

レーザー干渉計型重力波検出器

Laser interferometric gravitational wave detectors

7. Future



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<https://yutamich.gitlab.io/lectures.html#lectures>

Assignment for Dec 5

- Describe your overall impressions of the lectures and list up the topics you want to study further.
- You may also answer from the Google Form below
<https://forms.gle/6AwJ48XcpWQXqMon9>

Don't forget to put
your name and
student#

You may answer in
any language



Plan of the Lecture Today

- My Top 5 favorite gravitational wave events
- Next generation detectors
- Space gravitational wave detectors
- **Goal:** Understand that improvements in the detectors are necessary for better future

My Favorite GW Events

1. GW170817

2. GW190521

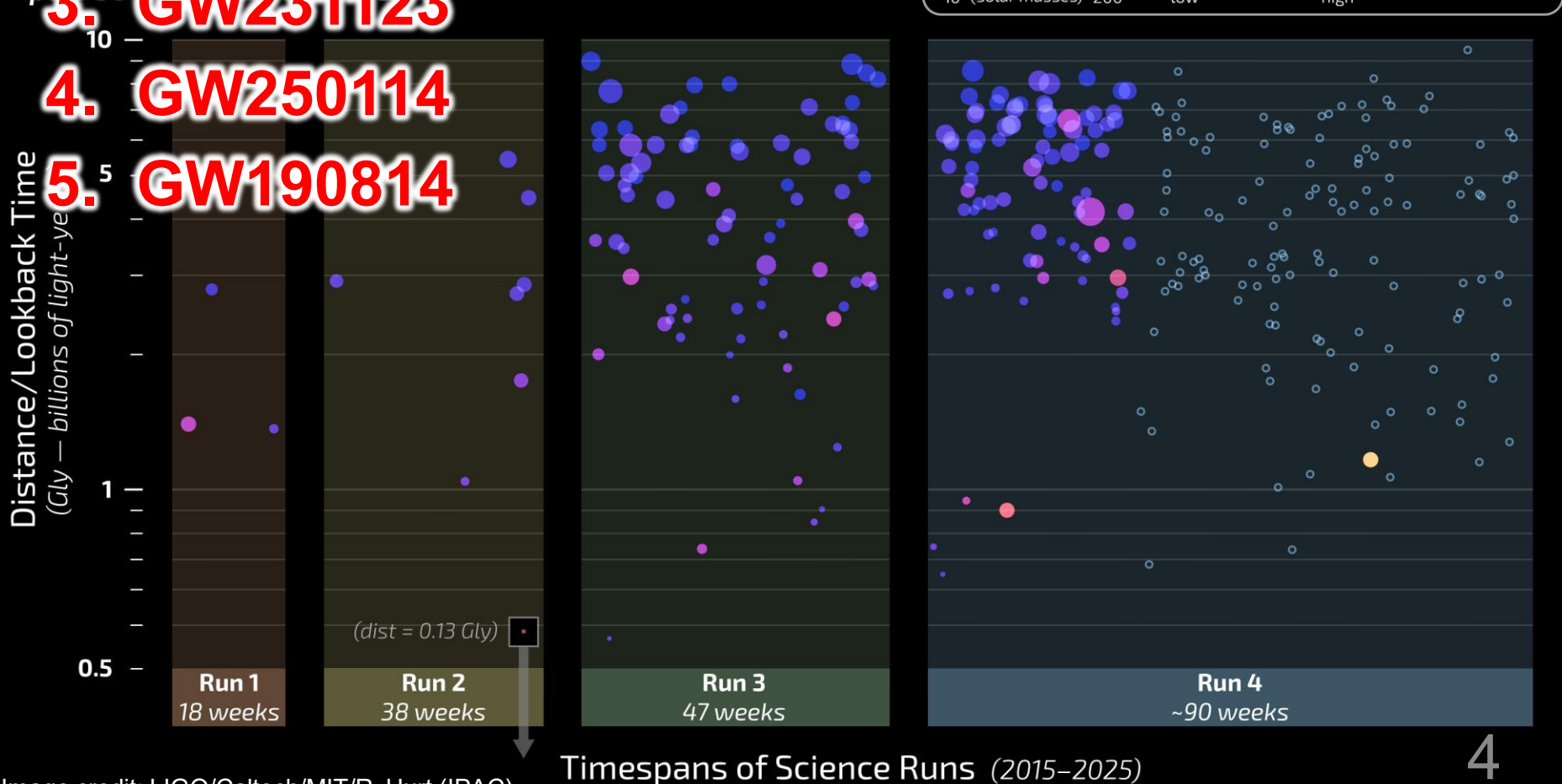
3. GW231123

4. GW250114

5. GW190814

10 Years of LIGO Black Hole* Mergers

*plus several

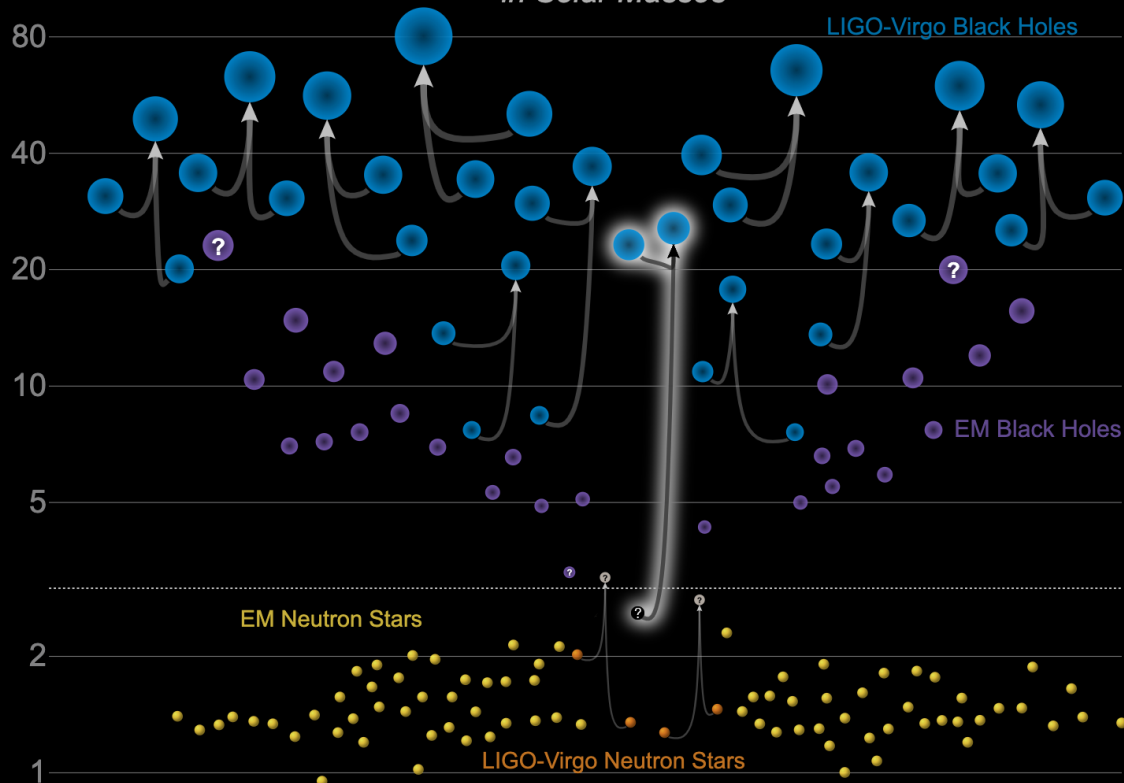


GW190814: $23M_{\odot} + 2.6M_{\odot}$

- Lowest mass ratio, mystery compact object

[2020 ApJL 896 L44](#)

Masses in the Stellar Graveyard in Solar Masses

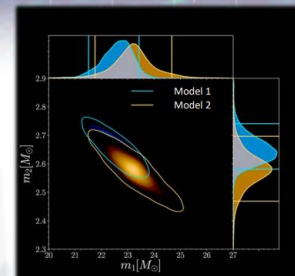


Updated 2020-05-16
LIGO-Virgo | Frank Elavsky, Aaron Geller | Northwestern

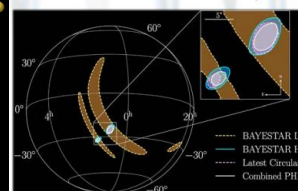
GW190814 Factsheet

Lowest mass ratio event to date
Strongest evidence of higher order modes

Observed by:	LIGO Hanford, LIGO Livingston and Virgo detectors
Source type:	BH and compact object
Date:	August 14 th 2019
Time of merger:	21:10:39 UTC
Network SNR:	25
Distance:	196 – 282 Mpc
Redshift:	0.05
Chirp Mass:	6.1 $M_{\odot}$
Primary Mass:	23.2 $M_{\odot}$
Secondary Mass:	2.6 $M_{\odot}$
Mass ratio:	0.11
Final Mass:	25.6 $M_{\odot}$



Spin Perpendicular to Orbital Plane:	0.0
Spin Parallel to Orbital Plane:	0.0
Spin of Final BH:	0.28
SNR in Octupole Mode:	5.2 – 7.9
# GW cycles (above 20Hz)	300 cycles
Sky Area:	18 deg ²
Merger Rate:	1 – 23 Gpc ³ yr ⁻¹
Initial Public Alert Delay:	5 min



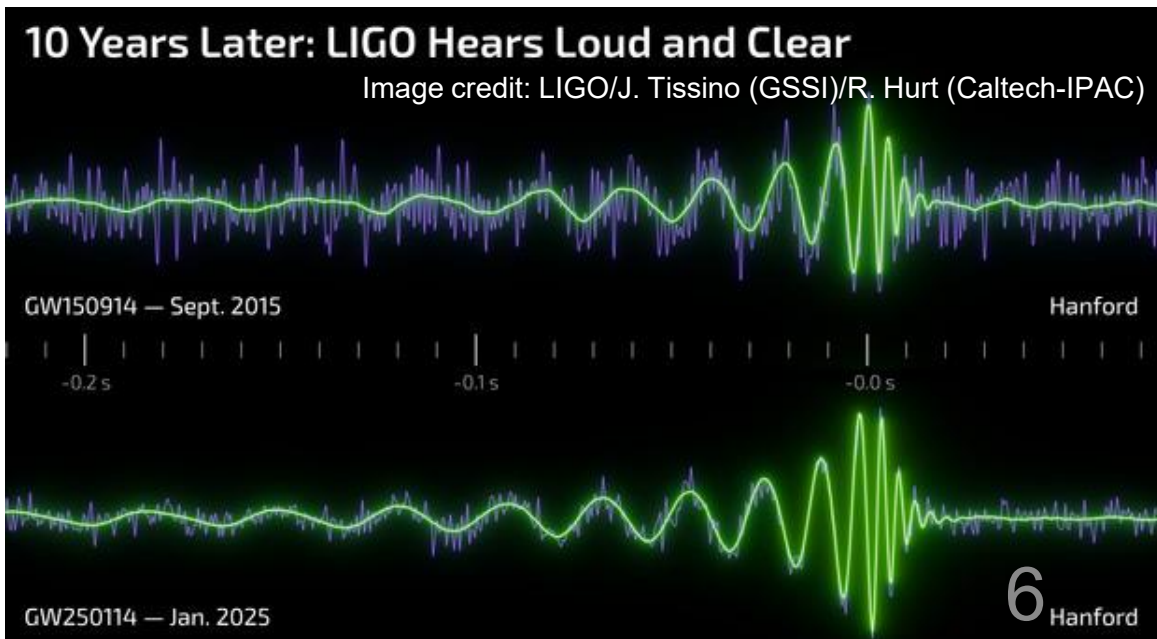
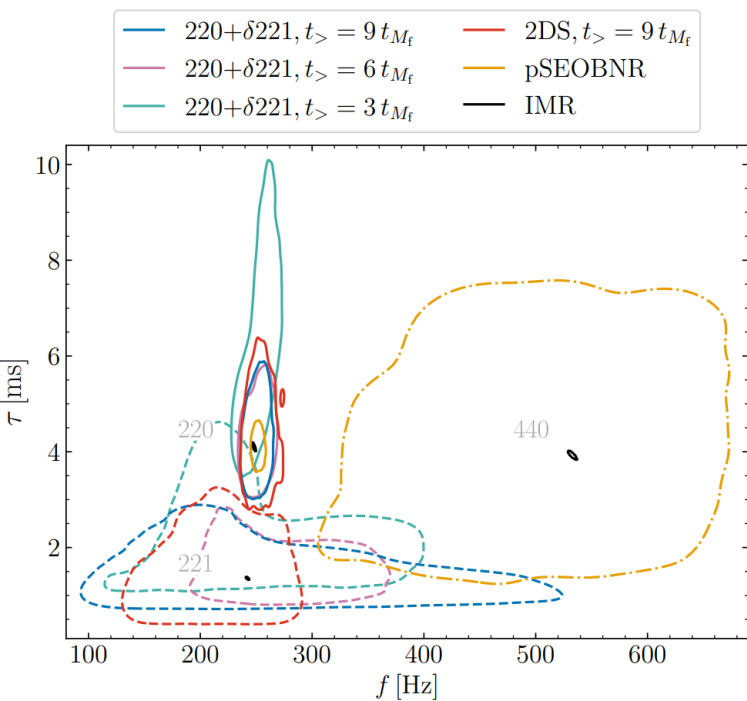
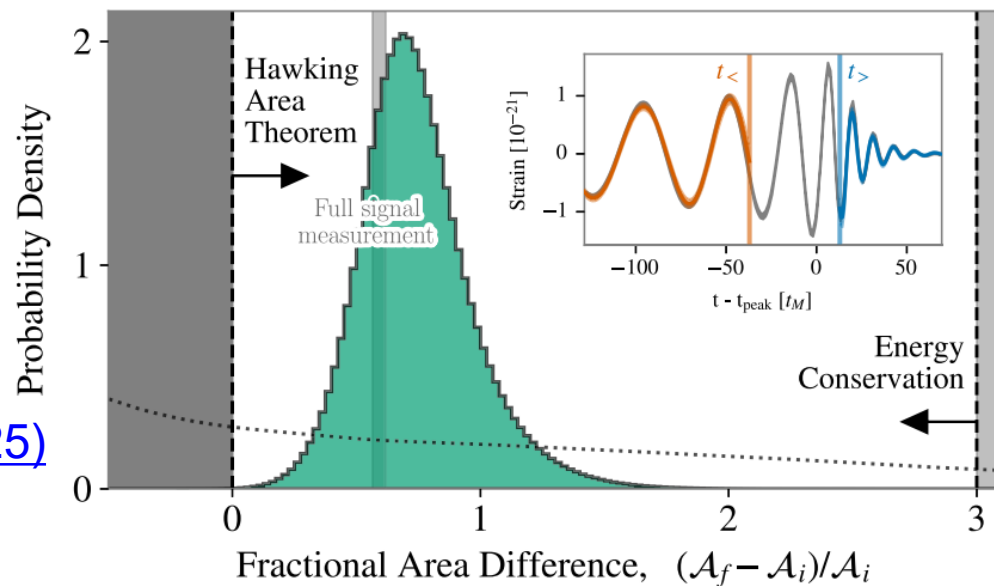
No. 4

GW250114: Area Law, Overtones

- Largest network SNR of ~ 80 (L+H) enabling new tests

[PRL 135, 111403 \(2025\)](#)

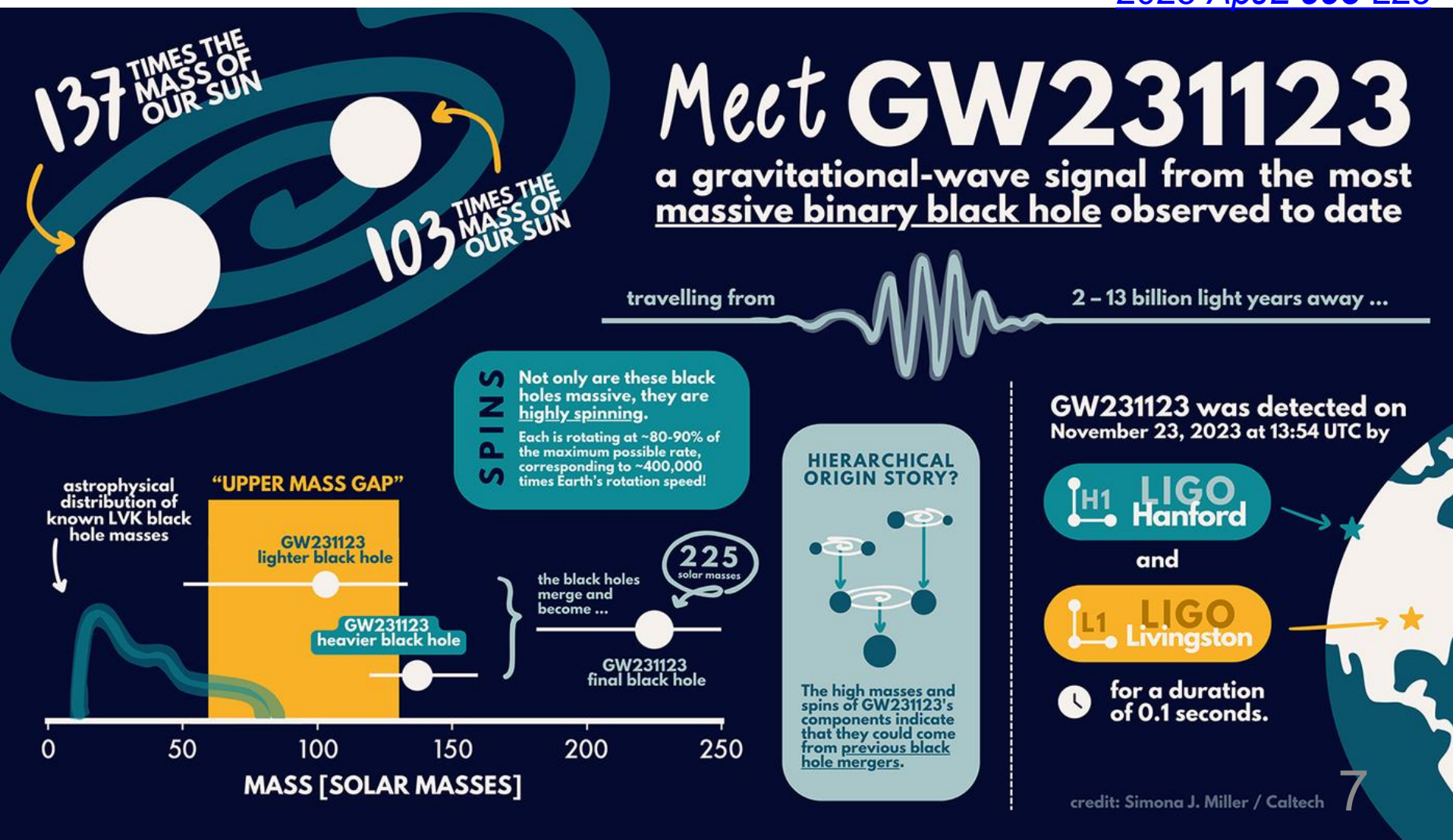
[arXiv:2509.08099](#)



GW231123: Heaviest Binary BHs

- Hint for the origin of heavy stellar-mass BHs?

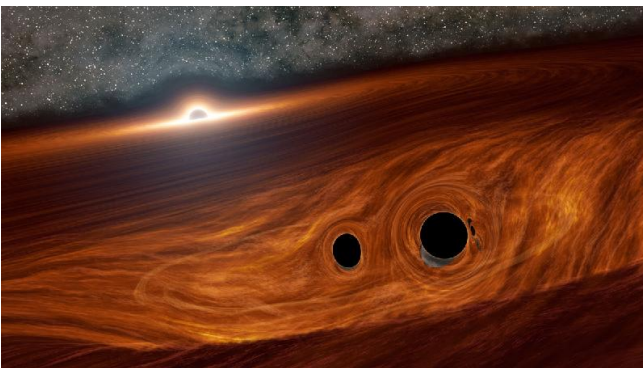
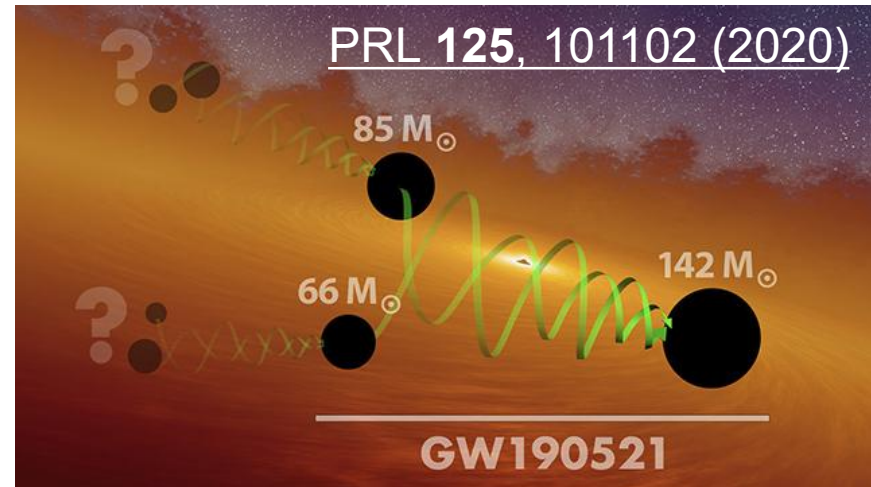
2025 ApJL 993 L25



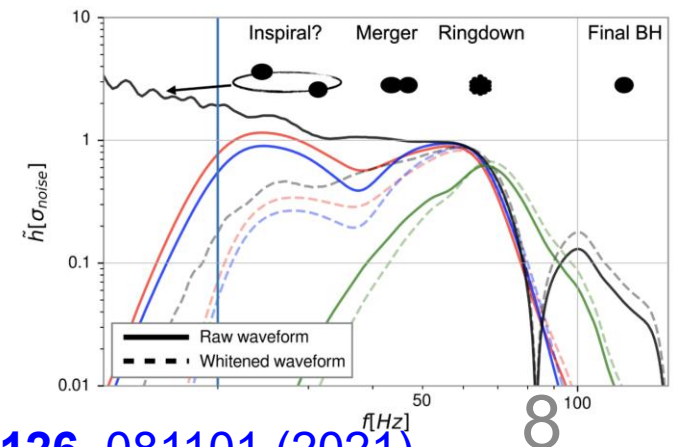
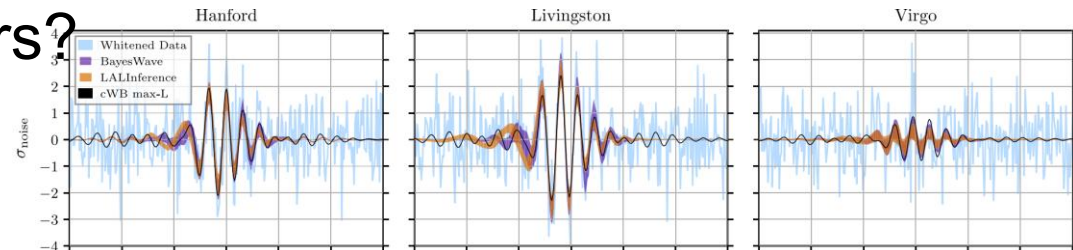
GW190521: First IMBH event

- Zwicky Transient Facility found the **electromagnetic flare** consistent with expectations for a kicked binary black hole merger in the accretion disk.

Repeat flare in 1.6 years?



