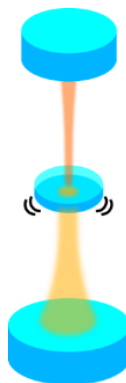


Cat state acoustic wave,
[Bild+ \(2023\)](#)

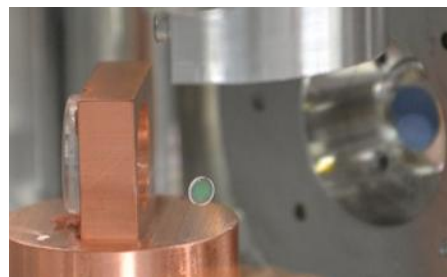
Planck mass
22 μg



Our focus: 0.1-10 mg scale



optical levitation,
~0.2 mg



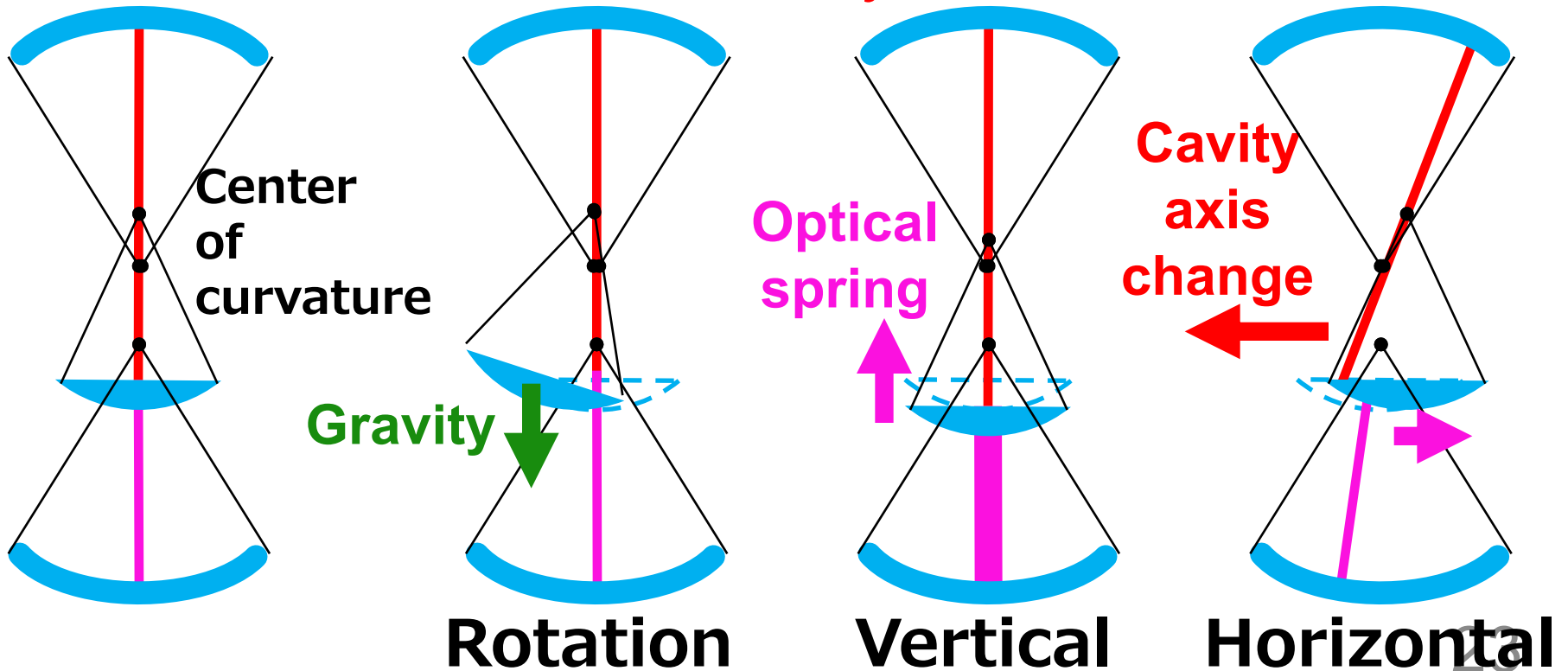
suspended disk, 7 mg
[Matsumoto+ \(2019\)](#)



suspended bar, 10 mg
[Komori+ \(2019\)](#)