M. J. Graham+,
[PRL 124, 251102 \(2020\)](#)

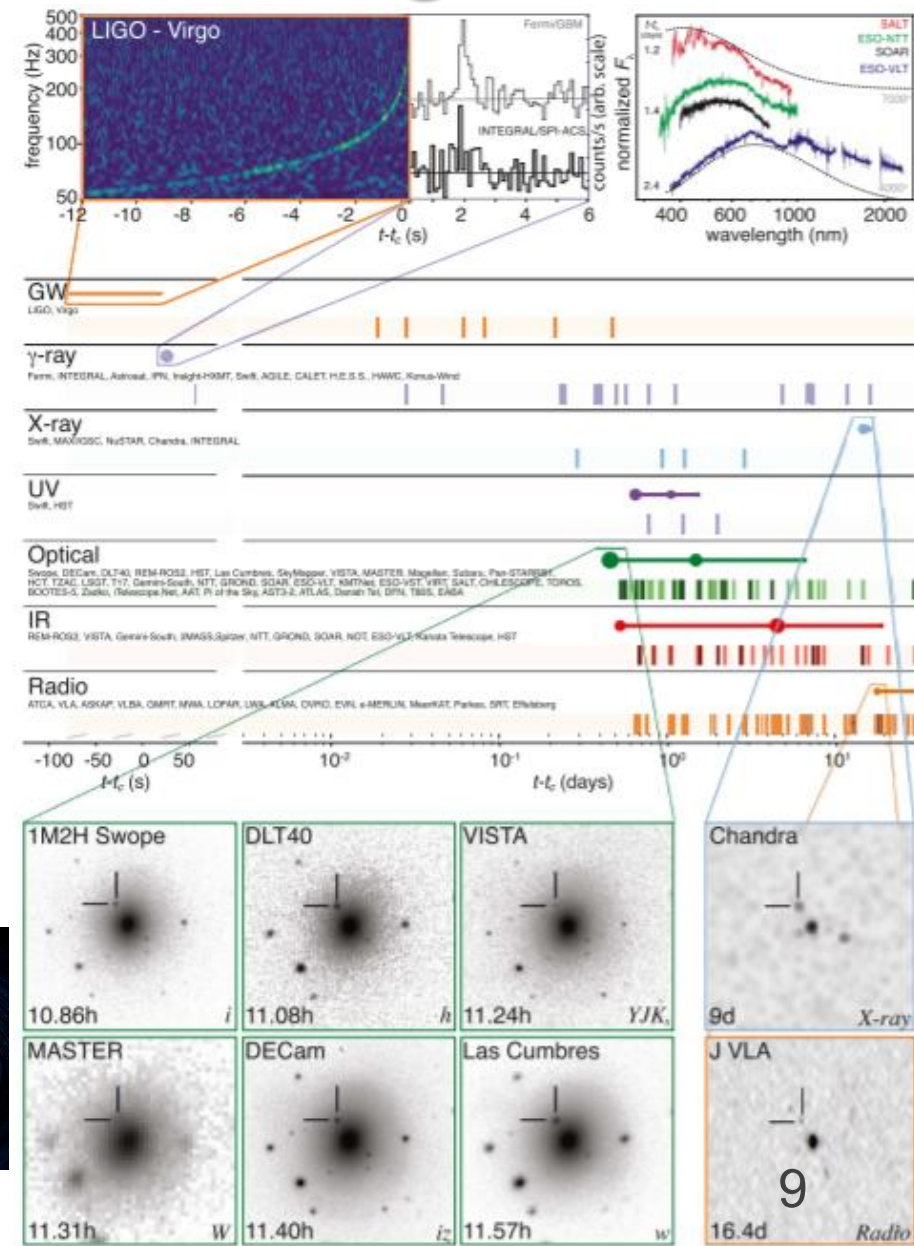
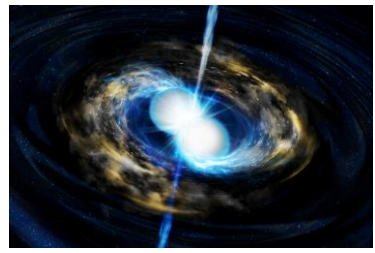


- Could be collision of Proca stars?
Vector boson star of $8.7e-13$ eV

Juan Calderón Bustillo+, [PRL 126, 081101 \(2021\)](#)

GW170817: Multi-messenger Event

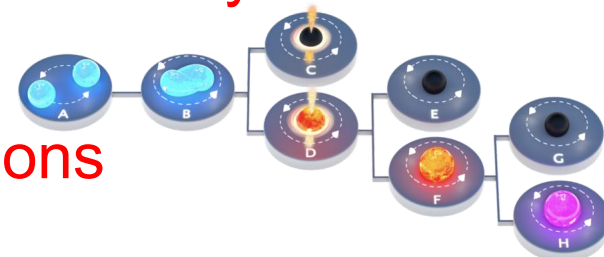
- Detected by HLV, localized $\sim 30 \text{ deg}^2$
- Short gamma-ray burst, kilonova detected
- Speed of gravity
- Hubble constant
- Studies of neutron star equation of state
- Evidence for production of heavy elements



LV and many, [ApJL 848, L12 \(2017\)](#)

So, What's Left?

- What is the origin of **heavy black holes**?
- What are the compact objects in $\sim 3\text{-}5 M_{\odot}$ range?
- What happened **after the BNS merger**?
- What are the progenitors of **GRBs** and **kilonovae**?
 - Short/long GRBs explained by BNS?
 - Diversity of kilonovae? c.f. GRB211211A, GRB230307A
- Can BNS mergers explain the origin of all **heavy elements**?
- QCD **phase transition**?
- Tests of general relativity with **polarizations**
- **Hubble** tension, **dynamical dark energy** ...
- Continuous waves, bursts from supernovae ...
- Clear need for **more** detectors with **better** sensitivity
- More **multi-messenger** detections

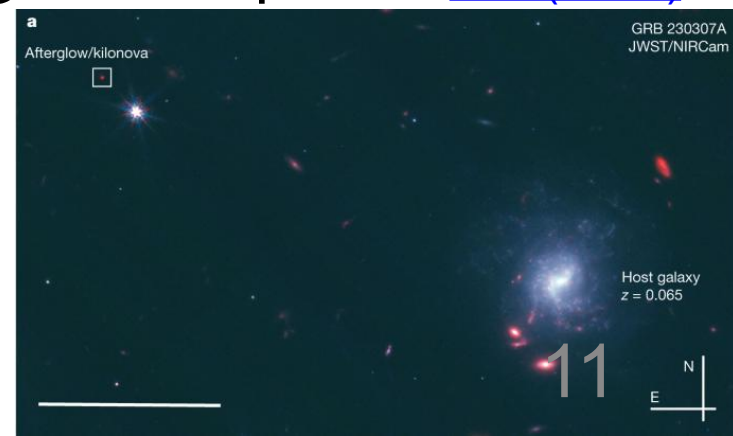


Sarin & Lasky,
[GRG 53, 59 \(2021\)](#)

Power of Multi-Messenger Obs.

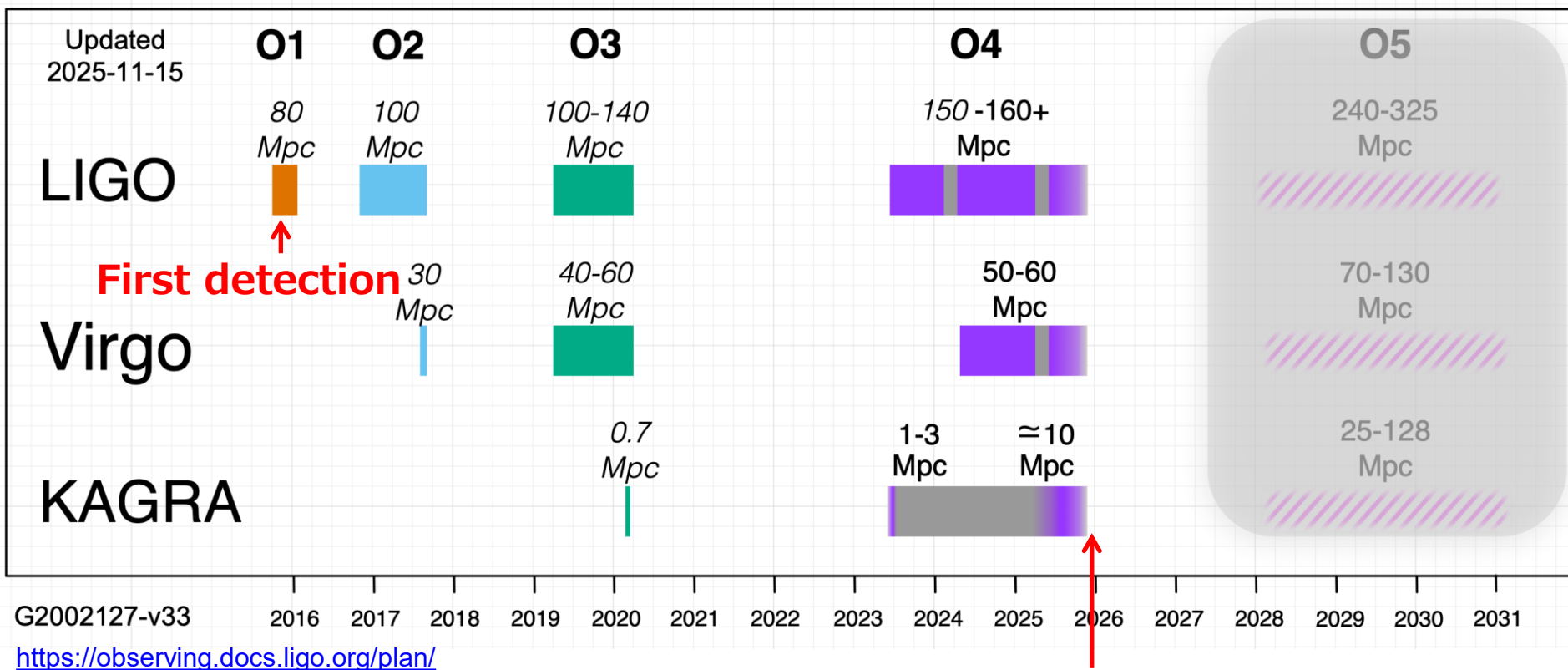
- **GW170817** (**GW** + **EM** event) @ 40 Mpc
 - Localized to **30 deg²** with Hanford, Livingston, Virgo
 - GW from BNS merger, short GRB, kilonova detected
- **GW190425** (**GW** only event) @ 159 Mpc
 - Localized to **~8000 deg²** with Livingston, Virgo
 - GW from BNS merger, no EM counterpart
 - Probably prompt collapse to BH??
- **GRB211211A** (**EM** only event) @ ~350 Mpc
- **GRB230307A** (**EM** only event) @ ~300 Mpc
 - GW detectors not operating
 - BNS merger??
 - **Long GRB**
 - **kilonova** spectrum different from GW170817 (really BNS??)

Levan+,
[Nature 626, 737 \(2024\)](#)

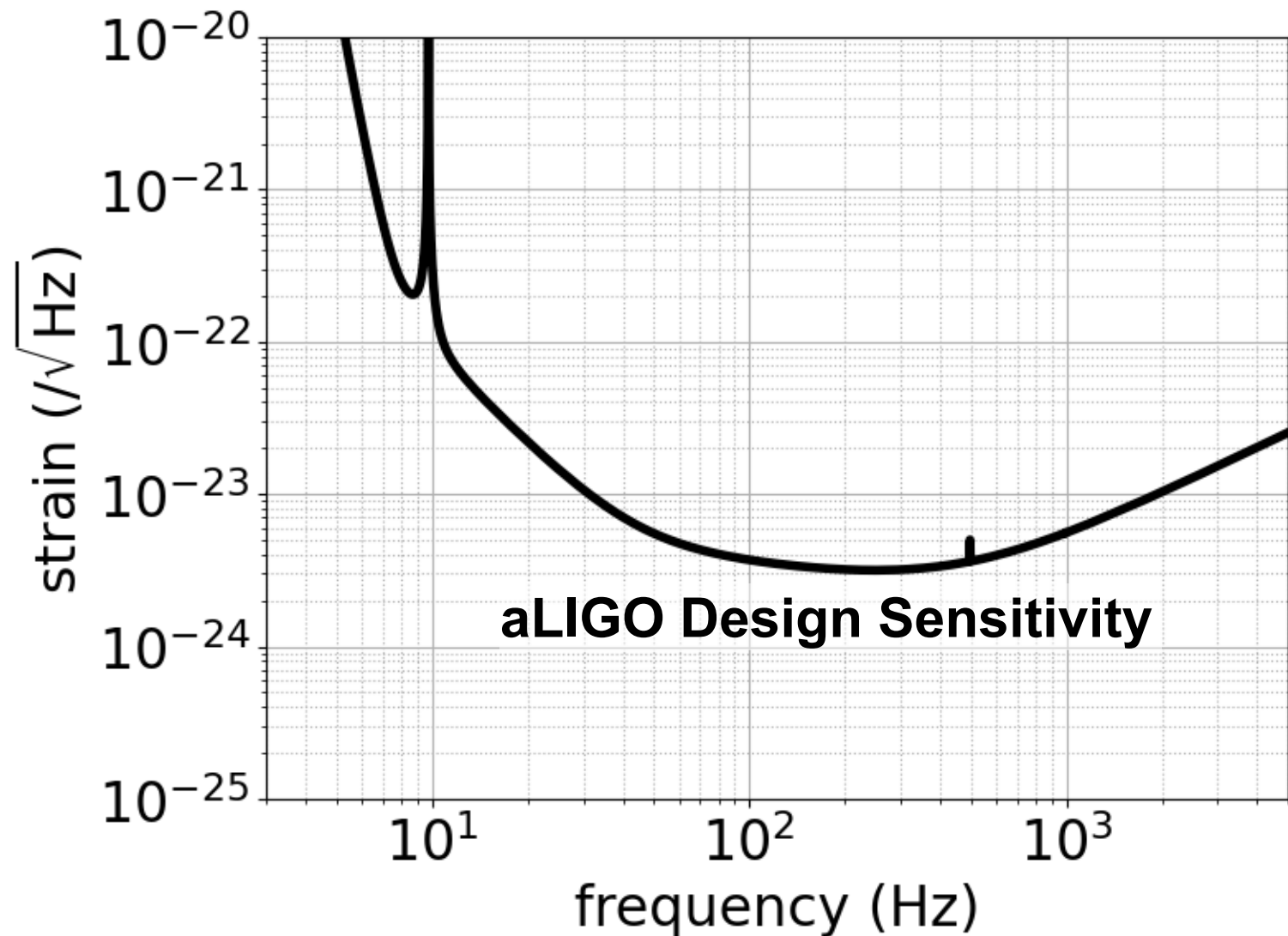


LIGO-Virgo-KAGRA Observations

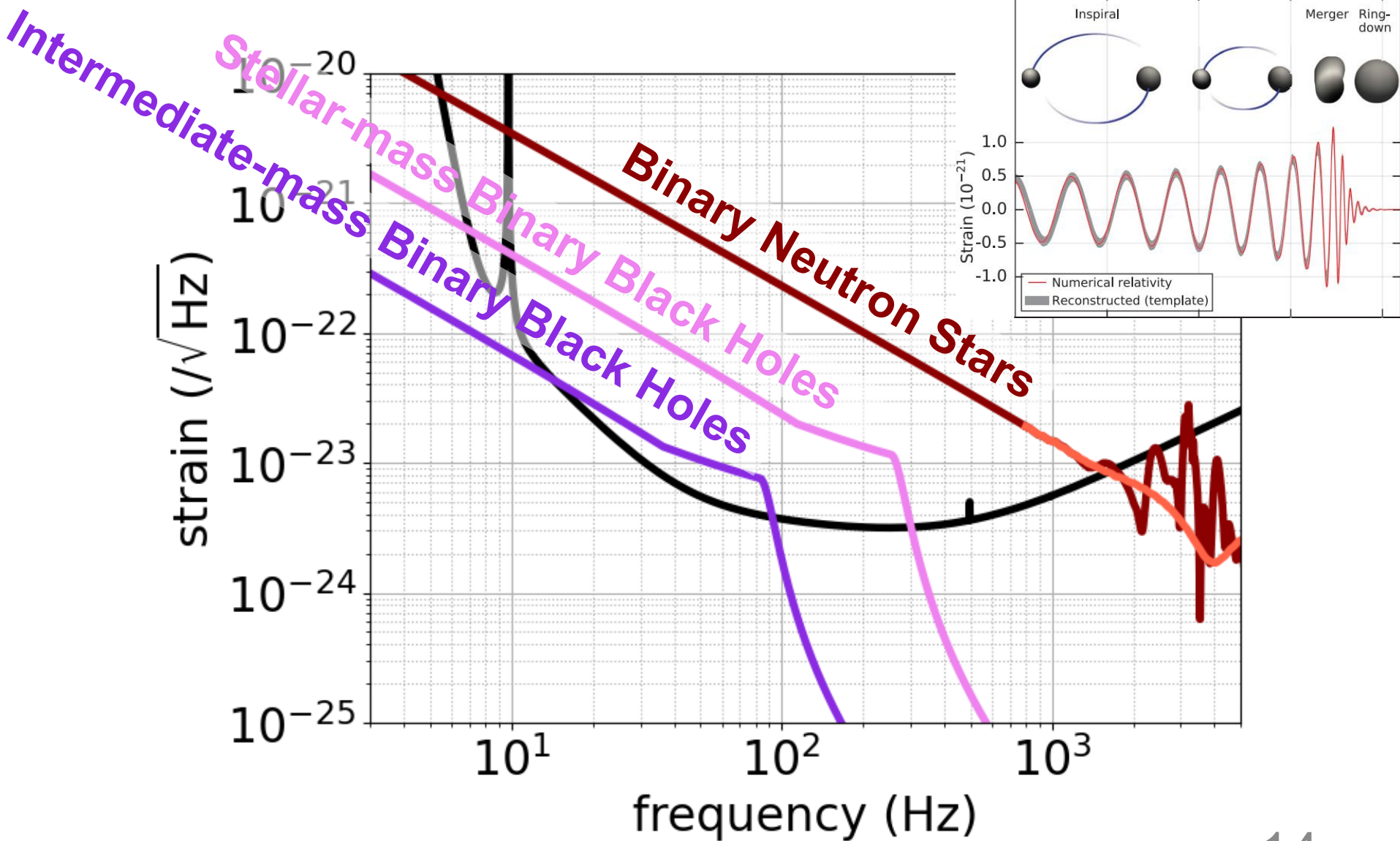
- **Coordinated runs** to detect GW signals by multiple detectors for better sky localization etc.



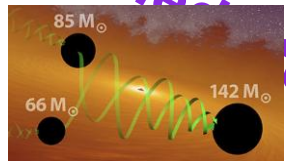
Sensitivity Band



Sensitivity Band and Science



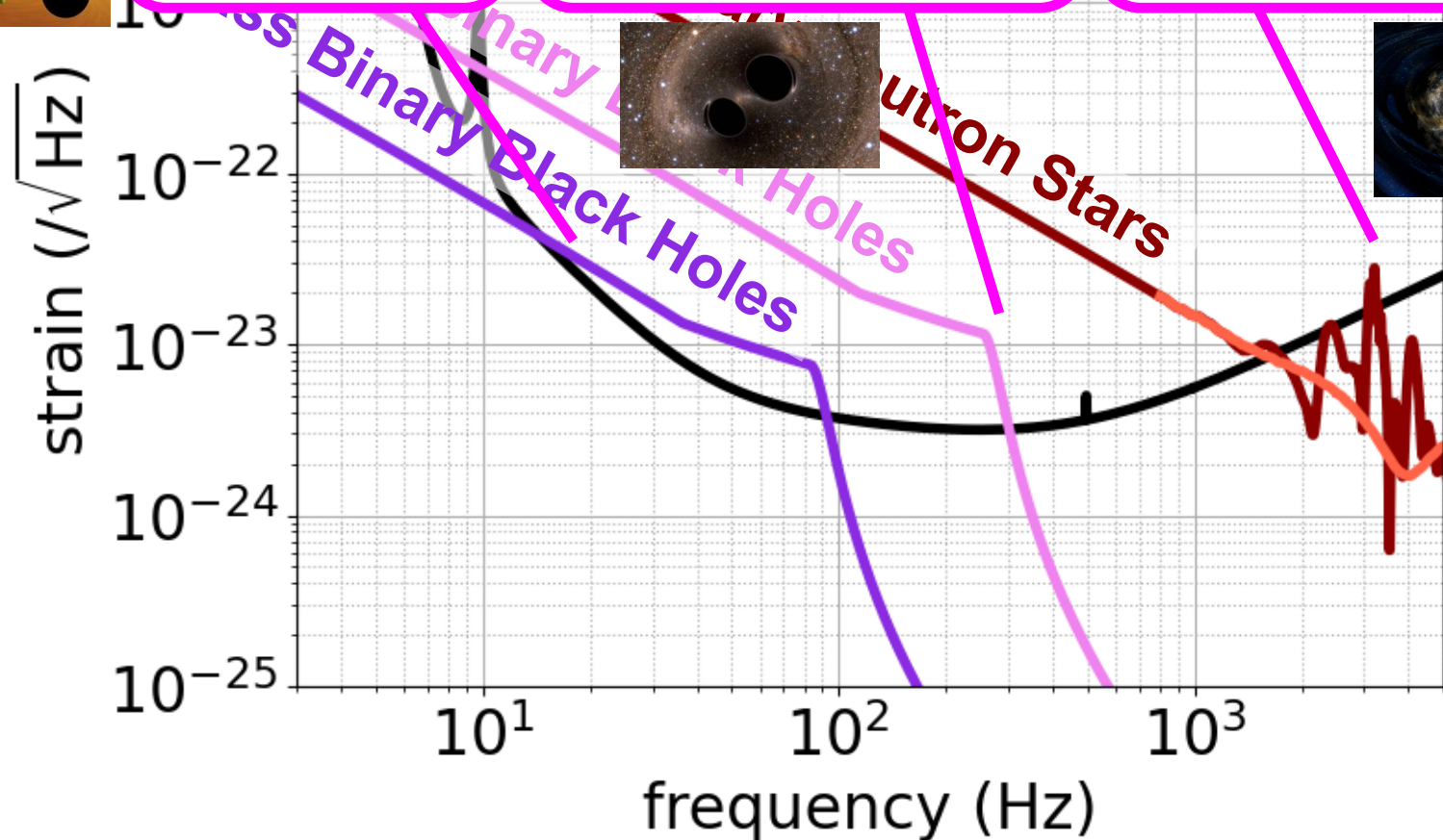
Sensitivity Band and Science



Origin of
heavy BHs

Ringdowns
Spins
Cosmic Expansion

Nuclear EoS
GRBs, Kilonovae
Heavy Elements

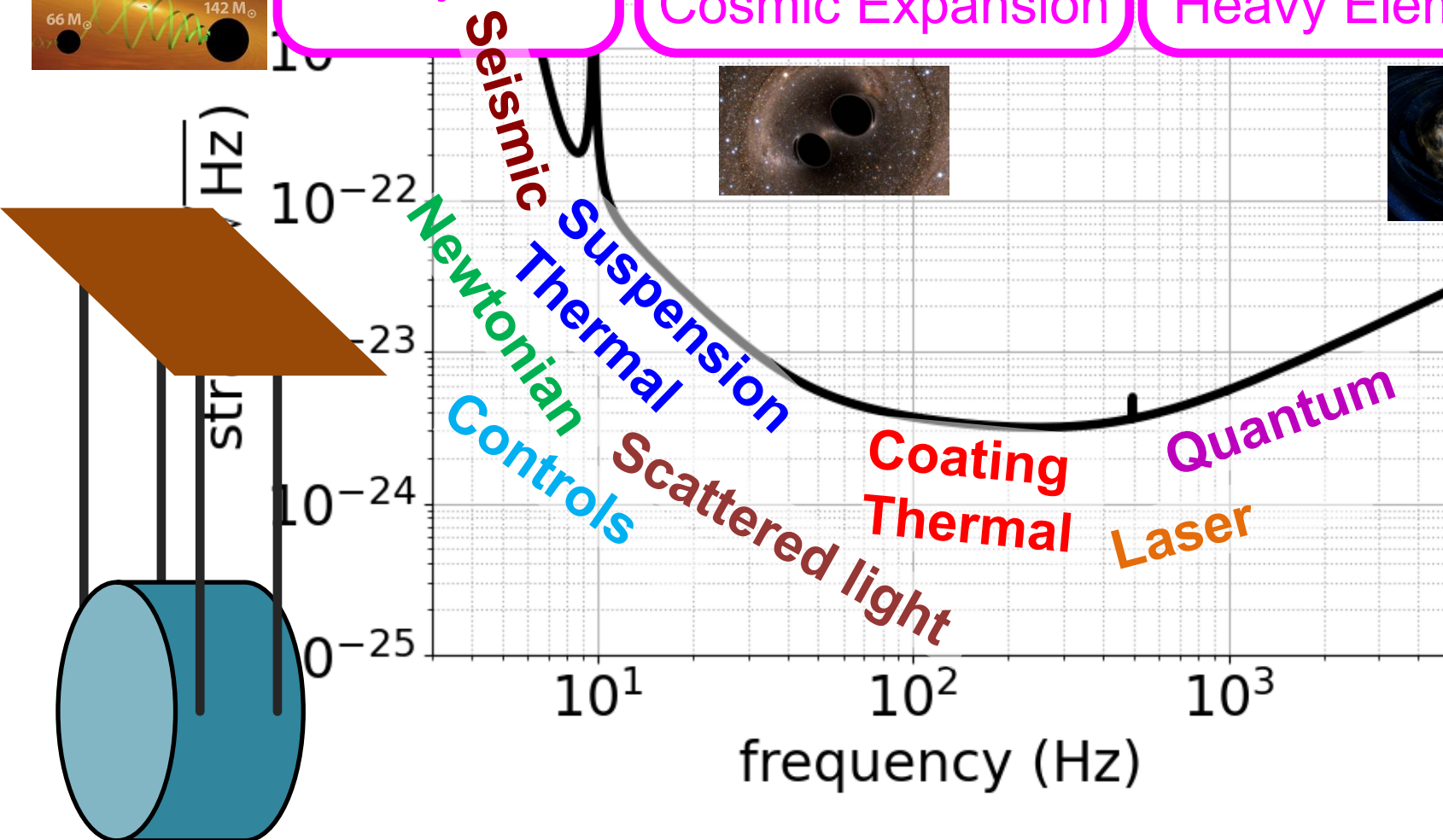
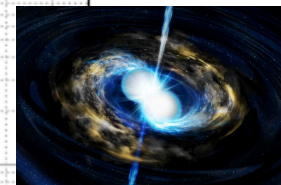
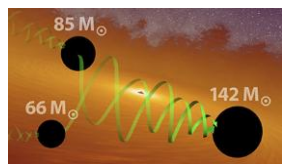


Limiting Noises

Origin of
heavy BHs

Ringdowns
Spins
Cosmic Expansion

Nuclear EoS
GRBs, Kilonovae
Heavy Elements

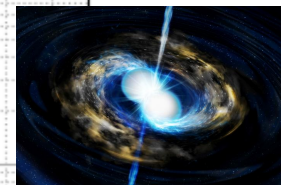
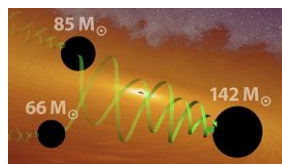


Noise Reducing Techniques

Origin of
heavy BHs

Ringdowns
Spins
Cosmic Expansion

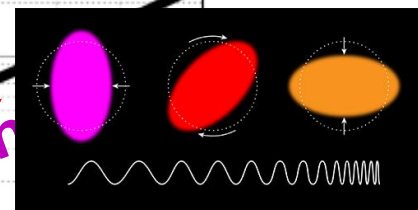
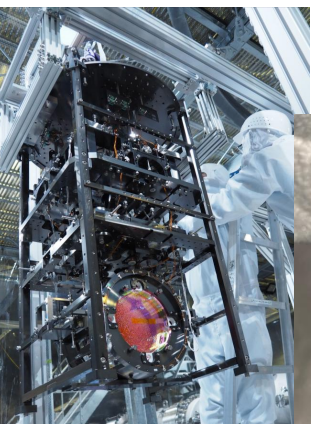
Nuclear EoS
GRBs, Kilonovae
Heavy Elements



Heavier Mirrors
Suspensions
Noise Cancellation
Machine Learning

Larger Mirrors
Coating Improvements
Cryogenics

Higher Power
Squeezing
(frequency dependent)

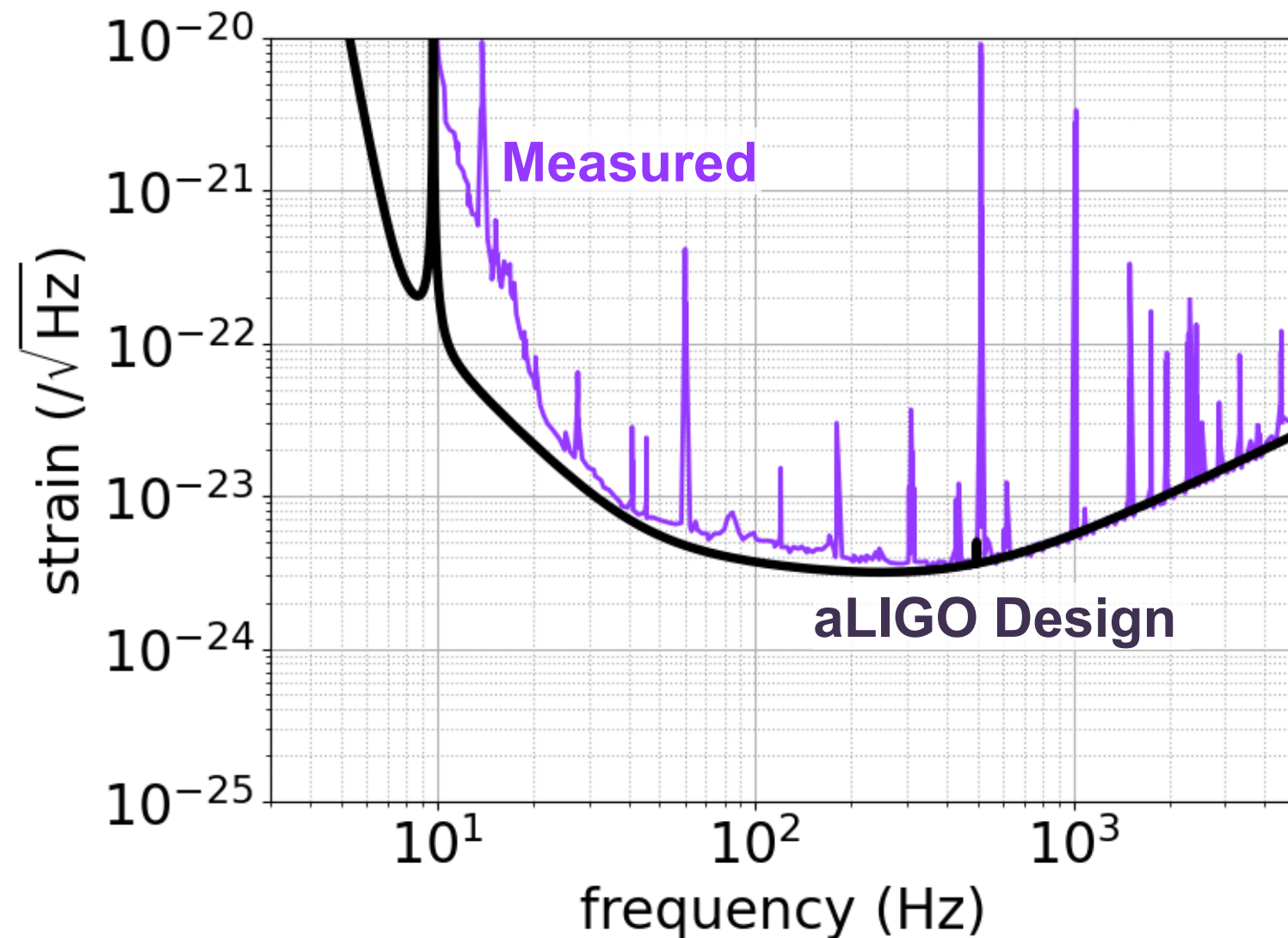


frequency (Hz)

[LIGO-G2200805](#)

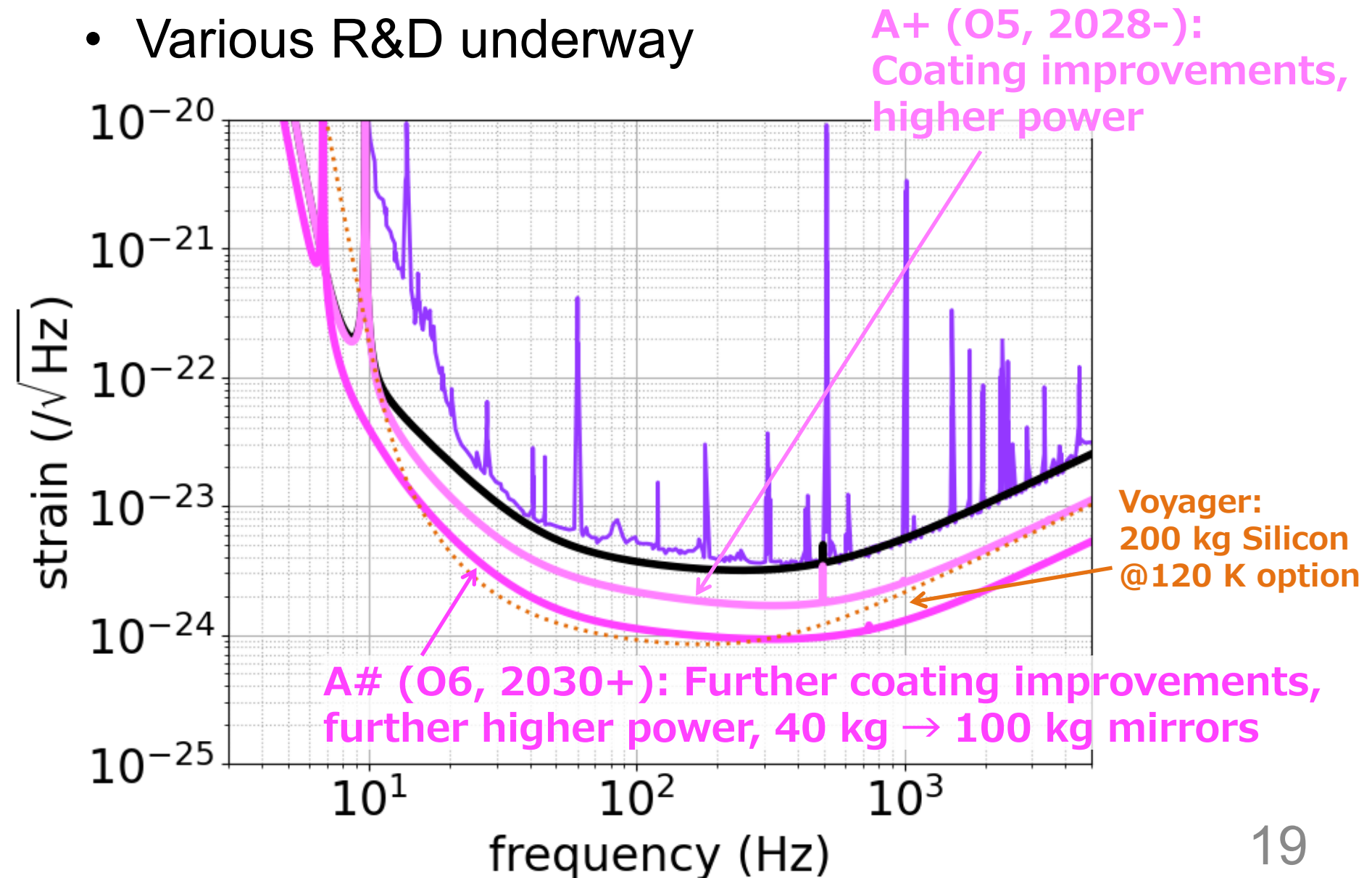
LIGO (US, 4 km, Room Temp.)

- Hanford & Livingston operating at ~150 Mpc



LIGO (US, 4 km, Room Temp.)

- Various R&D underway

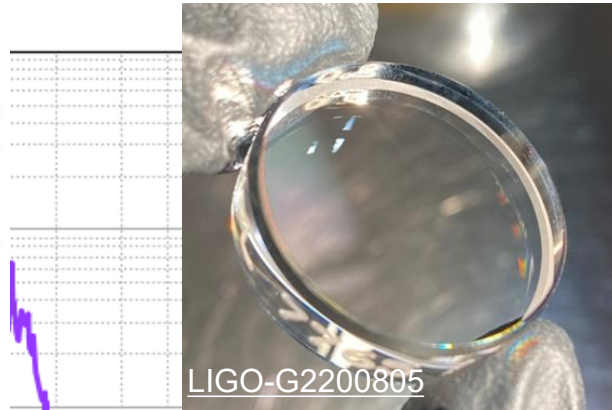
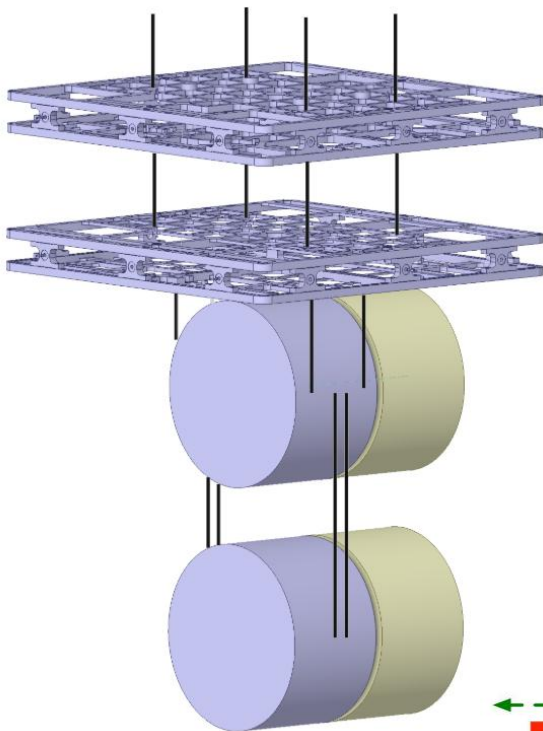


LIGO (US, 4 km, Room Temp.)

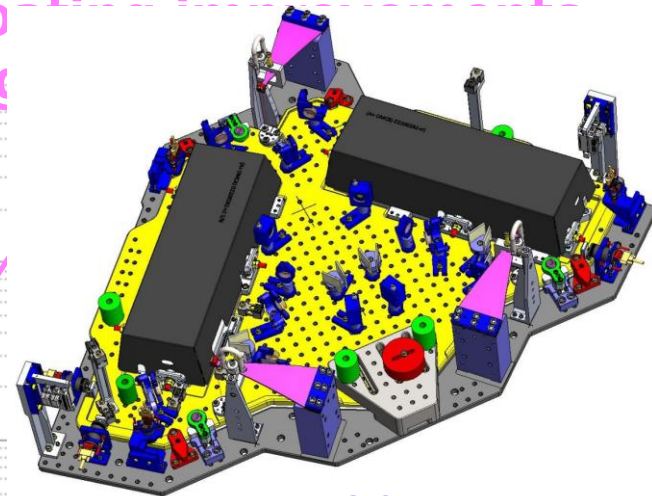
- Various R&D underway

A+ (O5, 2028-):

Co
high

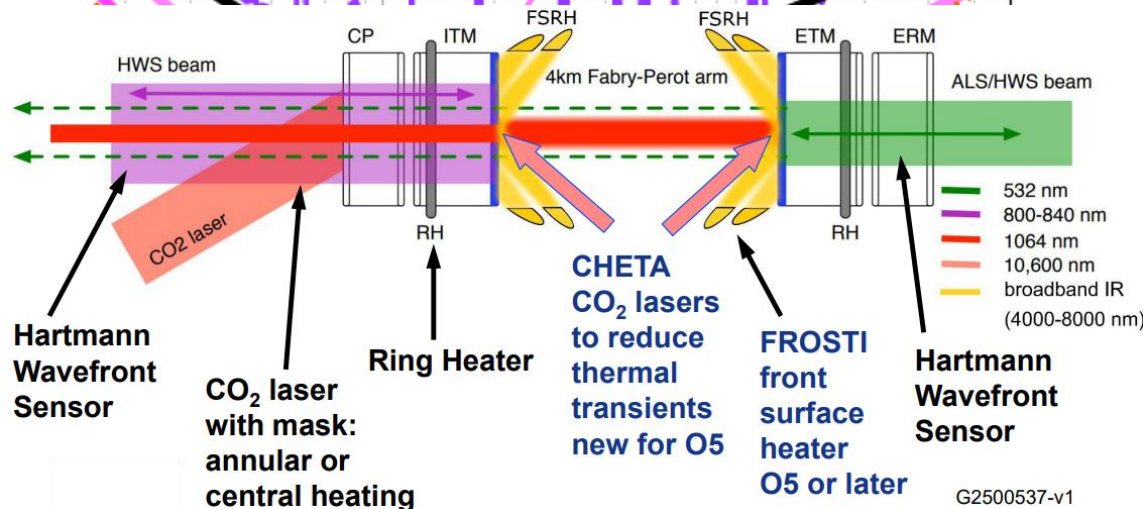
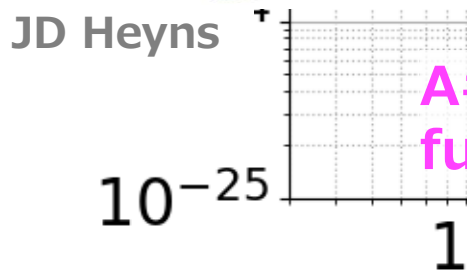


LIGO-G2200805



LIGO-T2100318

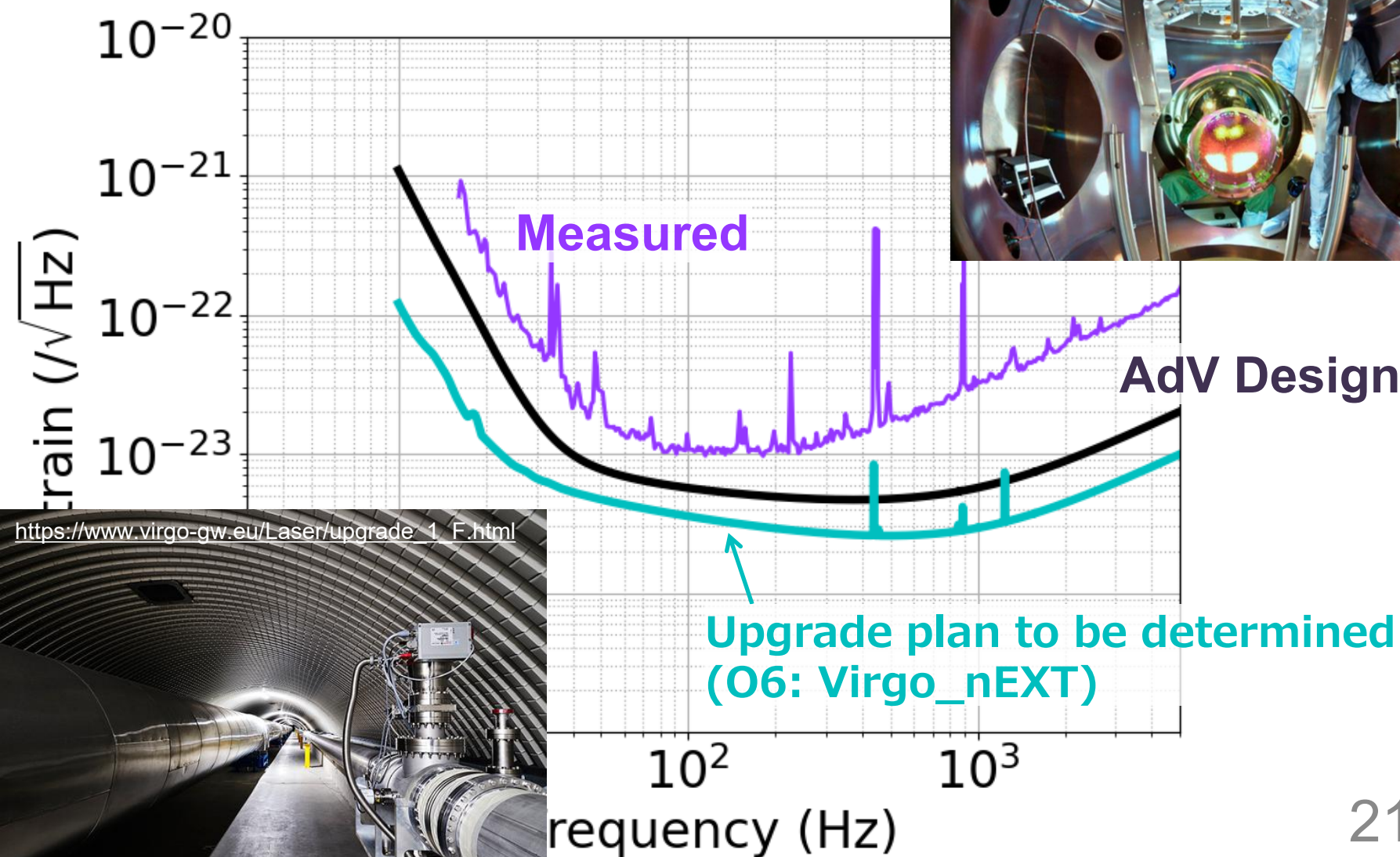
Voyager:
kg Silicon
0 K option



nents,
rors

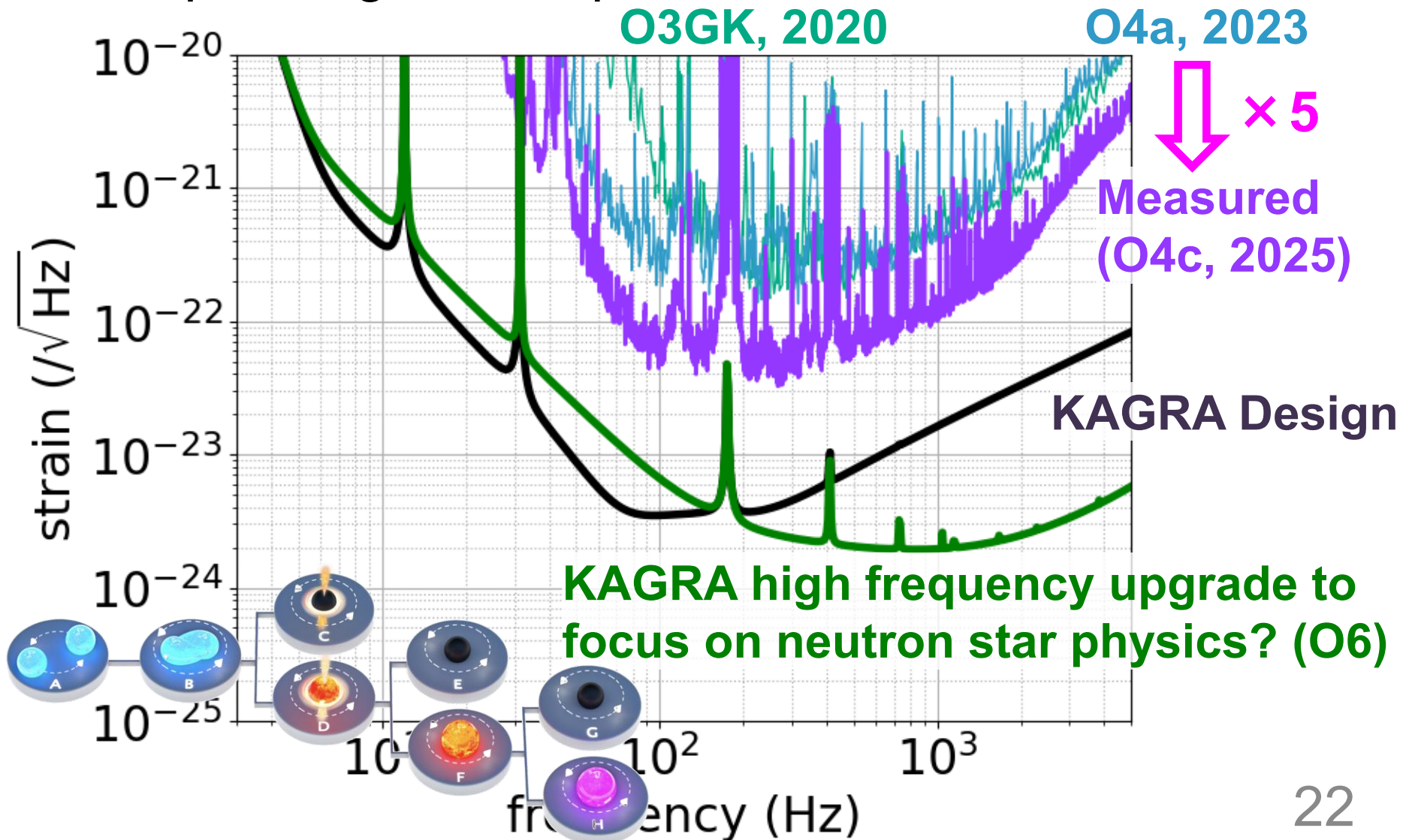
Virgo (Italy, 3 km, Room Temp.)

- Operating at ~50 Mpc



KAGRA (Japan, 3 km, 22 K)

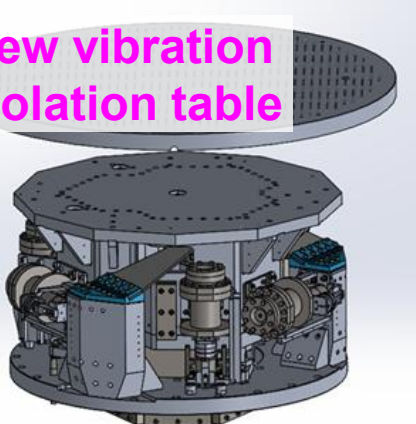
- Operating at ~ 7 Mpc at ~ 50 K (IX ~ 90 K)



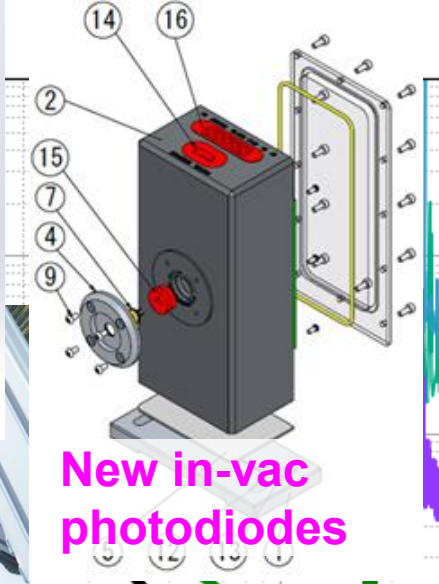
KAGRA (Japan, 3 km, 22 K)