Stability of Levitation

- Rotational motion is stable with **gravity**
- Vertical motion is stable with **optical spring**
- Horizontal motion is stable with **cavity axis change**
- *Curved mirror is necessary!*

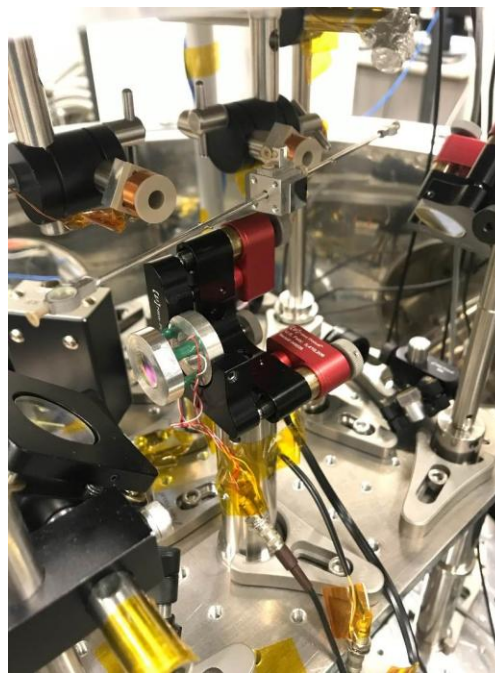
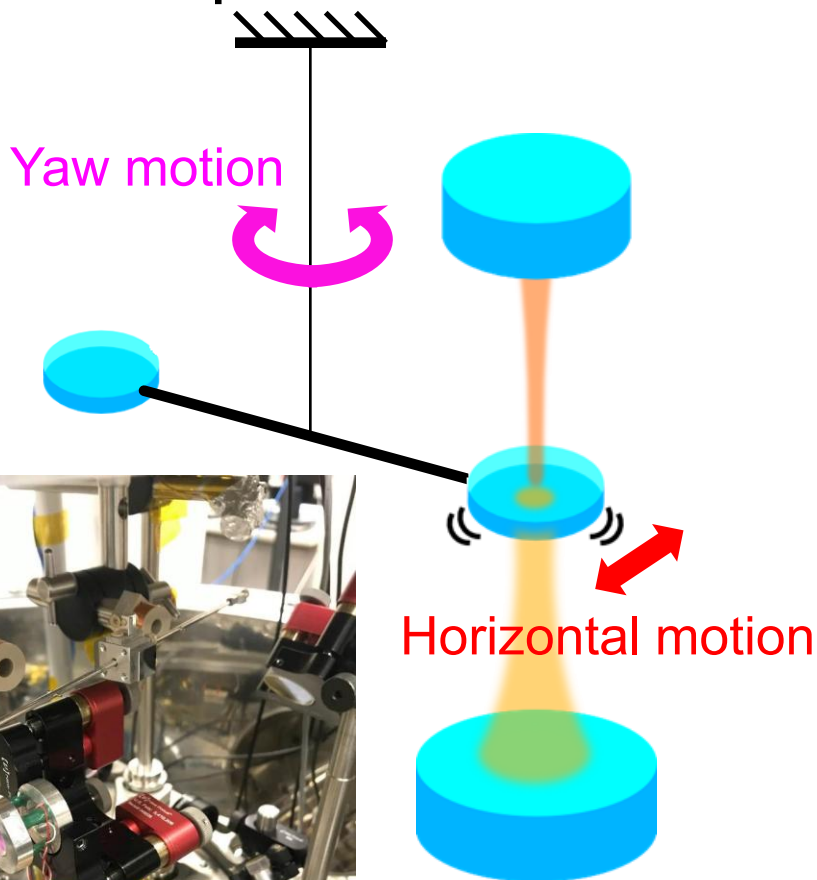
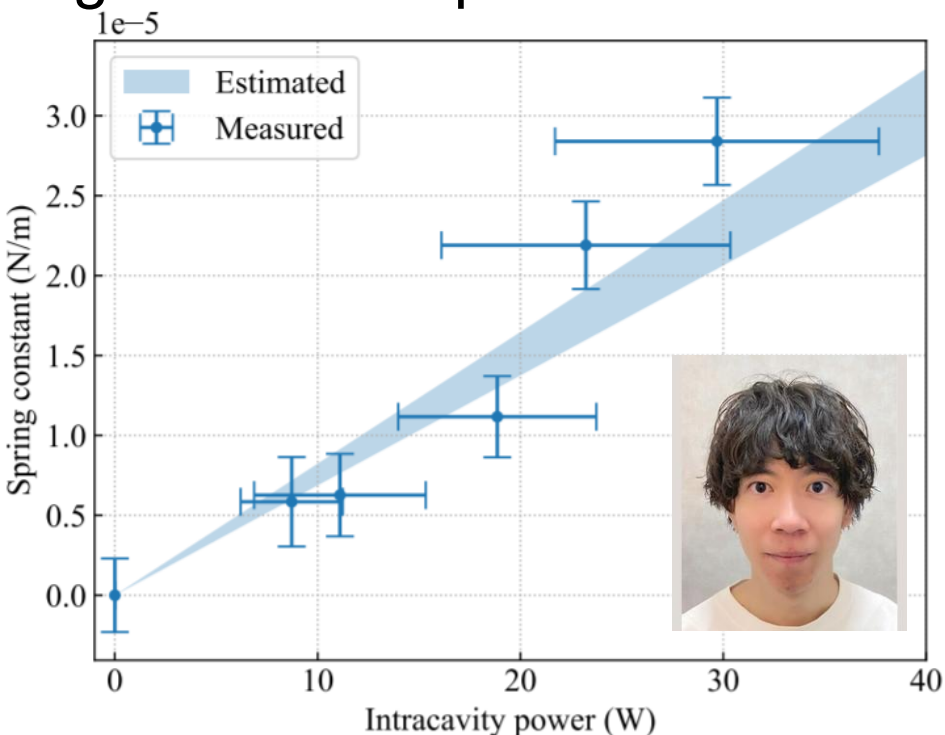