- Various efforts to improve sensitivity

New vibration isolation table



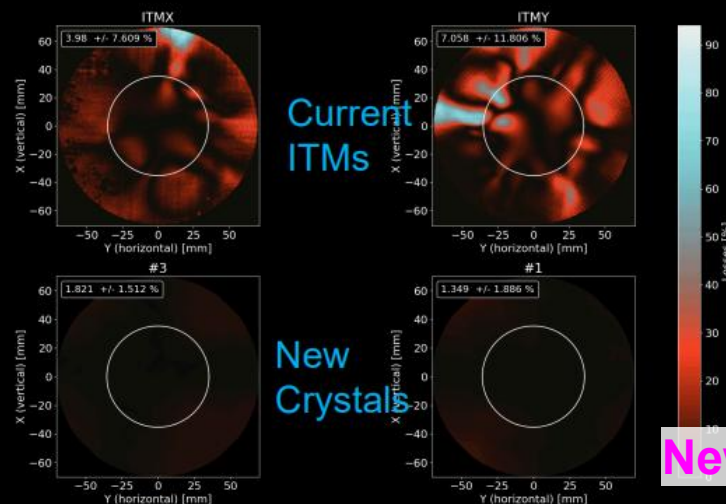
New in-vac photodiodes



Scattered light mitigations



Polarization conversion losses

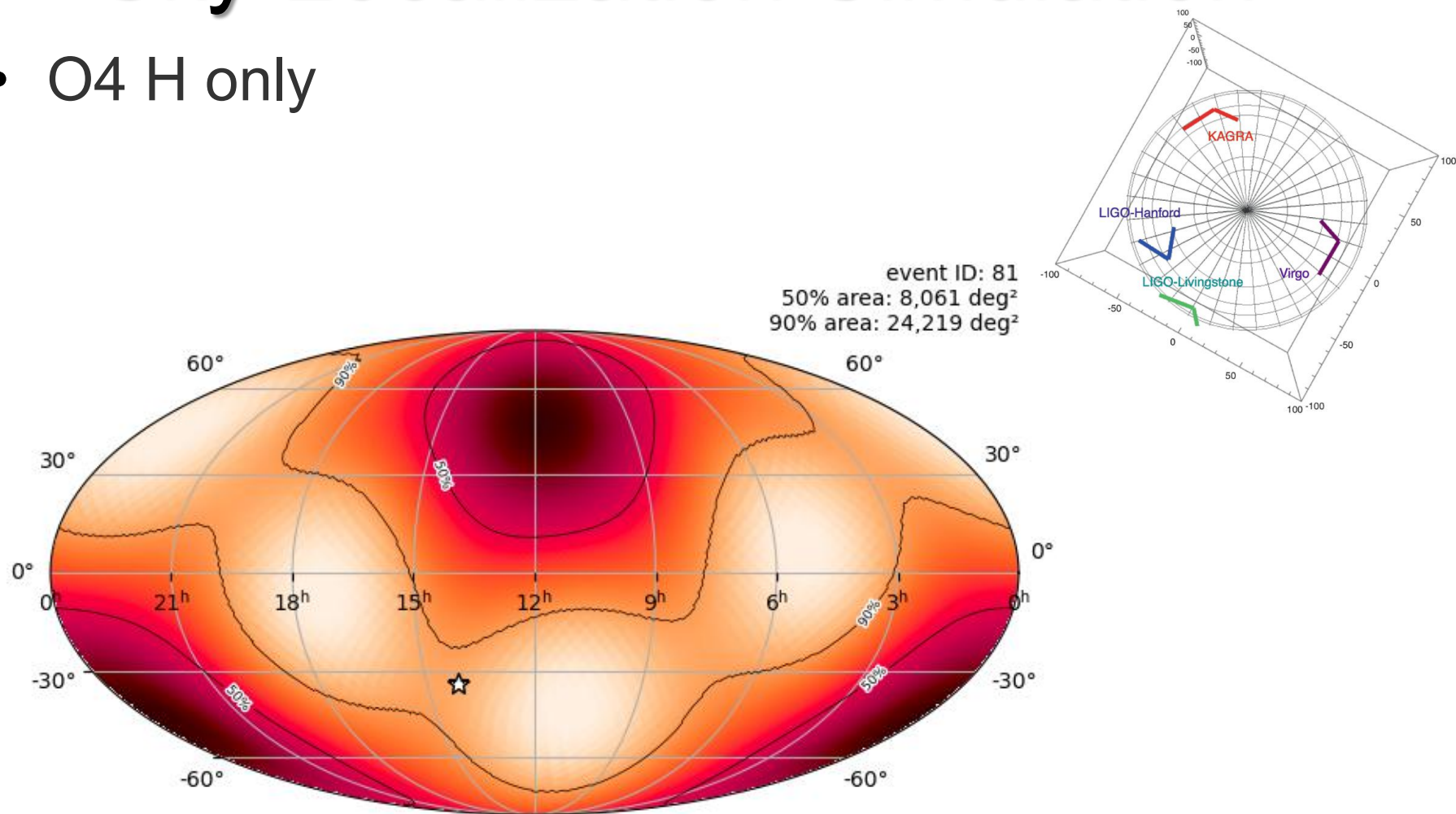


New sapphire mirrors



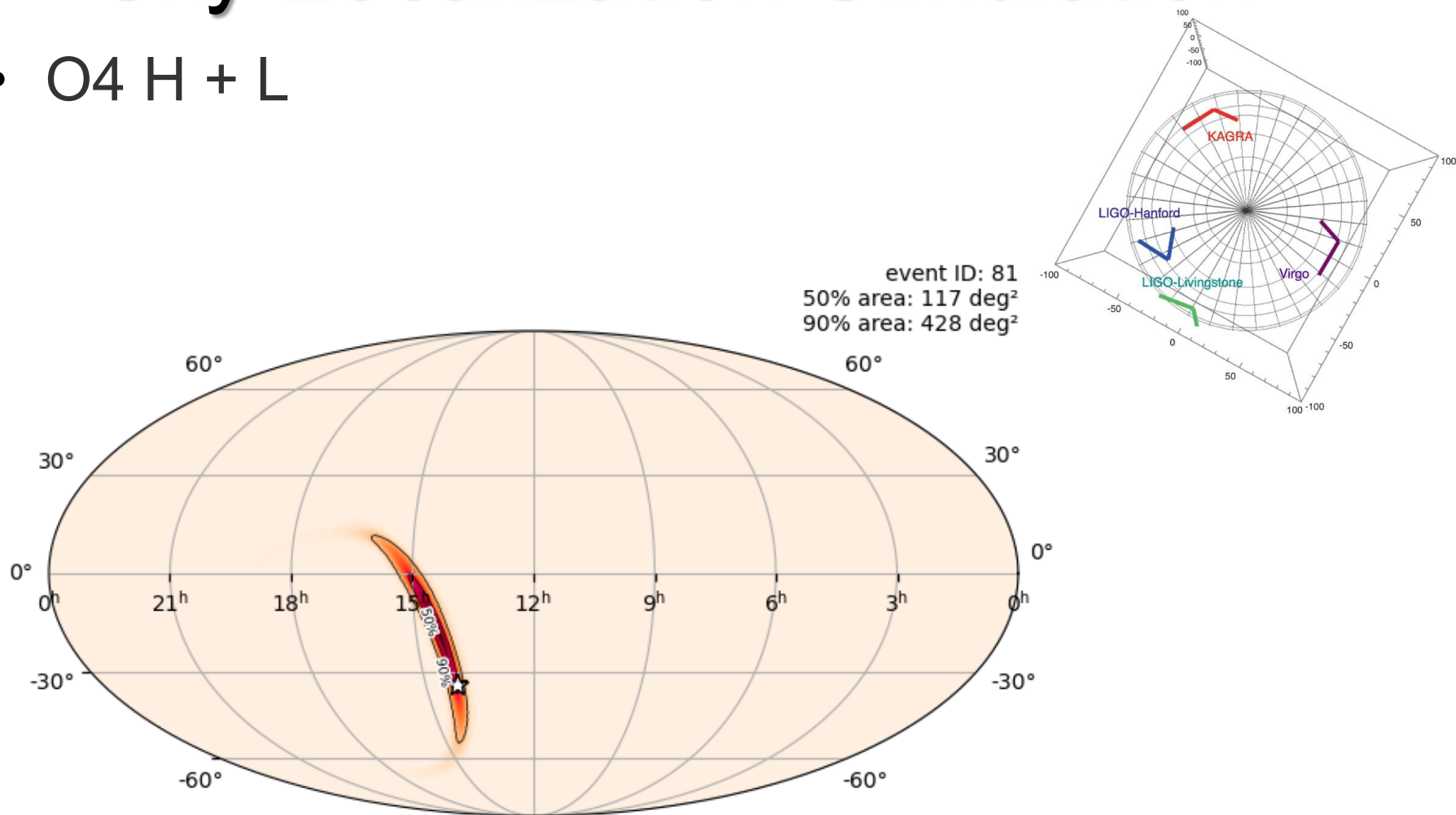
Sky Localization Simulation

- O4 H only



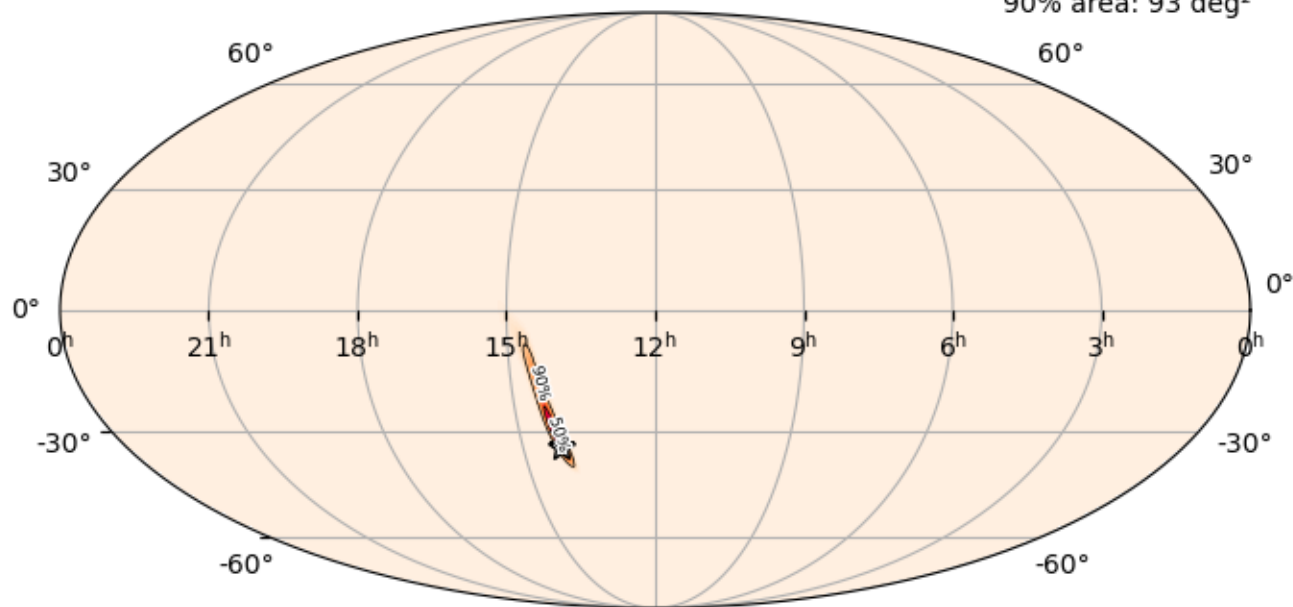
Sky Localization Simulation

- O4 H + L

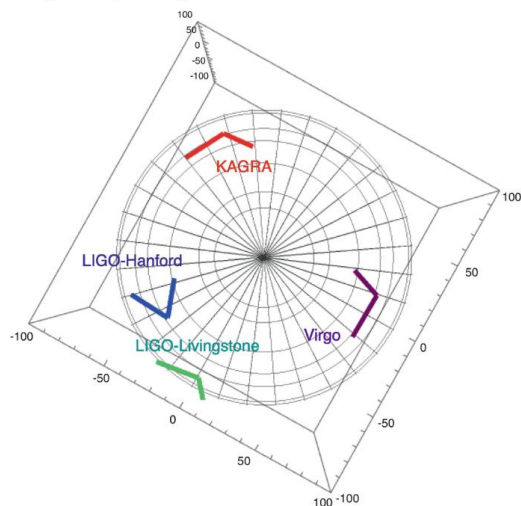


Sky Localization Simulation

- O4 H + L + V

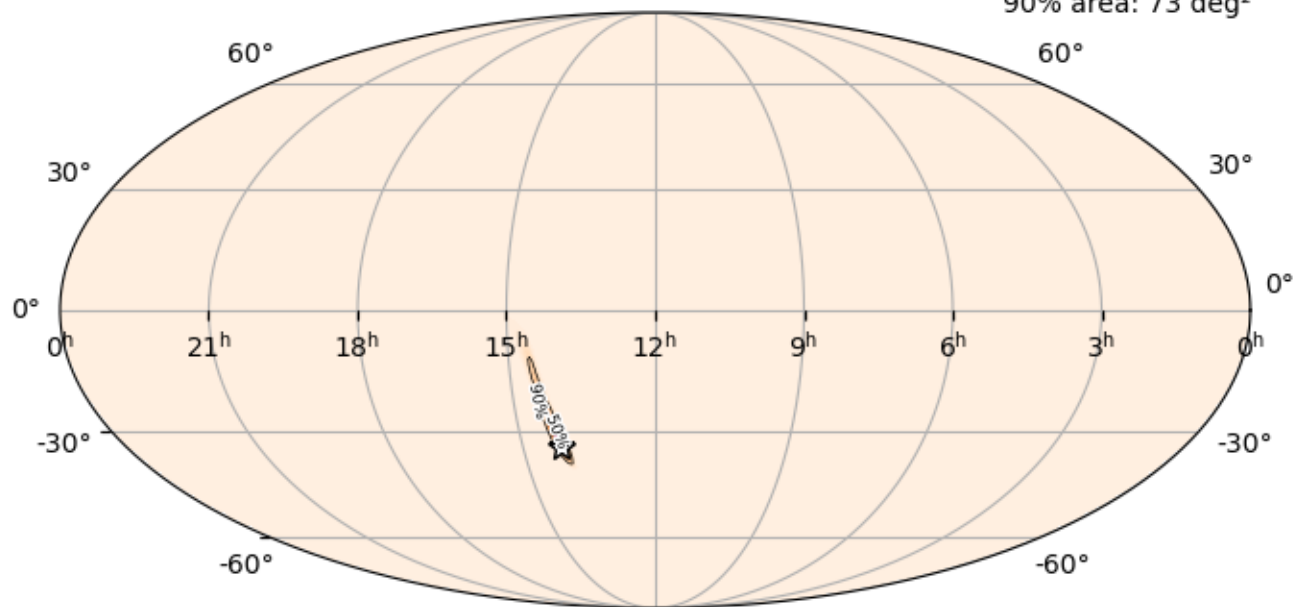


event ID: 81
50% area: 22 deg²
90% area: 93 deg²

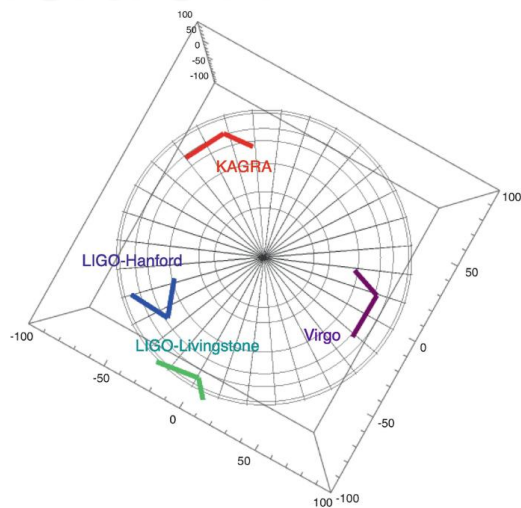


Sky Localization Simulation

- O4 H + L + V + K(10 Mpc)

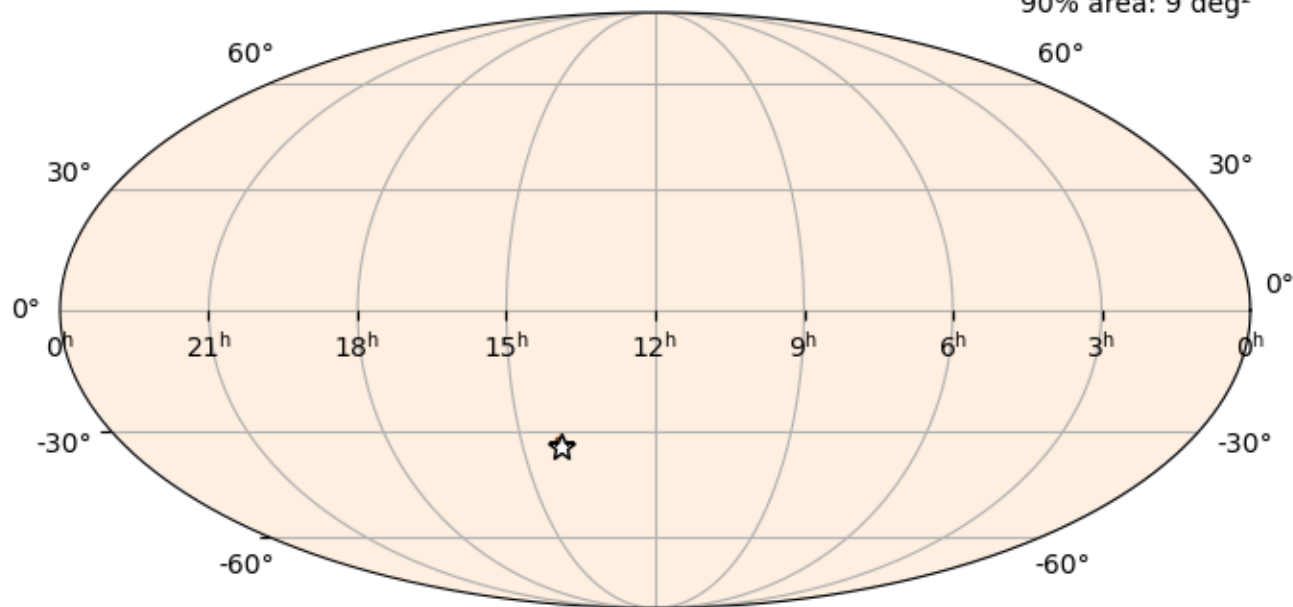


event ID: 81
50% area: 14 deg²
90% area: 73 deg²

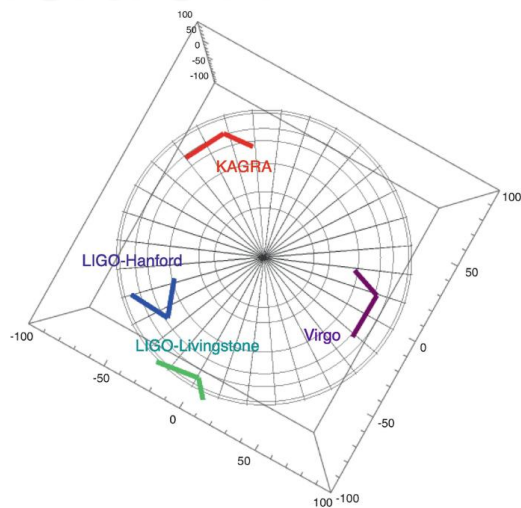


Sky Localization Simulation

- O4 H + L + V + K(25 Mpc)

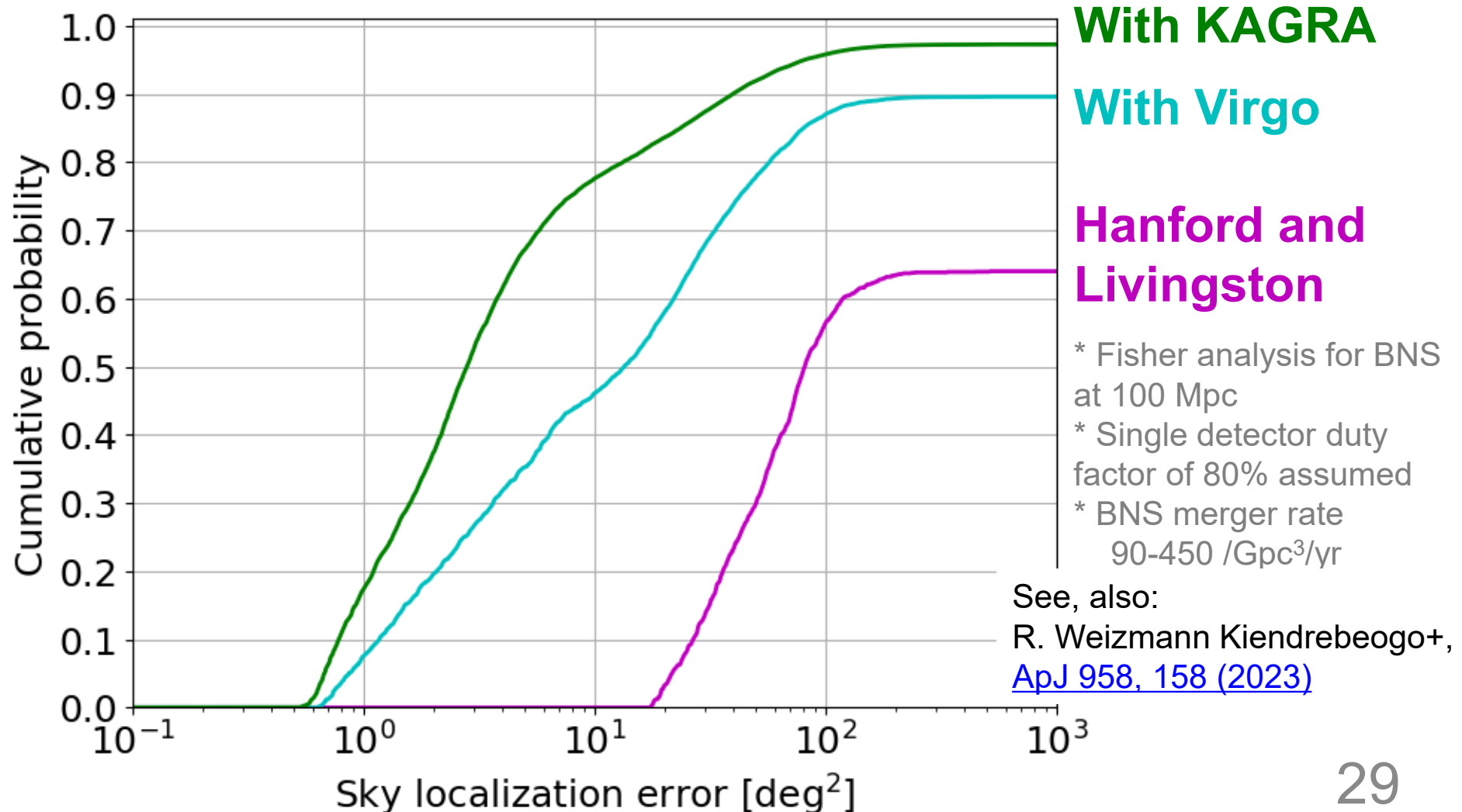


event ID: 81
50% area: 2 deg²
90% area: 9 deg²



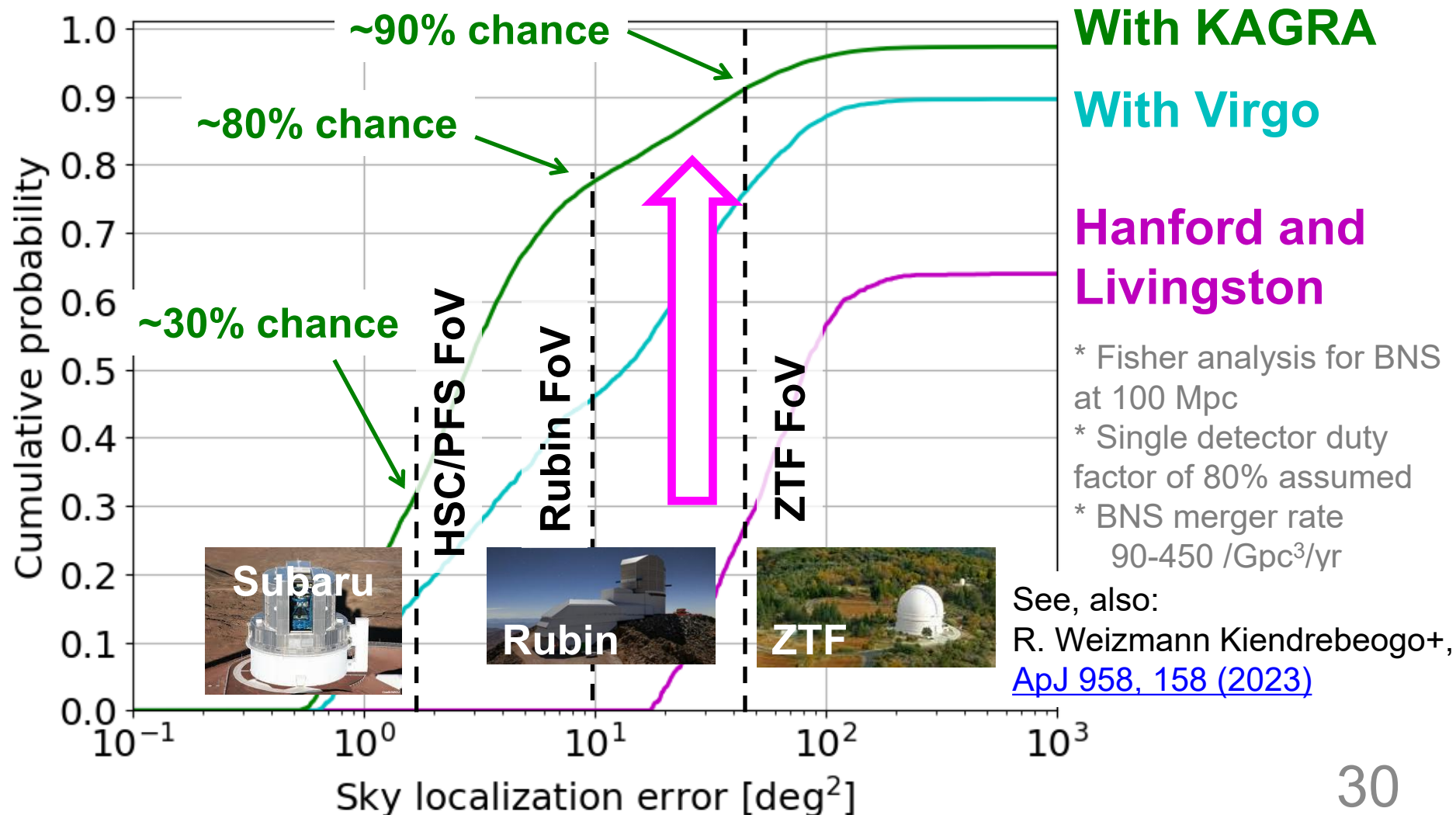
Sky Localization in O5 (2028~)

- 1~5 BNS detections per year localized $< 10 \text{ deg}^2$



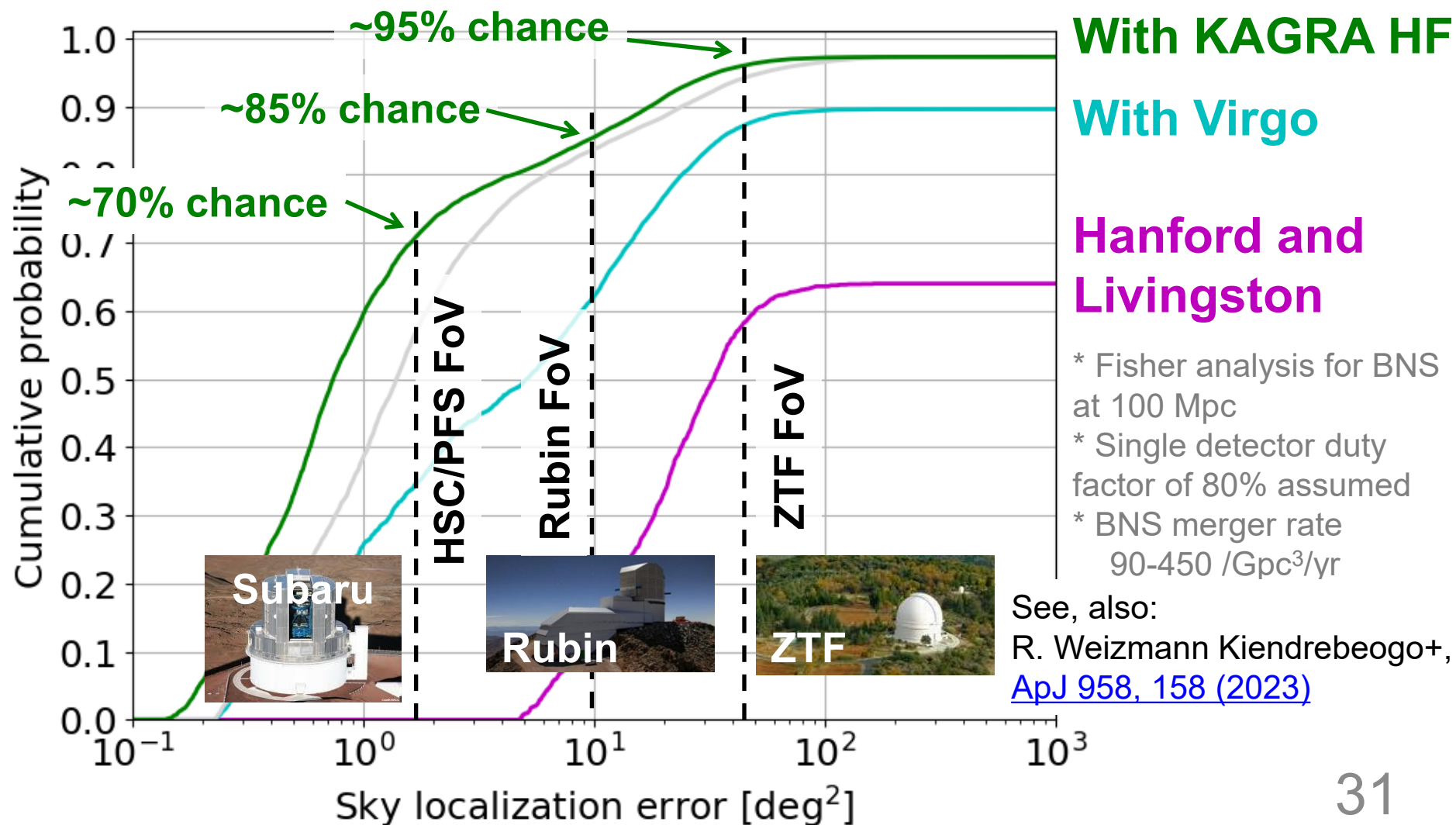
Sky Localization in O5 (2028~)

- 1~5 BNS detections per year localized $< 10 \text{ deg}^2$



Sky Localization in O6 (2030+)

- 5~23 BNS detections per year localized $< 10 \text{ deg}^2$



LIGO-India (4 km, Room Temp.)