Experiment to Verify the Stability

- **Verified the stability** with a torsion pendulum and a dummy mirror

T. Kawasaki, ..., YM,
[PRA 102, 053520 \(2020\)](#)

Measured optical geometrical spring agreed with expectation



Decoherence Effects

- Decoherence estimates suggest
 $T < 1 \text{ K}$ and $P < 10^{-16} \text{ Pa}$ are required
- Also, free-fall time and height are in the orders of
 $\sim 1 \text{ sec}$ and $\sim 10 \text{ m}$
- Sounds tough...



Table 3. Free-fall times t and heights $h = \frac{1}{2}gt^2$, with $g \simeq 9.8 \text{ m s}^{-2}$, required to generate the amount E of entanglement at fixed values of temperature T and pressure P for the proposals of BM and Krisnanda.

Proposal	T (K)	P (Pa)	E	T (s)	H (m)
BM	1	10^{-16}	10^{-2}	0.15	0.1
	1	10^{-16}	10^{-1}	1.5	11
	1	10^{-15}	No generation	/	/
	10^{-2}	10^{-15}	No generation	/	/
Krisnanda	1	10^{-16}	10^{-2}	1.1	6.2
	1	10^{-16}	10^{-1}	2.9	42
	1	10^{-15}	No generation	/	/
	10^{-2}	10^{-15}	10^{-2}	1.2	7.6

Is Fast Good?

- The process can be **repeated multiple times**
 - Also, now that the oscillator is not free-falling, height is not required, and repeatable
- **Air pressure** requirement could be **relaxed**
 - Entanglement speed is so fast that no molecule will hit the oscillator during the measurement time
 - Mean free time of the scattering

$$\tau_{\text{air}} = 0.64 \text{ sec} \left(\frac{R}{0.2 \text{ mm}} \right)^{-2} \left(\frac{p}{10^{-17} \text{ Pa}} \right)^{-1} \left(\frac{T}{1 \text{ K}} \right)^{-1/2}$$

- More rigorous study necessary for treating random force under extremely low pressure

Still, Decoherence is the Issue

- **Decoherence** effects also increases exponentially with inverted oscillators

$$E_N \simeq 3[\eta f_{\text{gra}}(t) - \mu f_{\text{dec}}(t)]$$

η Gravity
 μ Decoherence
 Logarithmic negativity

- $\eta > \mu$ is required

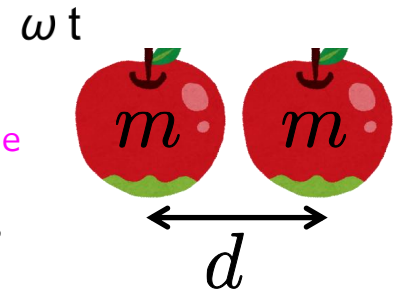
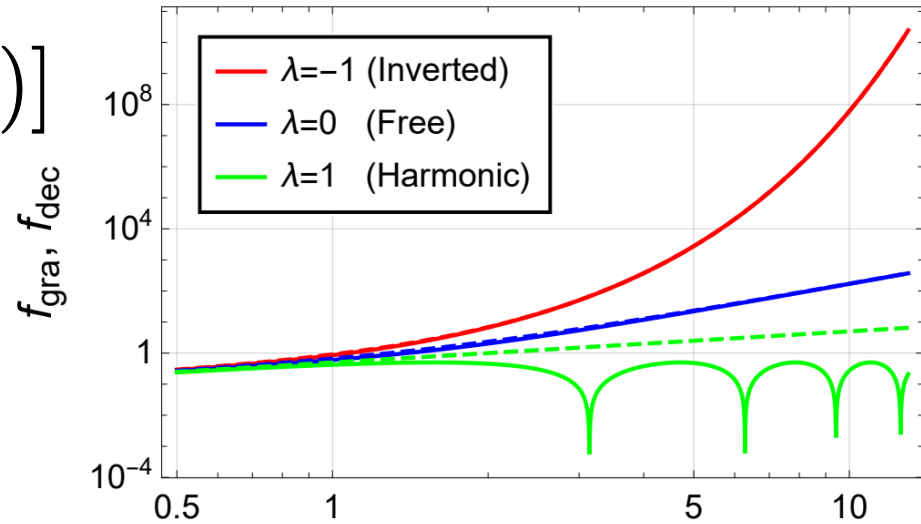
$$\frac{2Gm}{\omega_m d^3} > \frac{2k_B T_{\text{th}} \gamma_m}{\hbar \omega_m}$$

Damping rate

For 300 K
(smaller by ~ 10 orders of magnitude than state-of-the-art)

$$\gamma_m < \frac{\hbar G m}{k_B T_{\text{th}} d^3} = 1.7 \times 10^{-21} \text{ Hz} \frac{m/d^3}{1 \text{ g/cm}^3}$$

Fused silica: 2 g/cm³ Osmium: 22 g/cm³



Comparison with $f \cdot Q$ Criterion

- Necessary condition for **ground state cooling**

$$f_m Q_m \gg \frac{k_B T_{\text{th}}}{\hbar} \simeq 6 \times 10^{12} \left(\frac{T_{\text{th}}}{300 \text{ K}} \right)$$

Resonant frequency

Q-value

$$Q_m \equiv \frac{\omega_m}{\gamma_m}$$

- Thus,

$$\gamma_m \ll 1 \times 10^{-12} \text{ Hz} \left(\frac{f_m}{1 \text{ Hz}} \right) \left(\frac{300 \text{ K}}{T_{\text{th}}} \right)$$

Damping rate

- Criterion for testing gravity induced entanglement is **9 orders of magnitude harder**

$$\gamma_m < \frac{\hbar G m}{k_B T_{\text{th}} d^3} = 1.7 \times 10^{-21} \text{ Hz} \frac{m/d^3}{1 \text{ g/cm}^3}$$