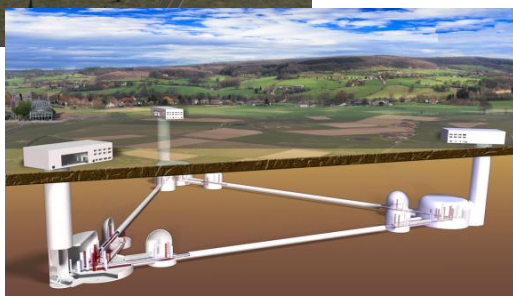
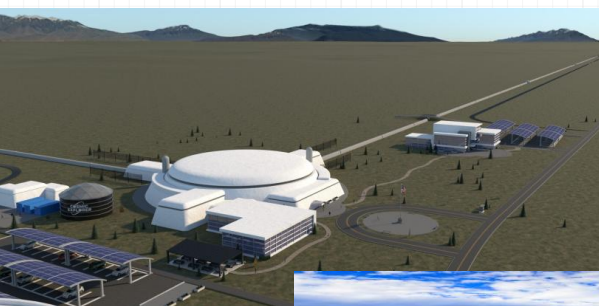
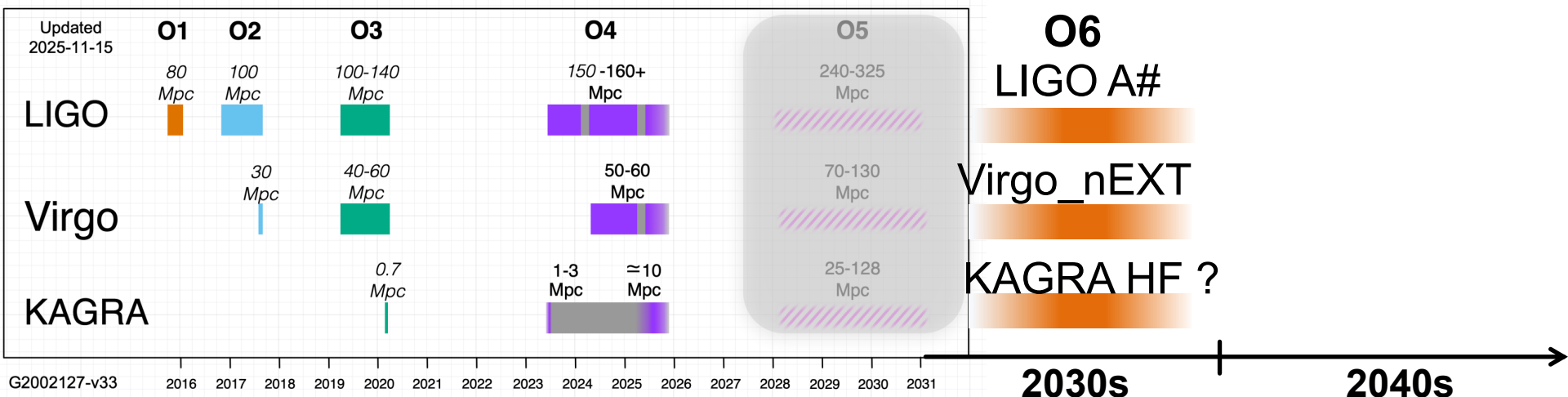
- Aundha **site acquired** in May 2023
- Being built as the Advanced LIGO configuration
- Aim to be operational in the **early 2030s**



**10 m prototype at RRCAT
being built for testing
and training**

Next Generation Detectors

- Next generation detectors coming in **late 2030s**, **with space-based** detectors (multi-band!)



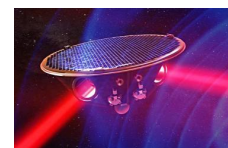
LIGO India

Cosmic Explorer

Einstein Telescope

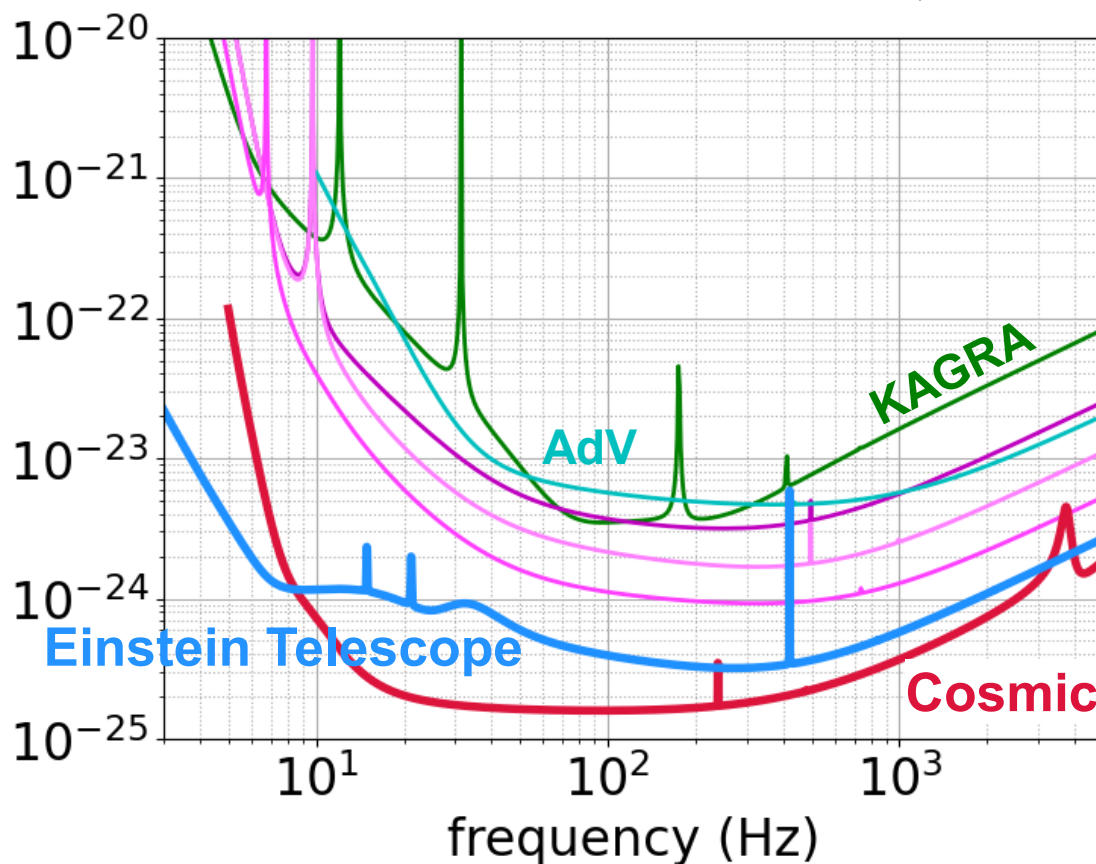
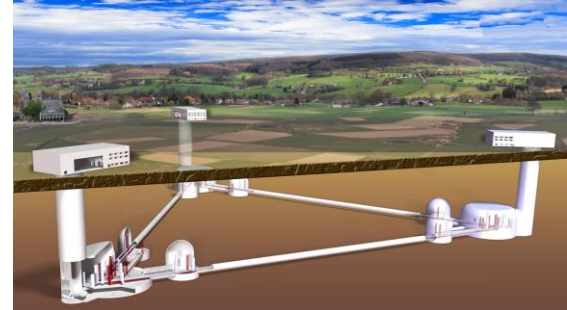
B-DECIGO

LISA

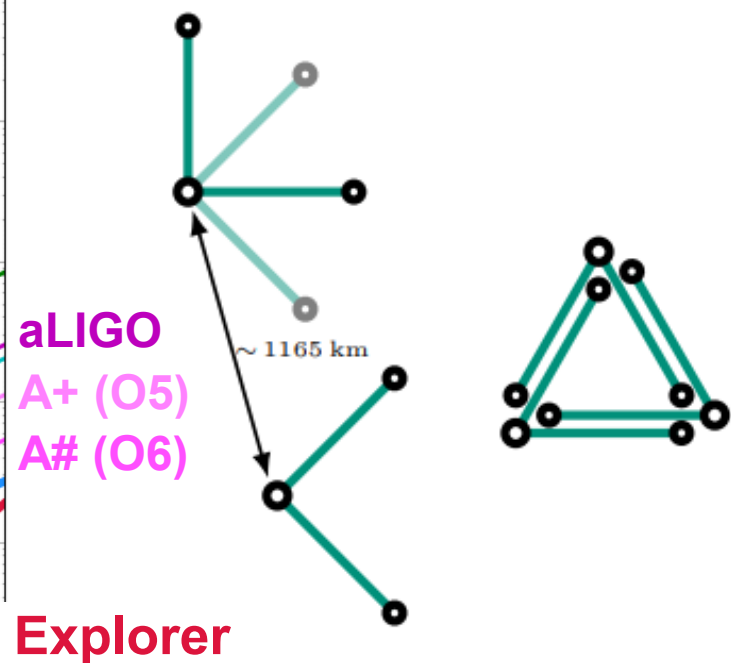


Einstein Telescope

- Xylophone configuration
 - 10 K silicon interferometer for low frequency
 - Room temp. fused silica interferometer for high frequency
- 10 km Δ or two 15 km L, underground



Branchesi+, [JCAP 07, 068 \(2023\)](#)



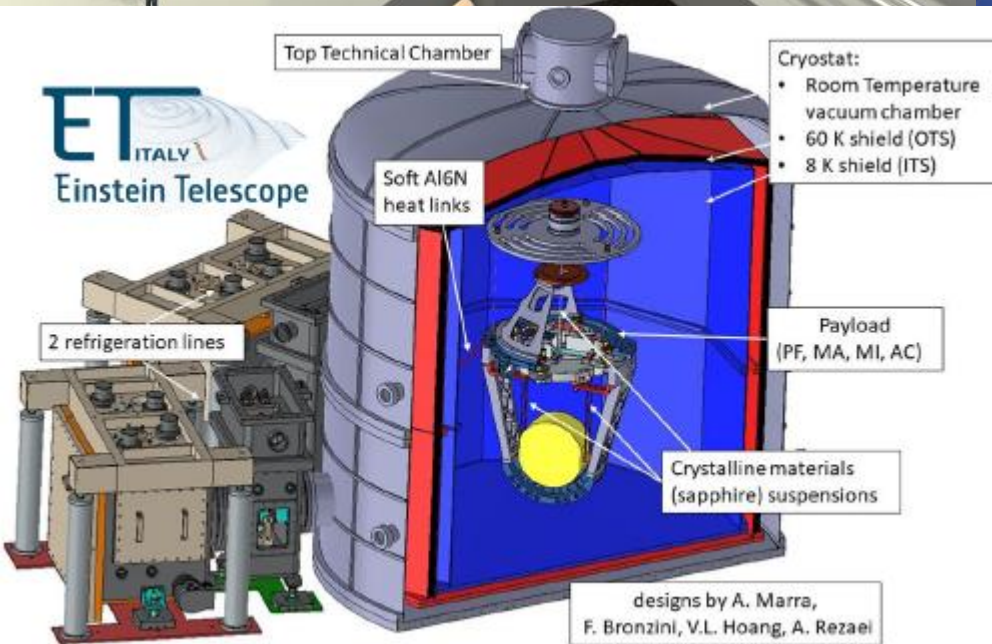


Layout studies

ETpathfinder in Maastricht

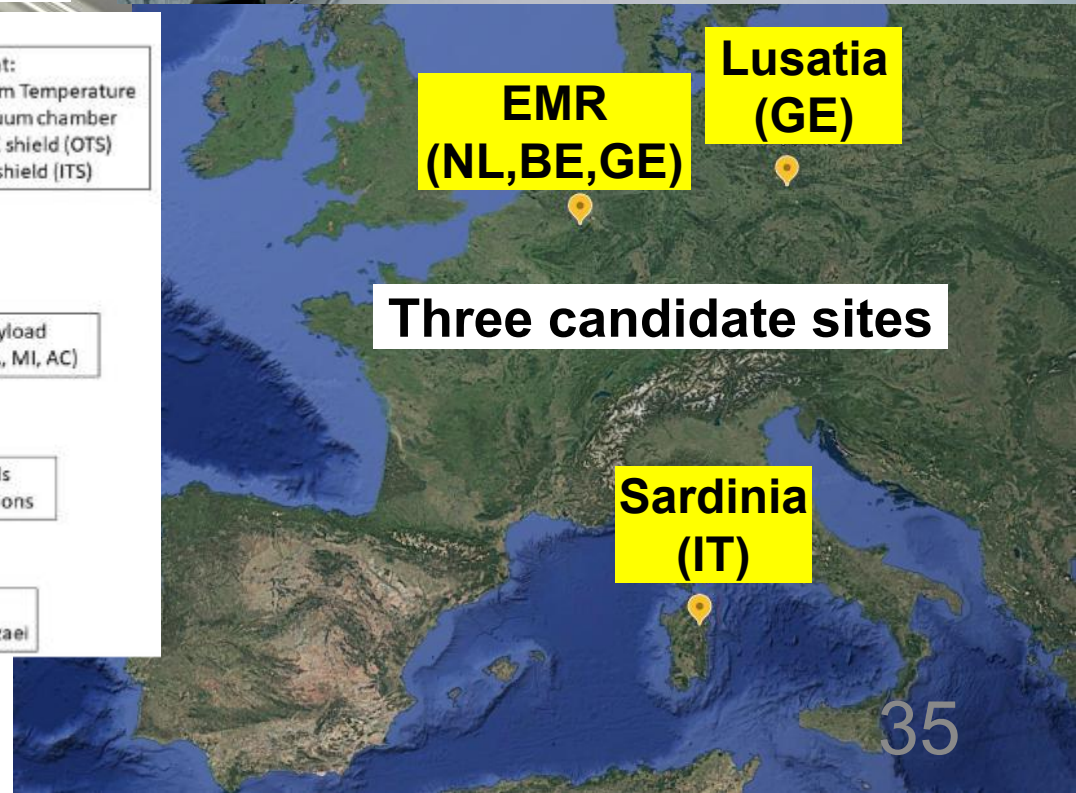


<https://www.etpathfinder.eu/gallery/>



Cryogenic payload in Rome

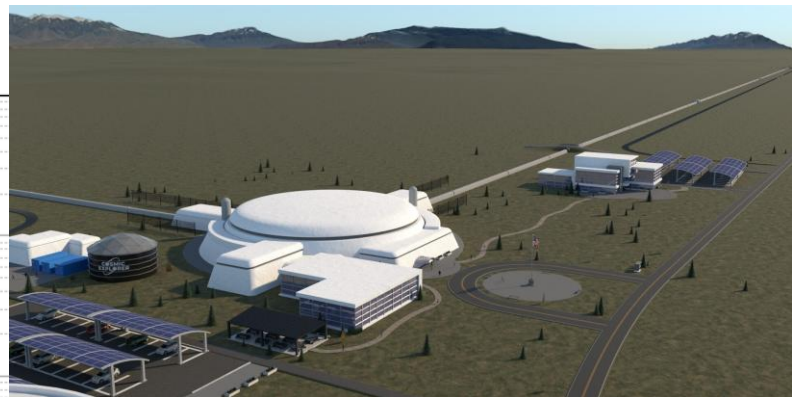
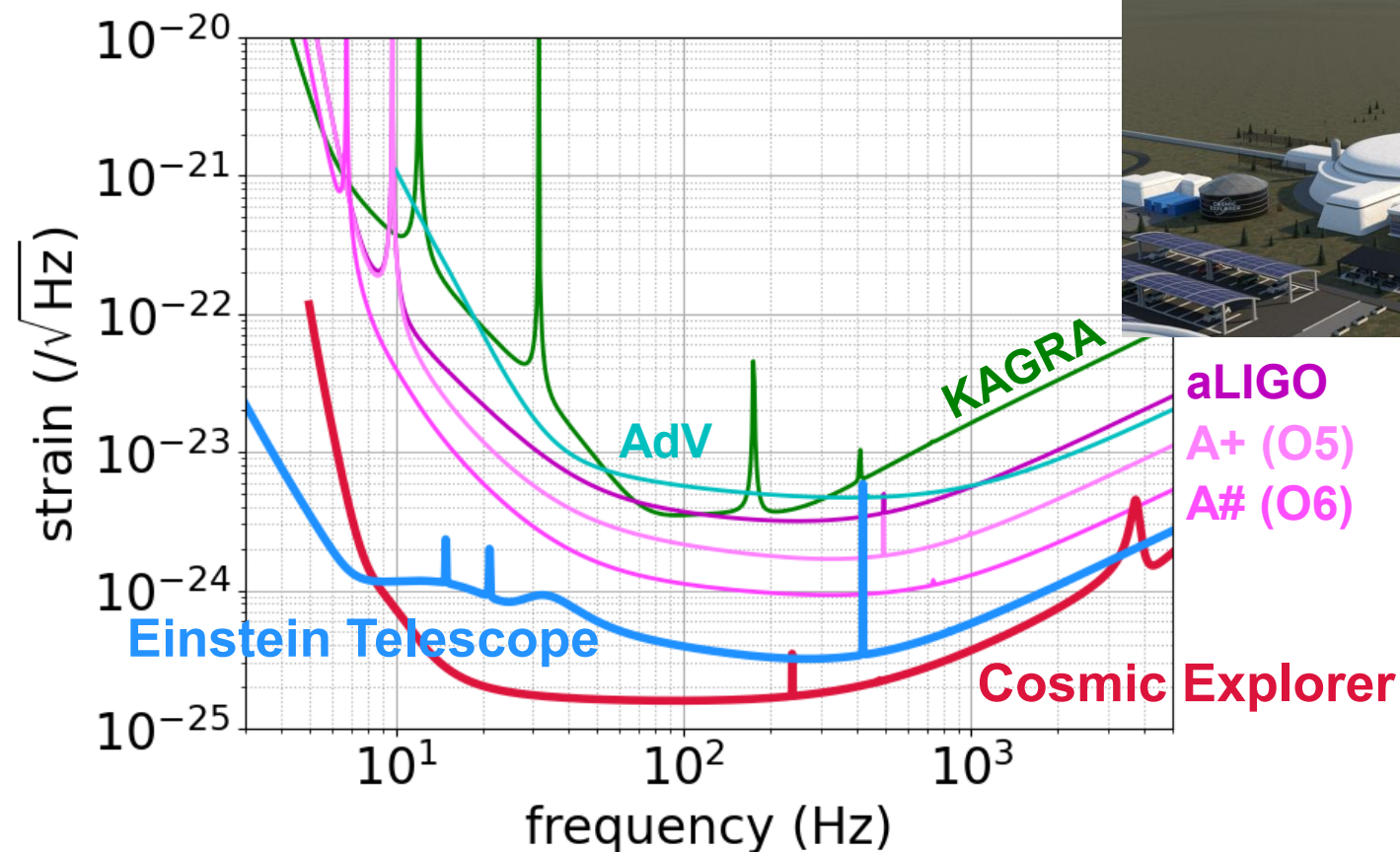
From L. Naticchioni (GWADW2025)

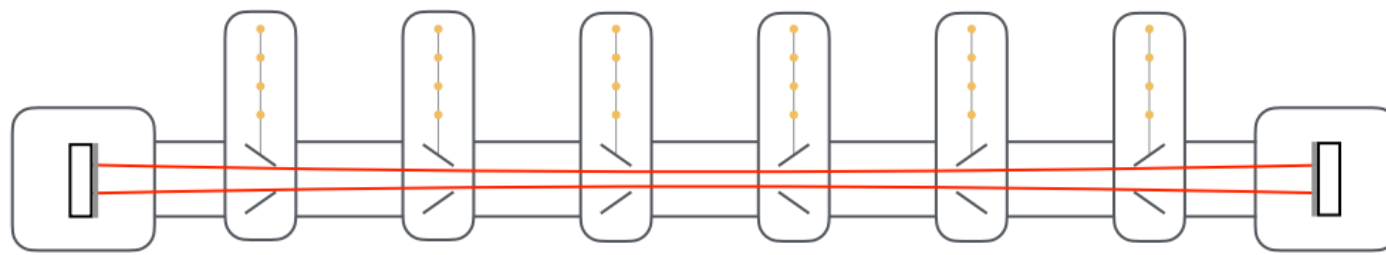


Three candidate sites

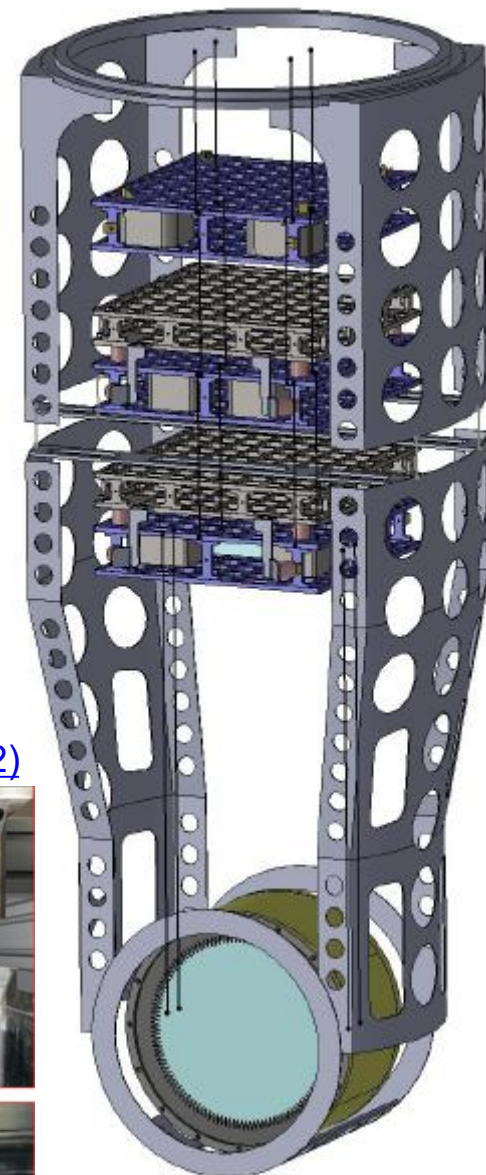
Cosmic Explorer

- 40 km and 20 km L-shaped
 - 40 km only if ET in Europe
- Room temp. fused silica (technical overlap with A#)



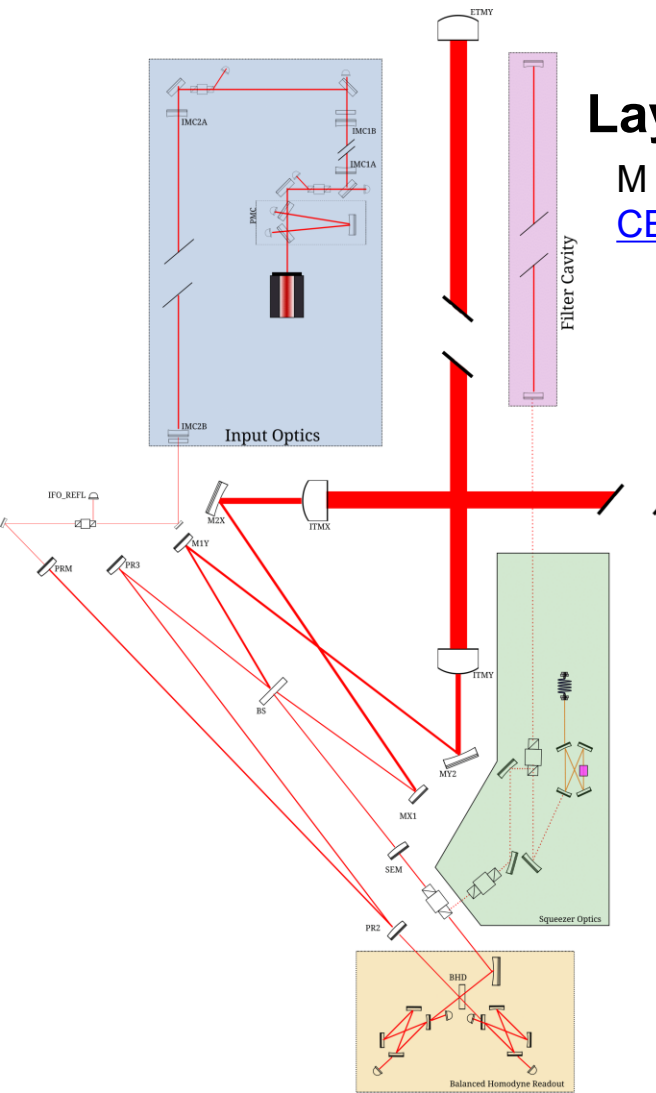


Stray light mitigation



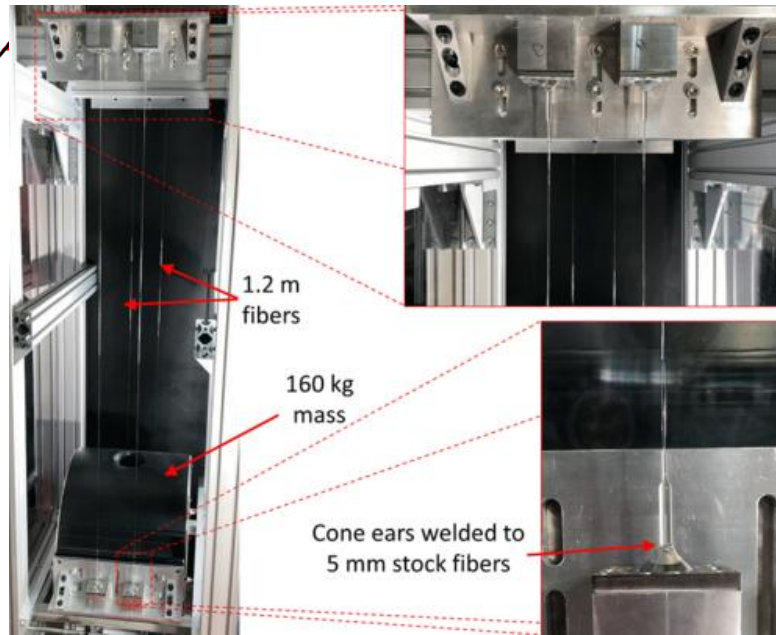
Layout studies

M Todd,
[CE-G2500002](#)



Heavy suspension tests

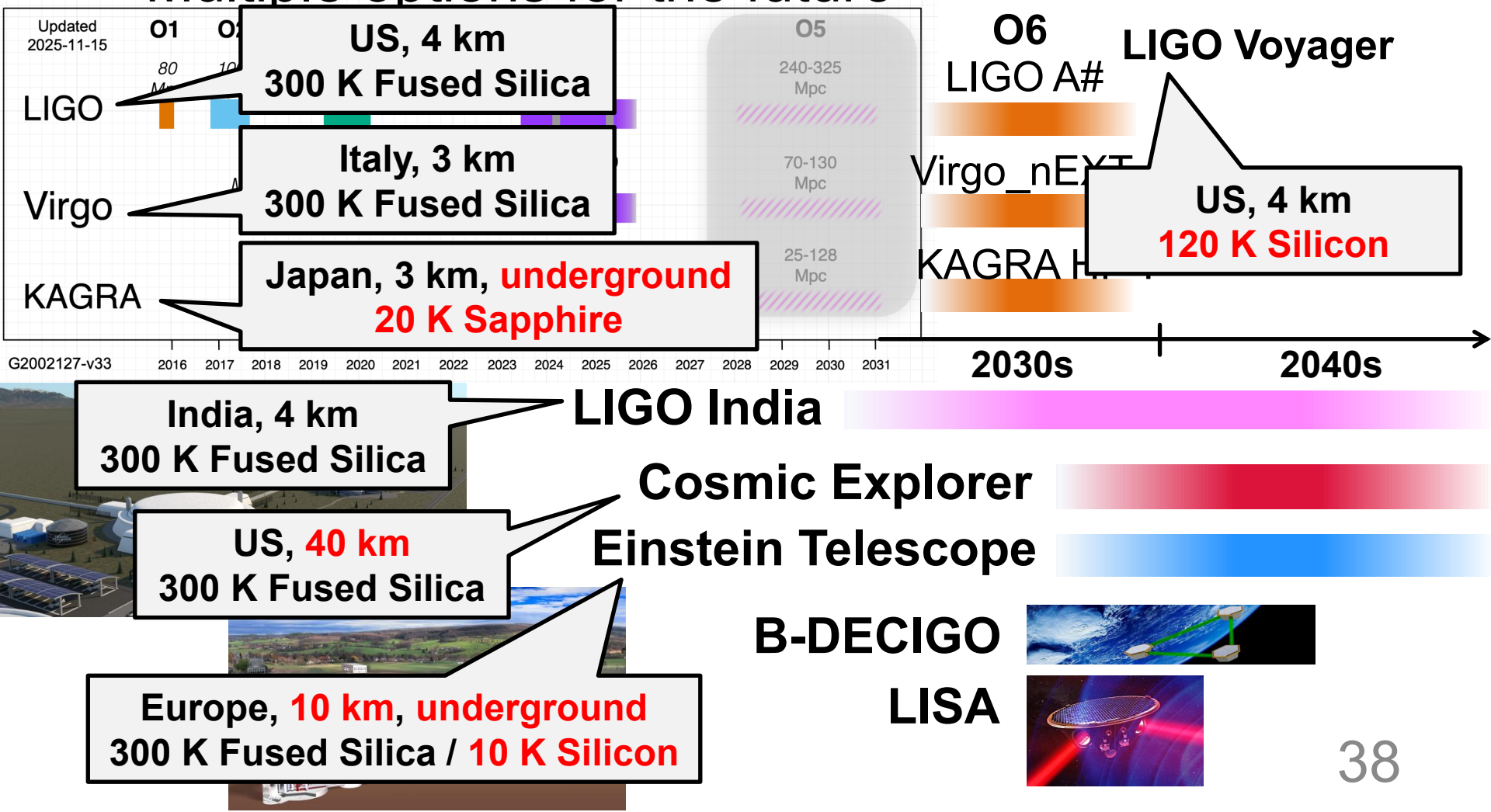
Cumming+, [PRApplied 17, 024044 \(2022\)](#)



From M. Evans
 (GWADW2025)

Different Strategies

- Different strategies for different detectors
- Multiple options for the future



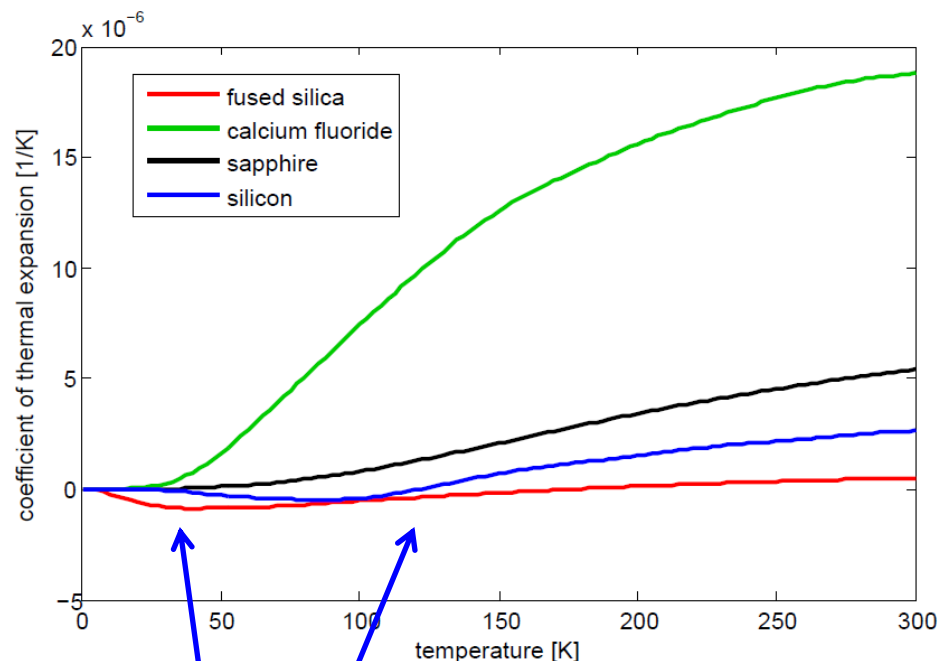
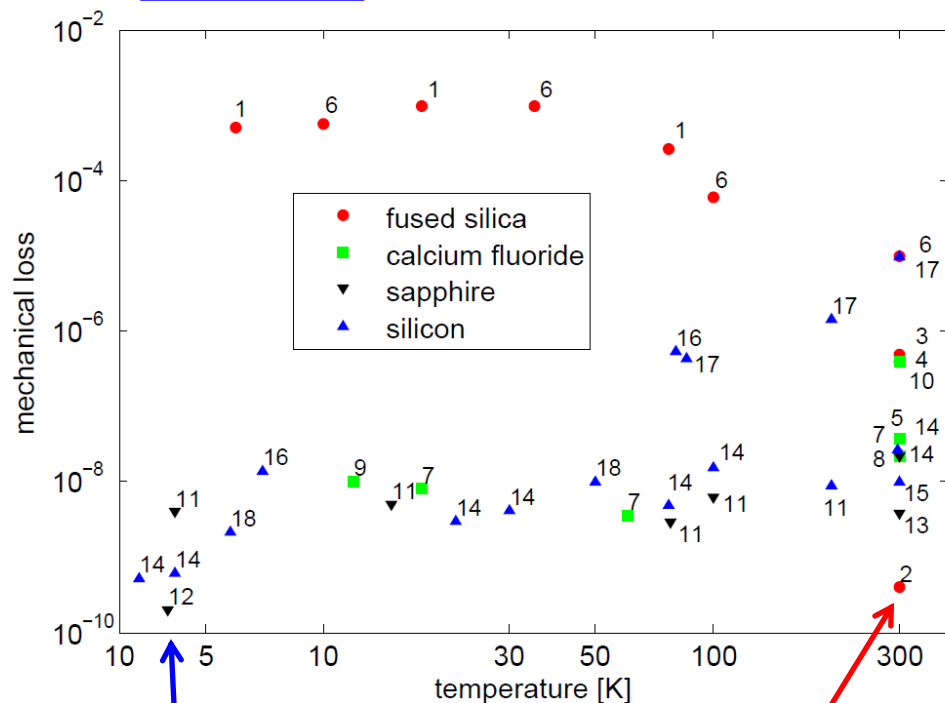
Why Different Mirror Materials?

- Thermal noise $\propto \sqrt{T\phi}$

Temperature

Mechanical loss angle
(temperature dependent)

[ET-027-09](#)



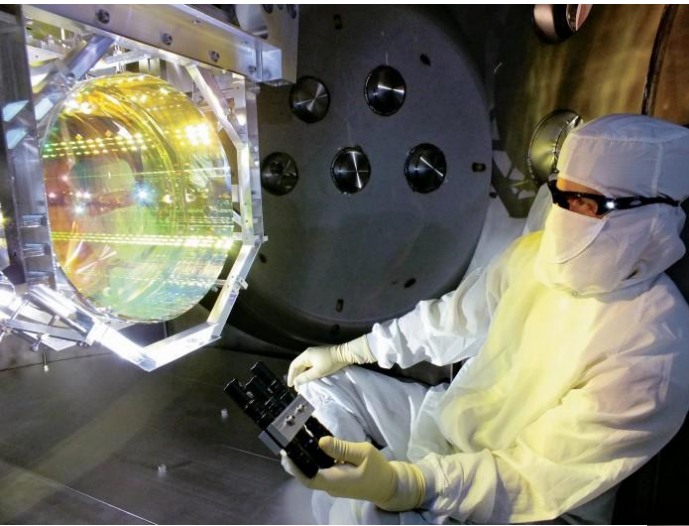
Sapphire / silicon
is good at
cryogenic temp.

Fused silica
is good at
room temp.

Silicon has zero
thermal expansion
at 18 K and 123 K

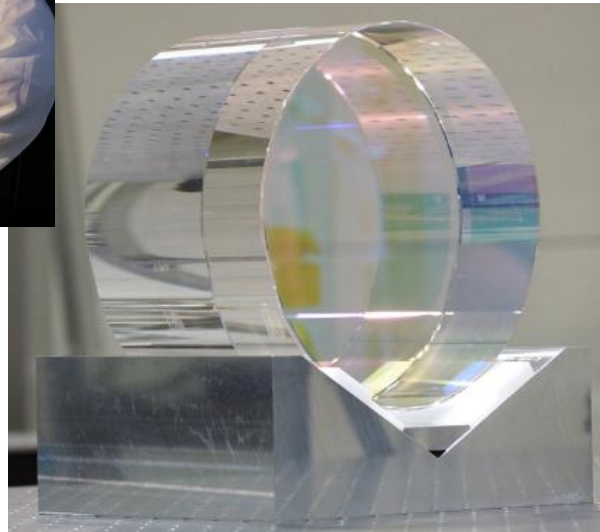
Different Wavelengths

- Different mirror materials require different laser wavelengths

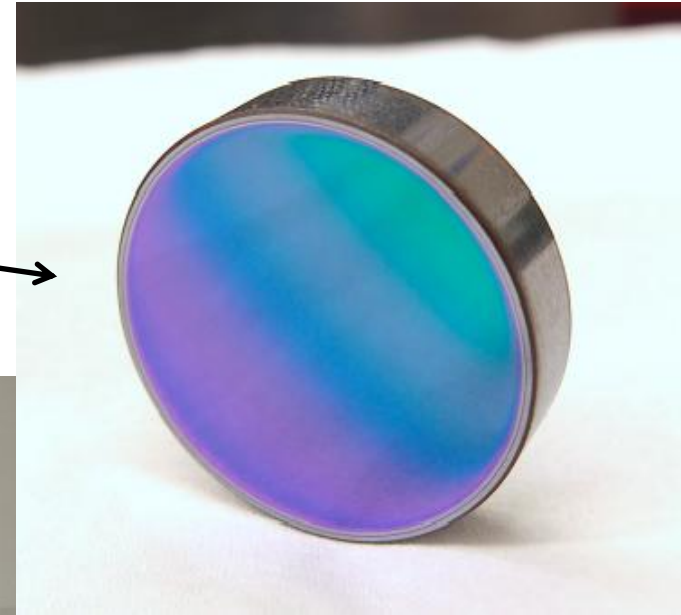


300 K Fused Silica
LIGO, Virgo,
Cosmic Explorer
@ 1064 nm

Amorphus
Crystalline



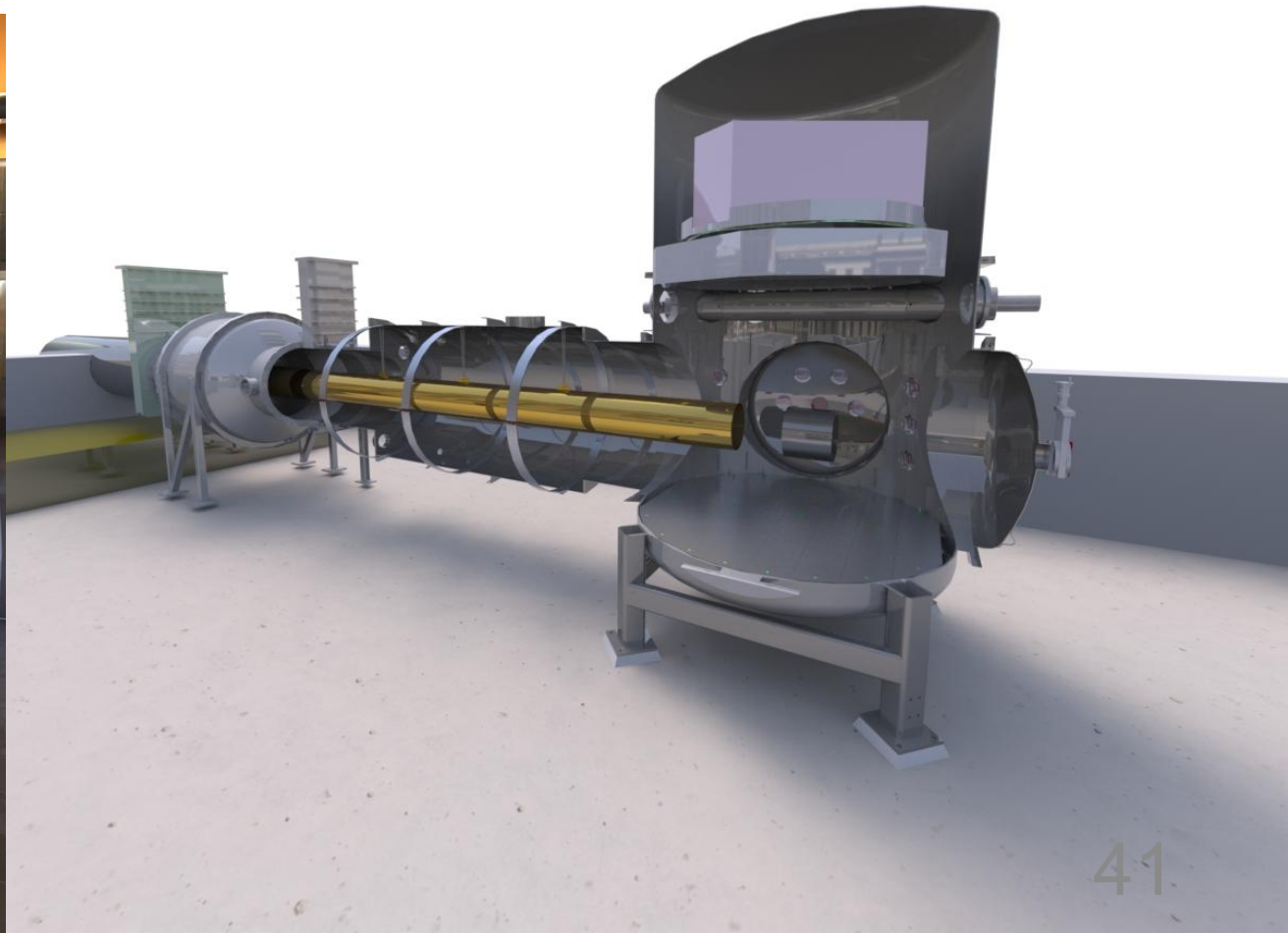
20 K Sapphire
KAGRA @ 1064 nm



120 K Silicon
Voyager @ 2050 nm
10 K Silicon
Einstein Telescope
@ 1550 nm

LIGO Voyager

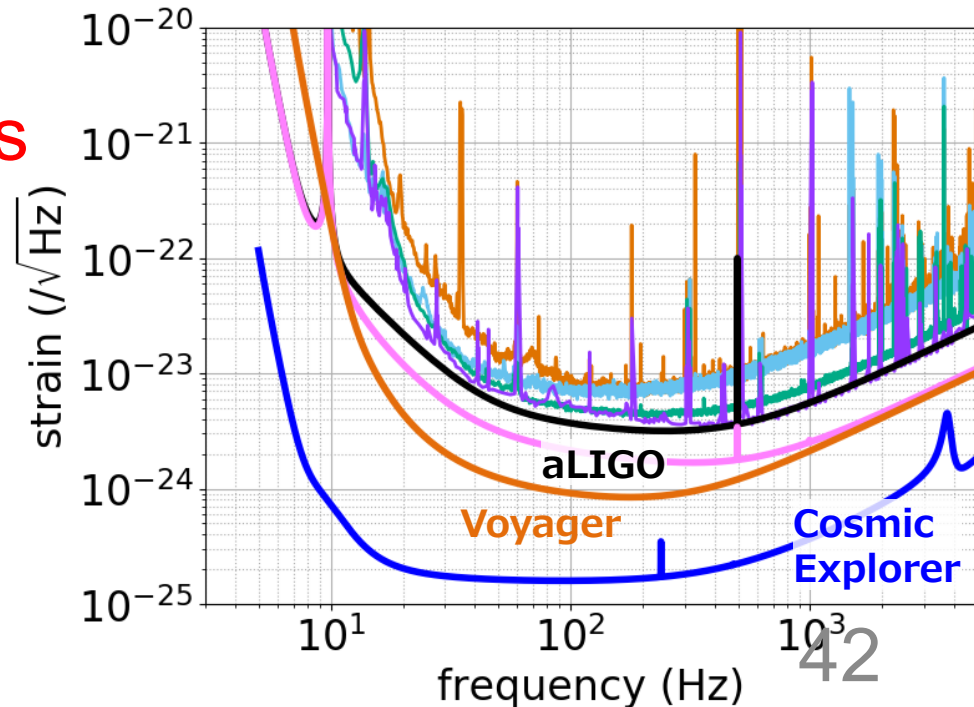
- Cryogenic upgrade to existing 4 km LIGO
- Intermediate step towards 10-40 km detectors



Exciting R&Ds for Next Generations

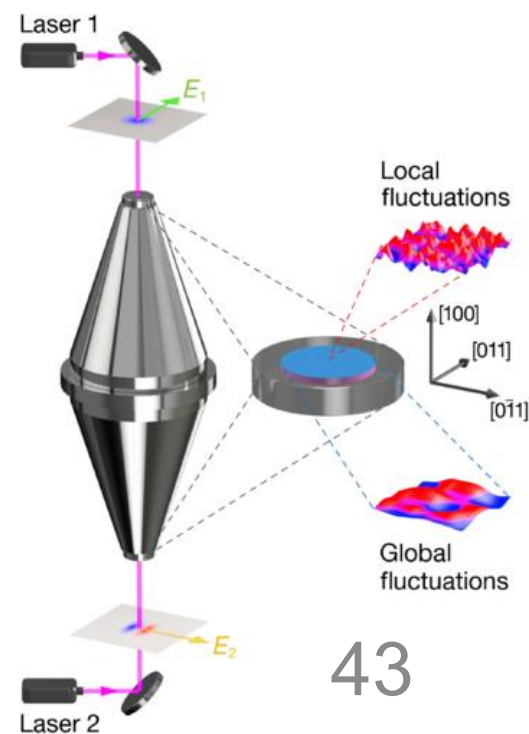
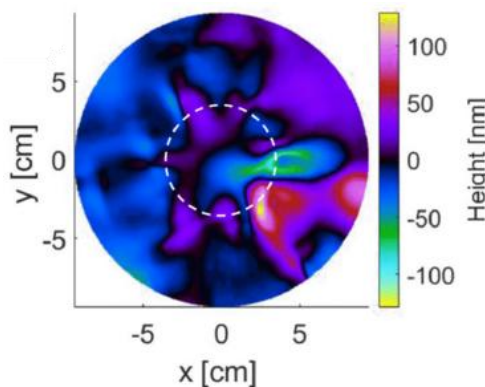
- Stable, high-power laser at **1.5-2 μm**
- High quantum efficiency photodiodes for 2 μm
- **Large silicon or sapphire** mirrors (φ 45 cm, 200 kg)
 - Low **birefringence**
 - Low absorption
- Low thermal noise
high-reflective coatings
- **Suspensions** for large mirrors
- **High power** handling

... and more



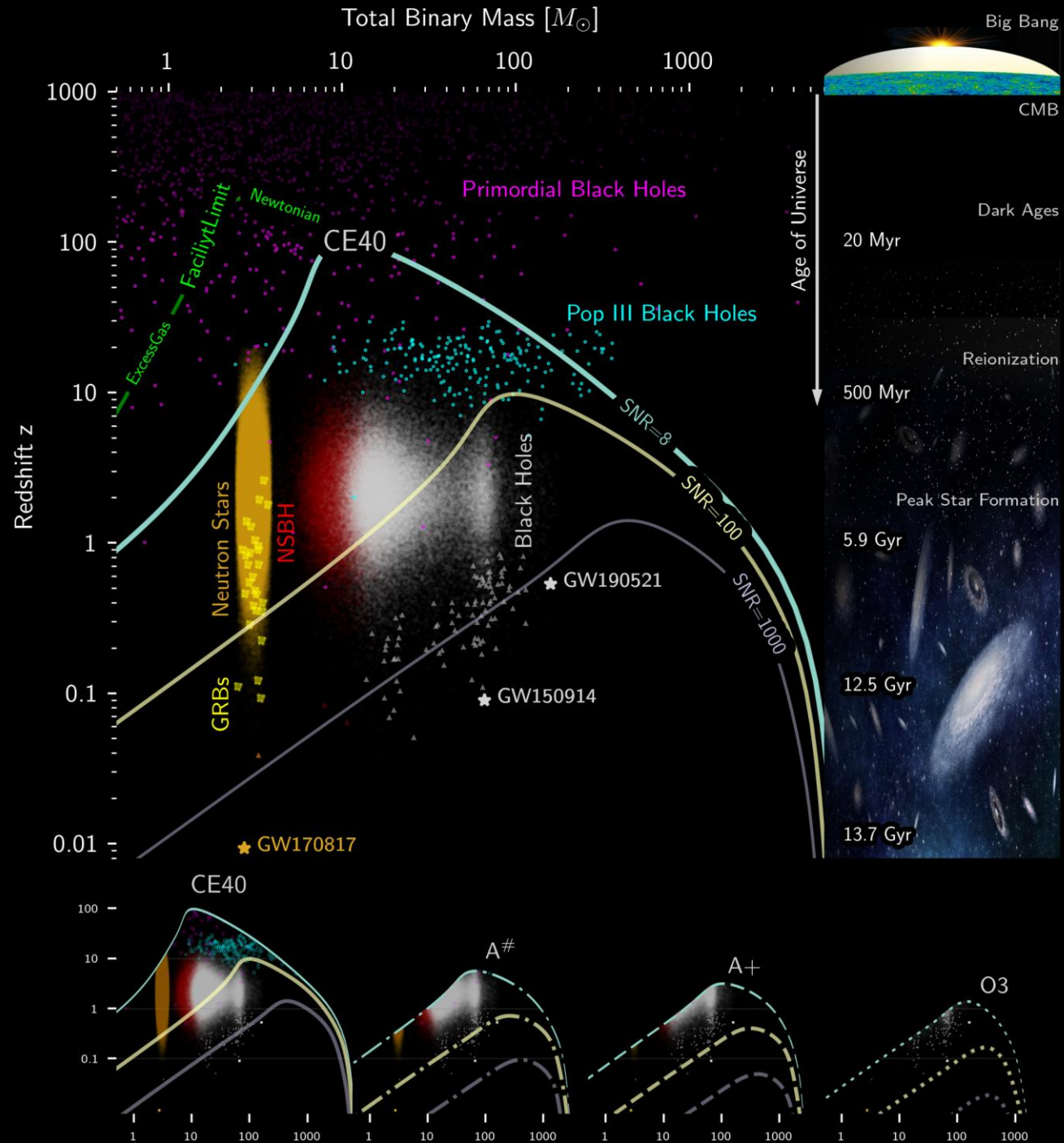
Birefringence and Its Fluctuations

- Birefringence ($\Delta n \sim 10^{-7}$ for silicon) needs to be small for reducing optical losses
- **Birefringence fluctuations** will also be additional phase noise ($\delta(\Delta n) < 10^{-15} / \sqrt{\text{Hz}}$) YM^+ , [PRD 109, 022009 \(2024\)](#)
- Excess birefringence noise reported by PTB/JILA
J. Yu+, [PRX 13, 041002 \(2023\)](#)
- **Inhomogeneous birefringence** experiences from KAGRA sapphire
H. Wang, ... , YM, [PRD 110, 082007 \(2024\)](#)
- Active research ongoing to study their effects and mitigation schemes



Next Gen.
detectors
can observe
compact
binaries
throughout
cosmic
history

<https://gravitationalwaves.syracuse.edu/about/>



Key Science Enabled by Next Gen.

Cosmic Explorer Science Themes

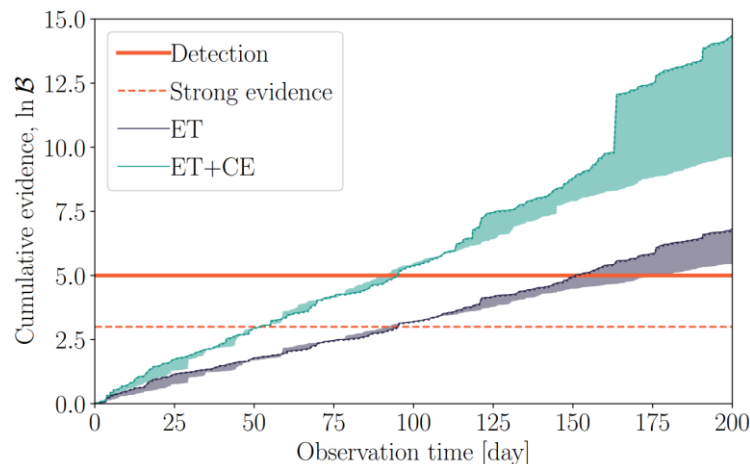
- Black Holes and Neutron Stars Throughout Cosmic Time
- Dynamics of Dense Matter
- Extreme Gravity and Fundamental Physics
- Discovery Potential

[arXiv:2109.09882](https://arxiv.org/abs/2109.09882)



Next Gen. Science Personal Picks

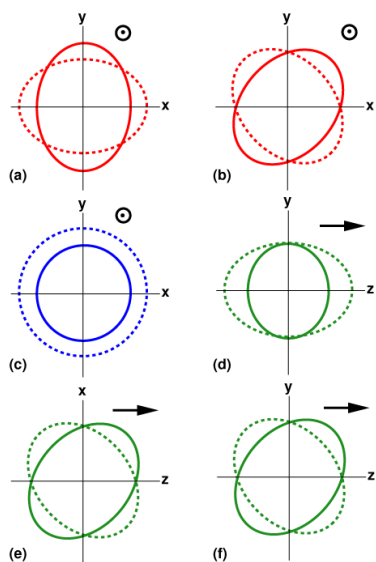
Displacement and Spin Memory



Permanent shift in the displacement and twist of the spacetime could be detected by ET and CE

Goncharov, Donnay, Harms,
[PRL 132, 241401 \(2024\)](#)

Polarization and Sky Localization

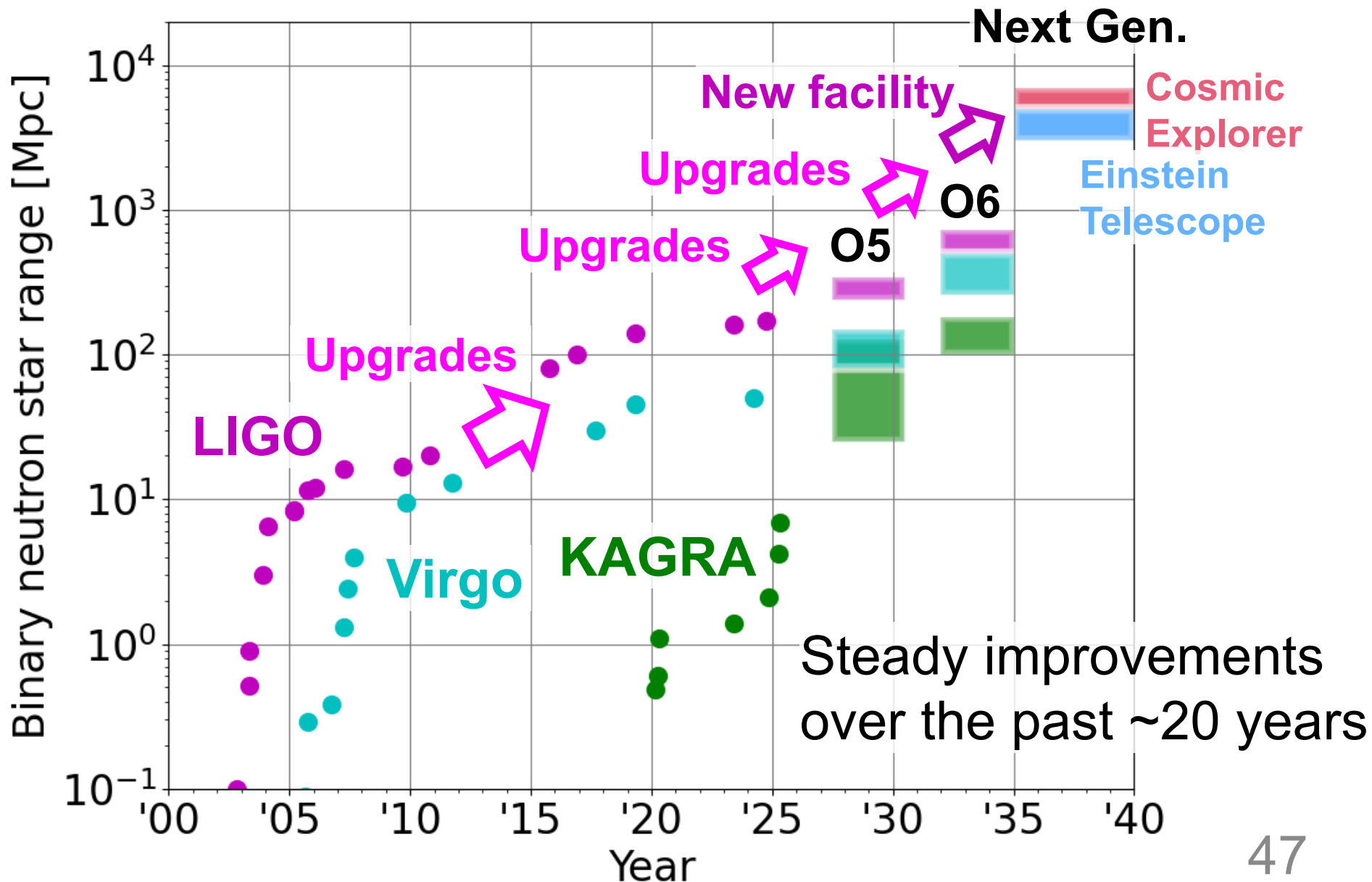


		BNS	BNS	BNS
Parameter		(ET-D—ET-D)	(ET-D—CE)	(CE-CE)
SNR		75.2	120	151
Model TS1	$\Delta \ln d_L$	0.0520	0.124	0.569
	$\Delta \Omega_s [\text{deg}^2]$	0.346	0.643	3.51
	ΔA_{S1}	0.0797	0.178	0.913

Takeda+,
[PRD 100, 042001 \(2019\)](#)

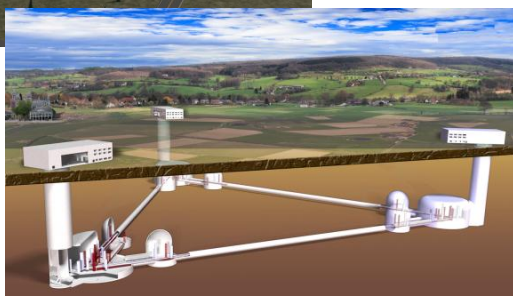
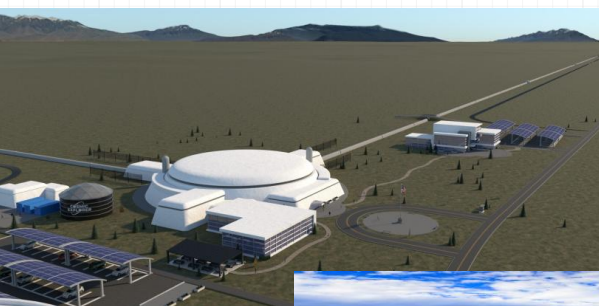
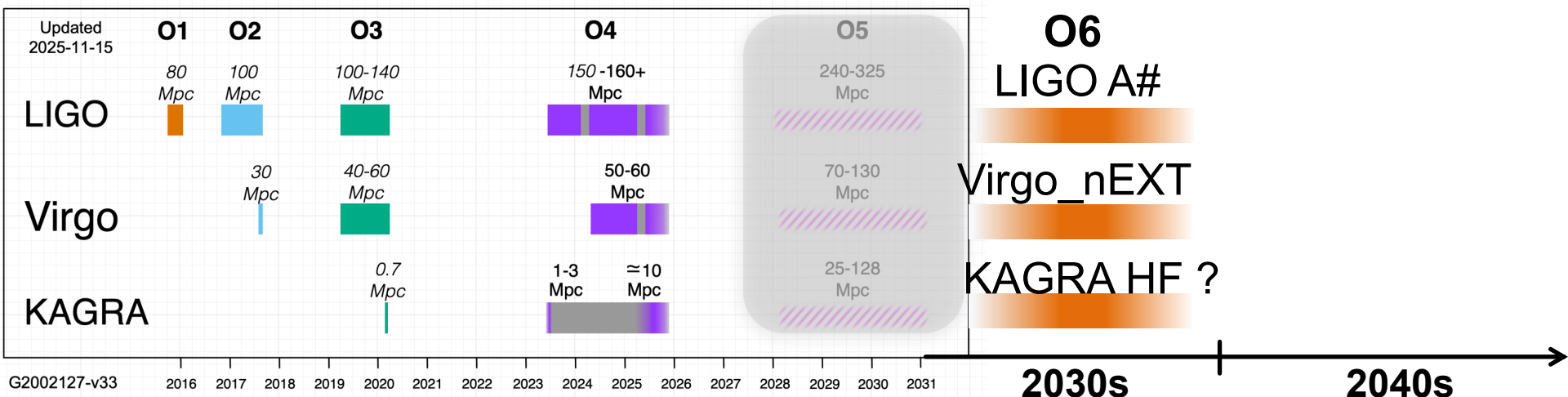
More polarization can be resolved & better sky localization with ET and CE due to low frequency sensitivity and **Earth rotation**

Sensitivity Evolution



Space-Based Detectors in 2030s

- Aiming **below 10 Hz** which is inaccessible with ground-based detectors (no seismic noise)



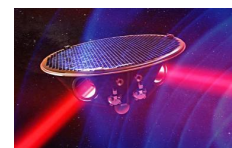
LIGO India

Cosmic Explorer

Einstein Telescope

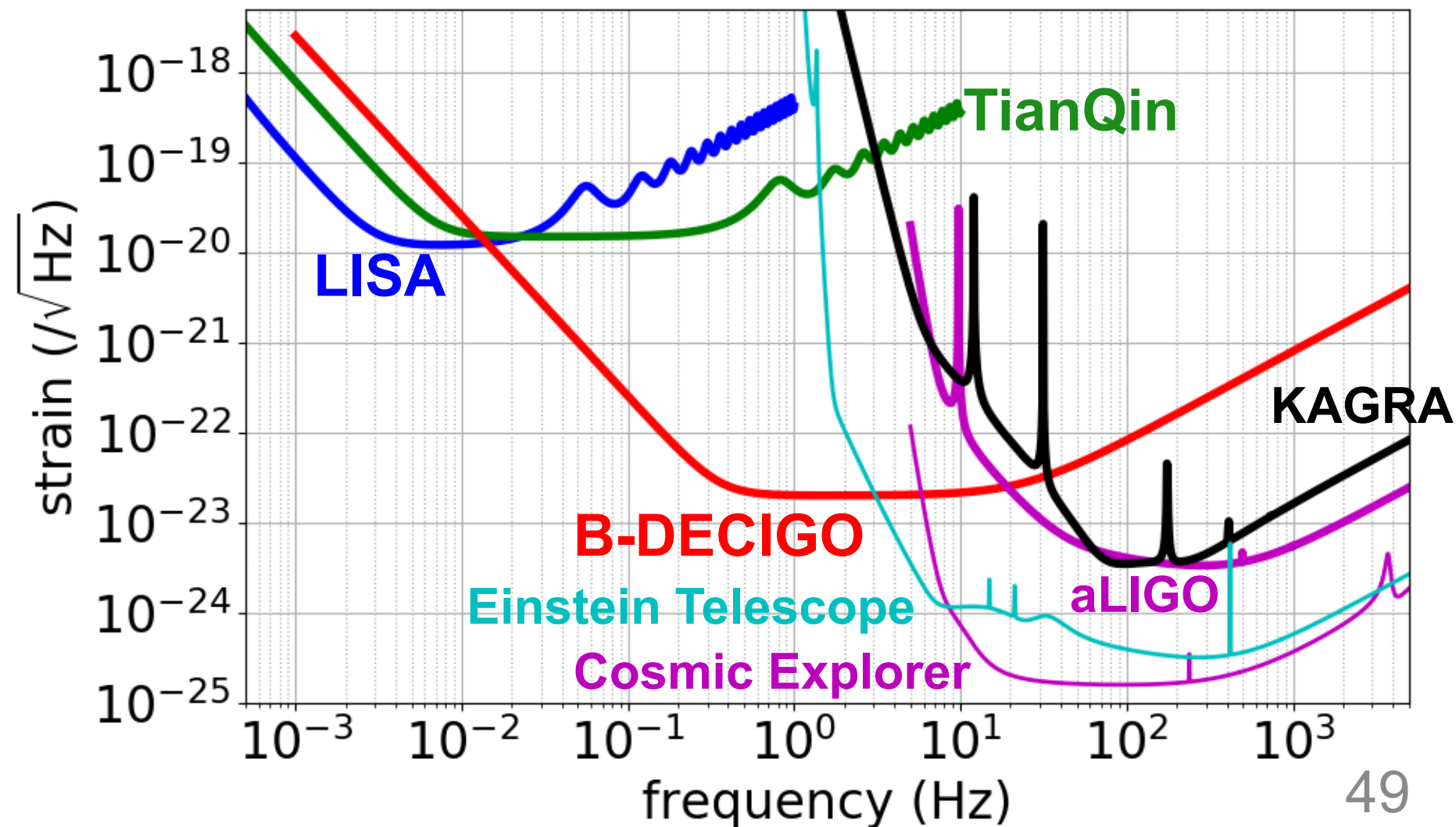
B-DECIGO

LISA

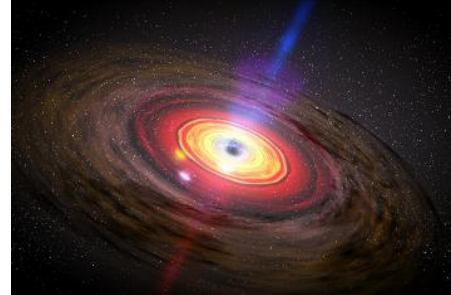


Space-Based Detectors: Sensitivity

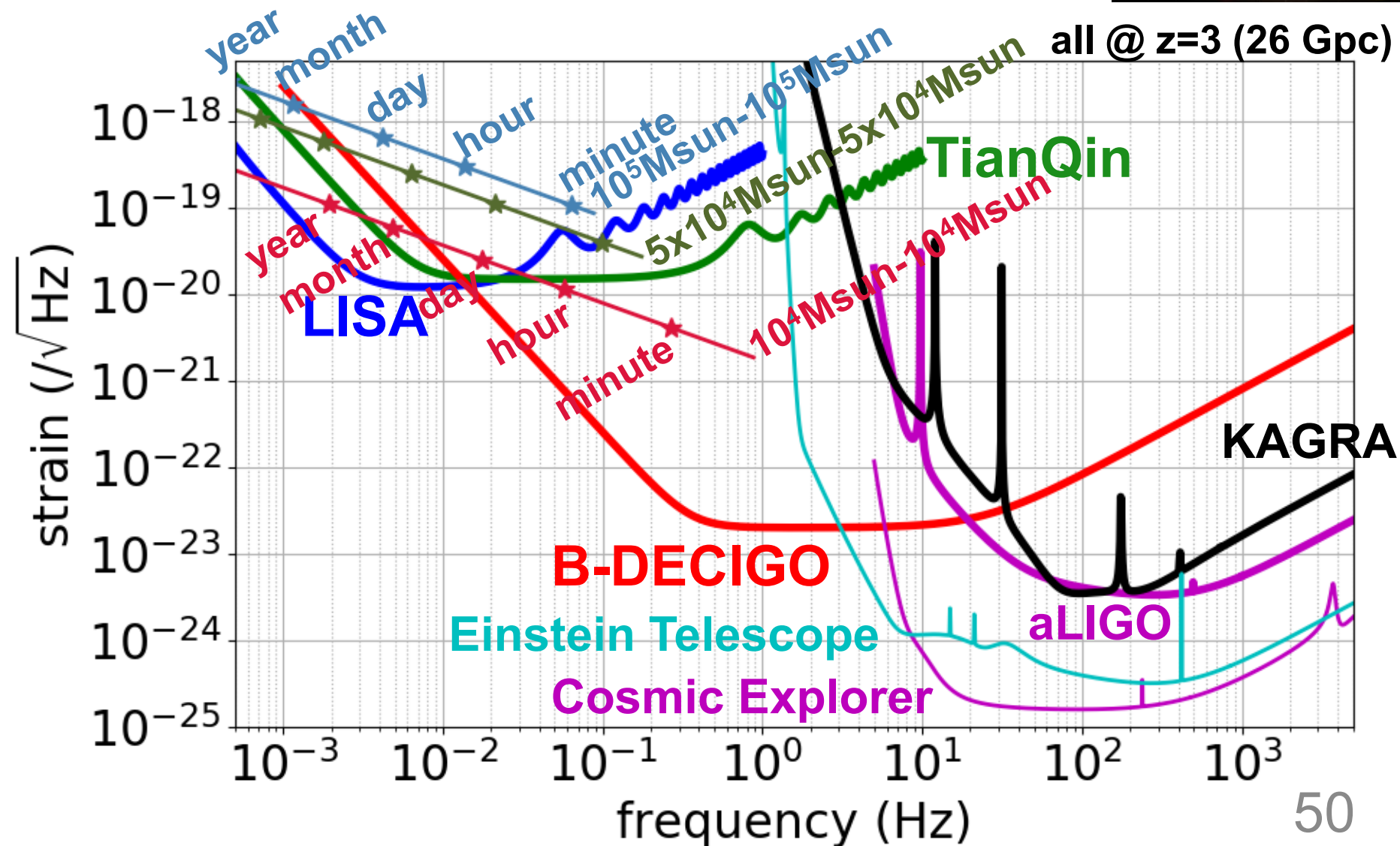
- LISA at 1-10 mHz, DECIGO at 0.1-1 Hz



Super Massive Blackholes

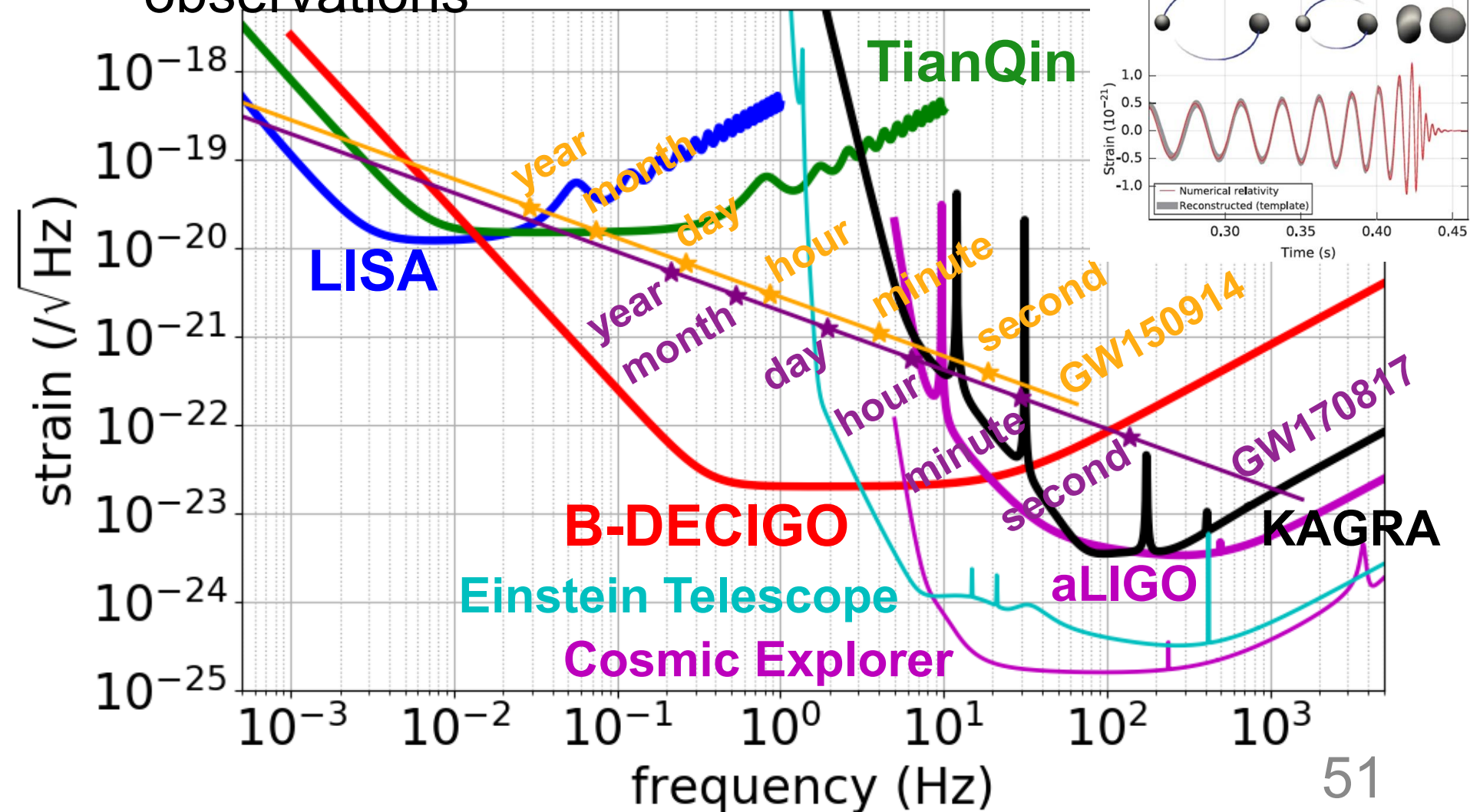


- LISA observes SMBH binaries



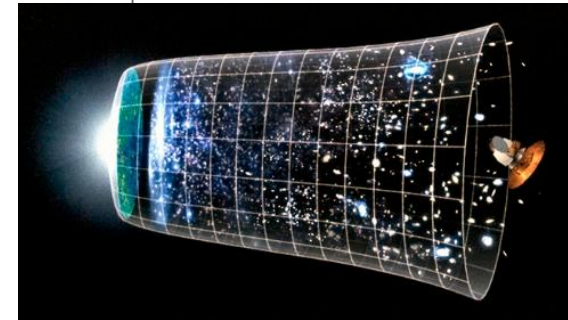
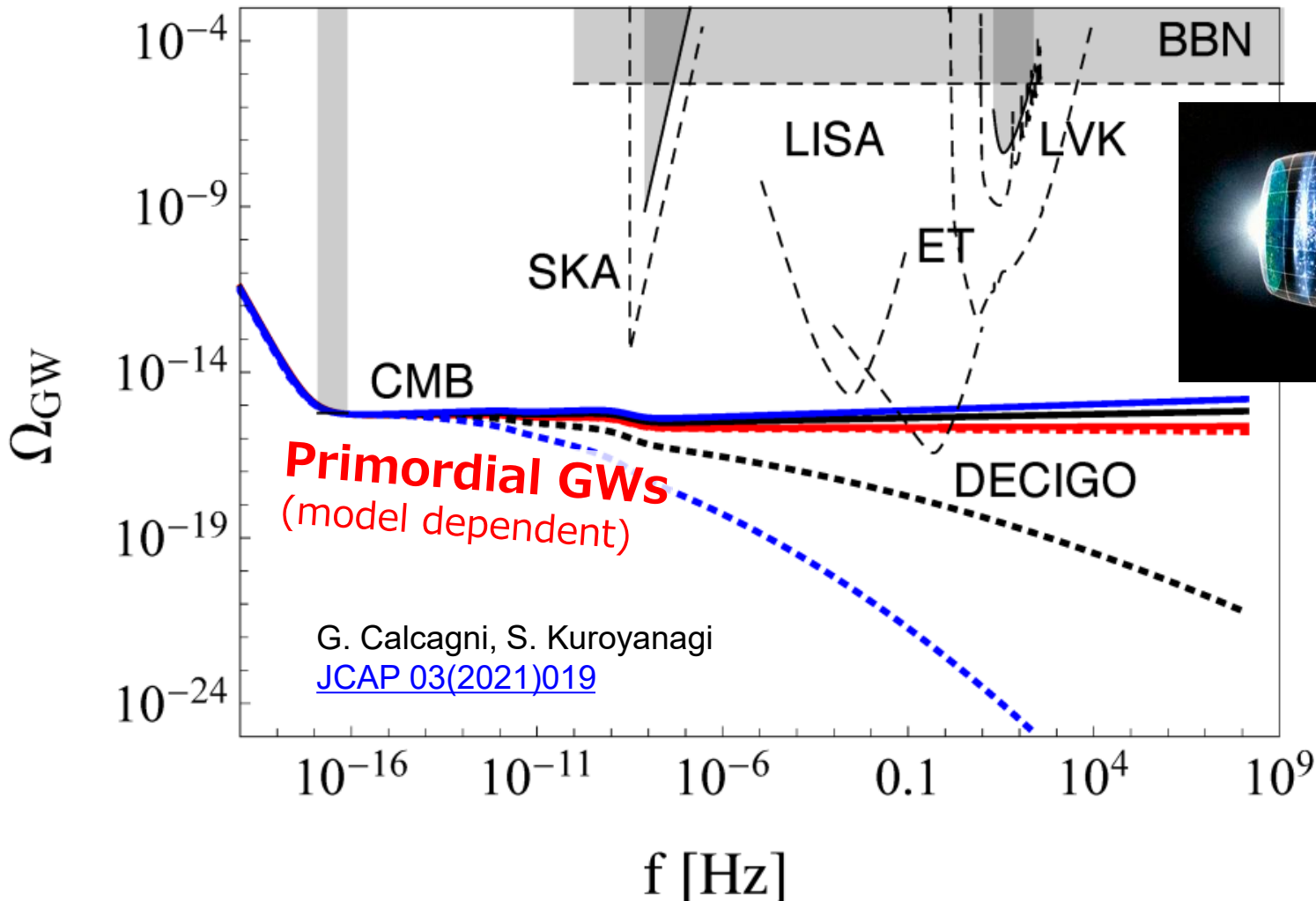
Multi-band Observations

- DECIGO can **predict merger time** for follow up observations



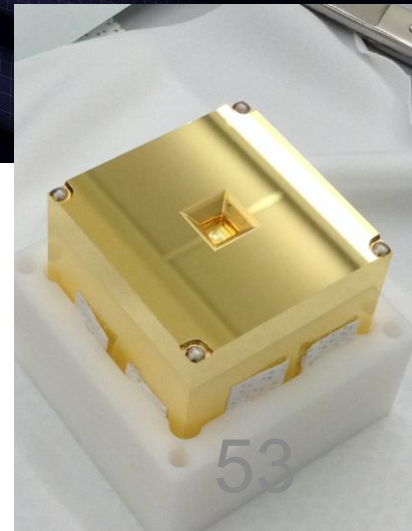
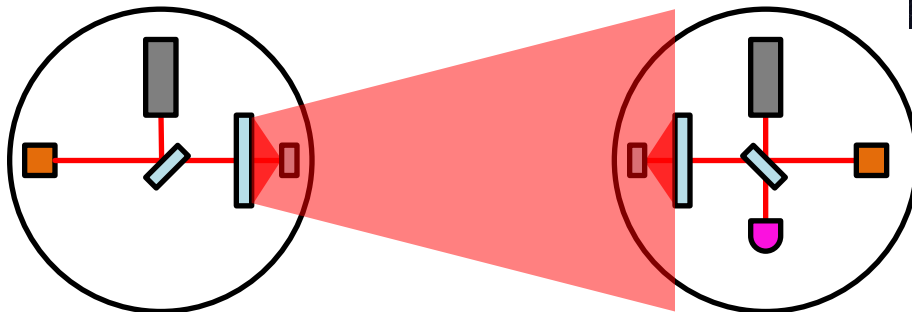
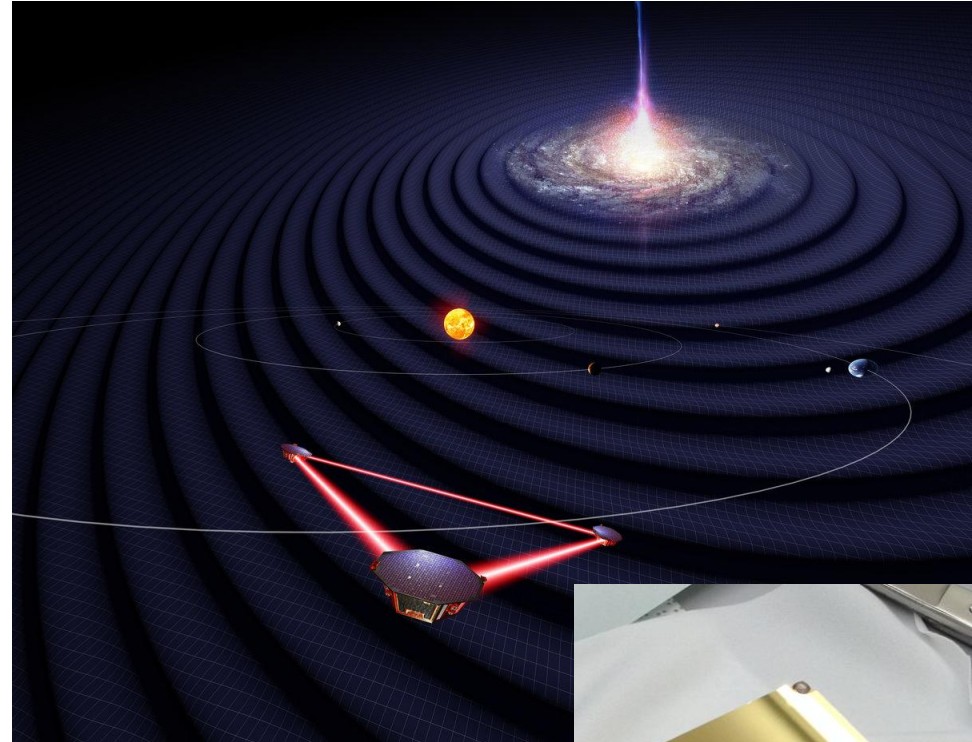
Primordial GWs from Inflation

- DECIGO band is suitable for observing **primordial gravitational waves**



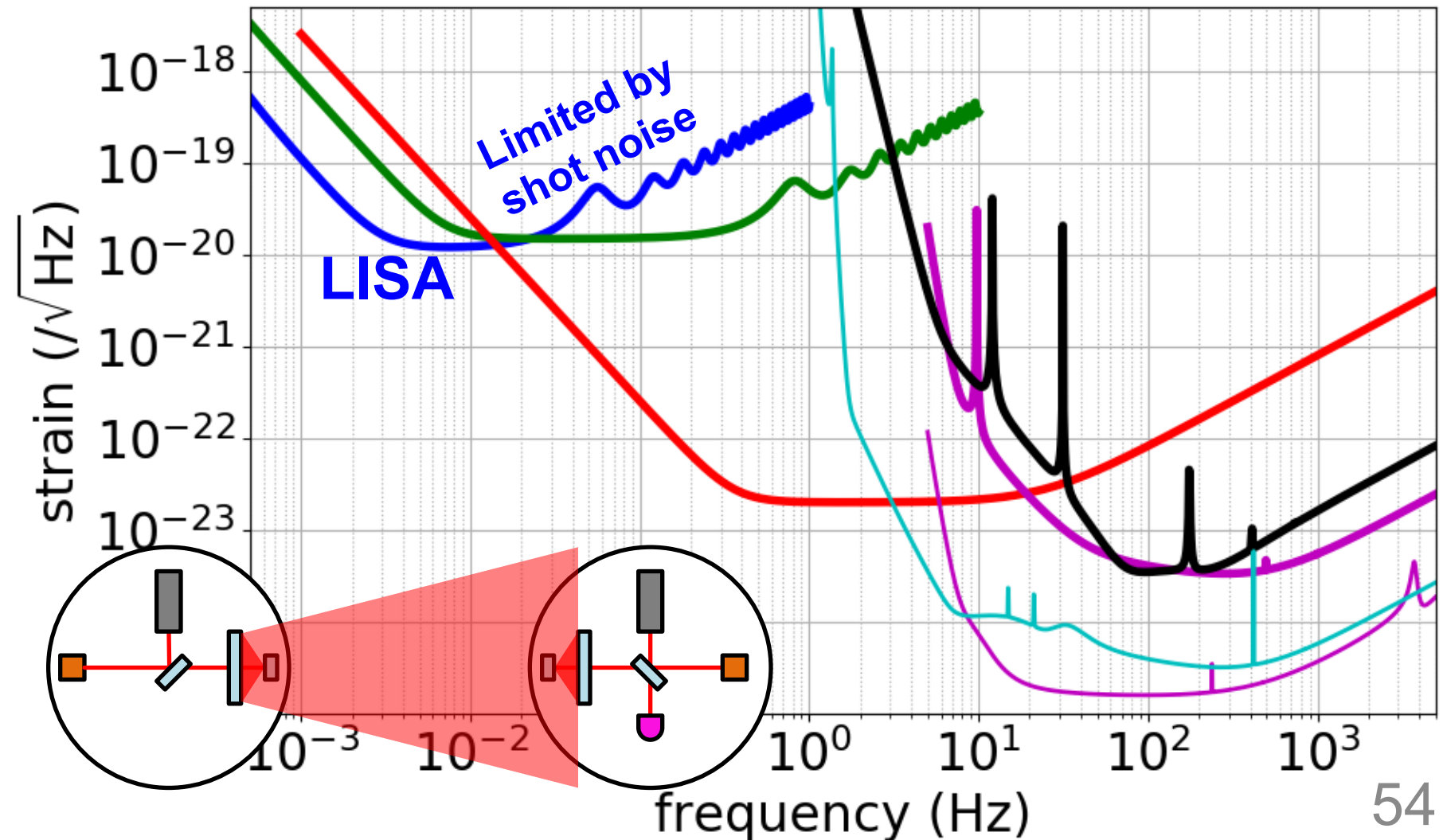
LISA to be Launched Mid-2030s

- Three satellites, 2.5×10^6 km arms
- Free-fall demonstrated with LISA Pathfinder in 2016
- Optical transponder:
Measures phase of laser beam



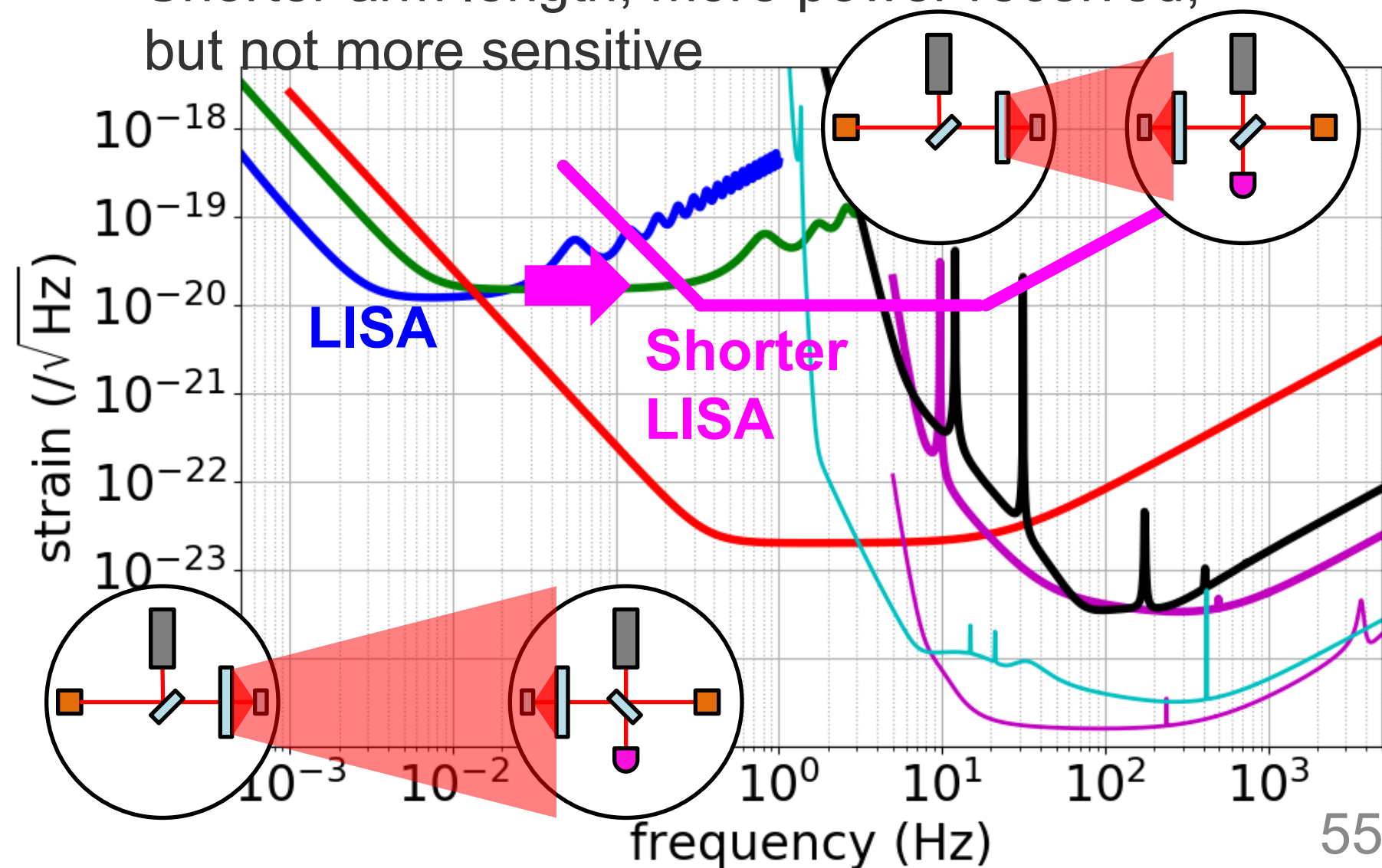
LISA Sensitivity Curve

- 1 W emitted, ~ 100 pW received



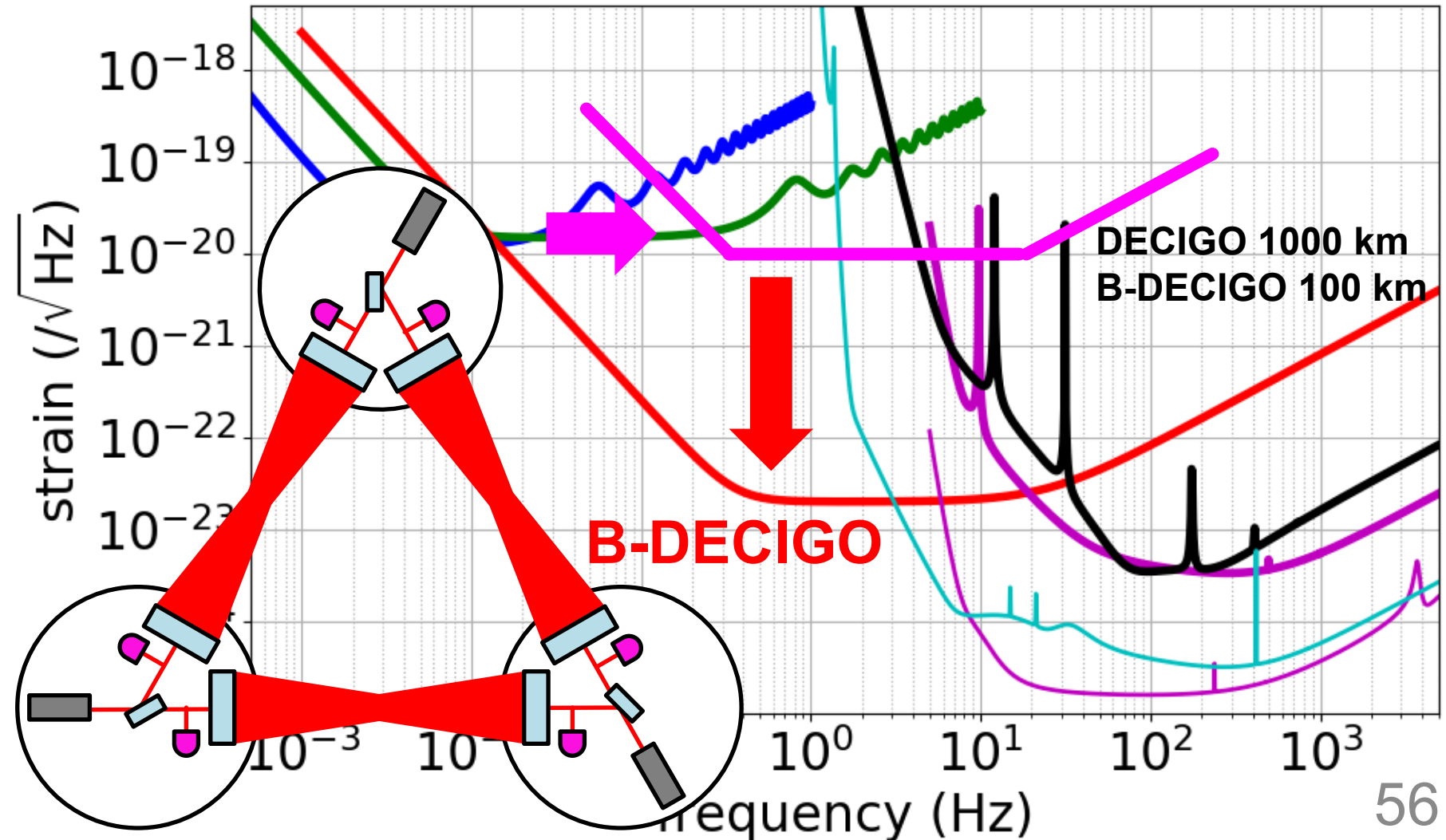
Shorter LISA will not be DECIGO

- Shorter arm length, more power received, but not more sensitive



Shorter LISA will not be DECIGO

- Form an optical cavity to enhance the sensitivity

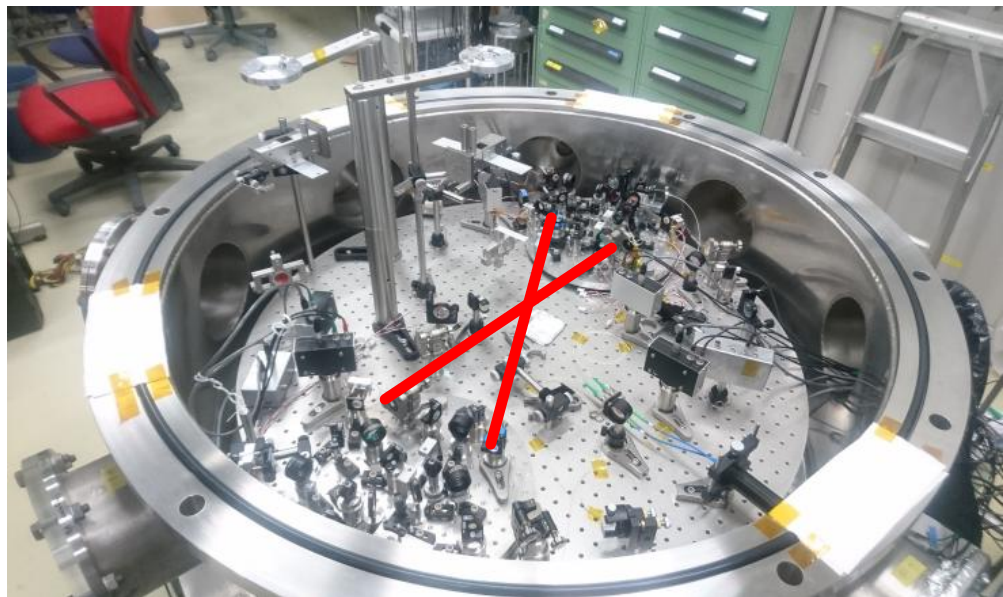
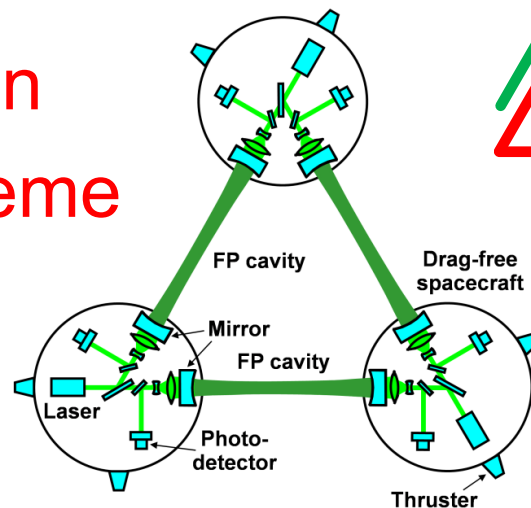


Exciting R&Ds for DECIGO

- Interferometer **configuration**
- Interferometer **control scheme**

Demonstration experiments
at UTokyo

- Stable laser source
 - Initial **link acquisition**
 - Low noise thrusters
 - Drag-free controls
 - Orbit and satellite controls
- ... and more!



SILVIA Project

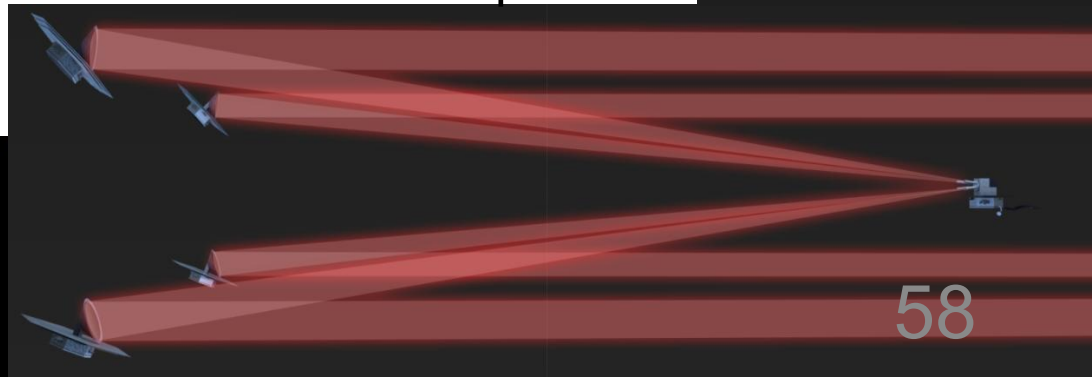
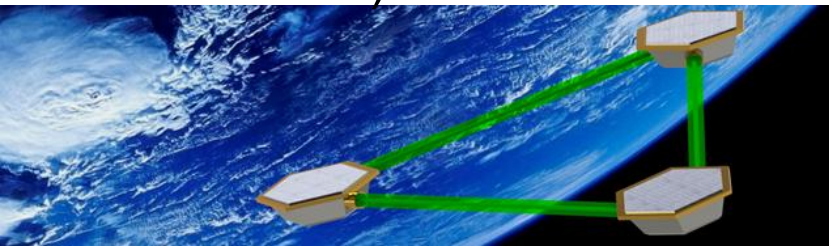


- Space Interferometer Laboratory Voyaging towards Innovative Applications
- Demonstration of ultra-precision formation flying with laser interferometer between satellites
- For DECIGO, LIFE etc.
- Proposal submitted to JAXA in Feb 2020 (currently at mission definition phase of JAXA's small satellite mission)



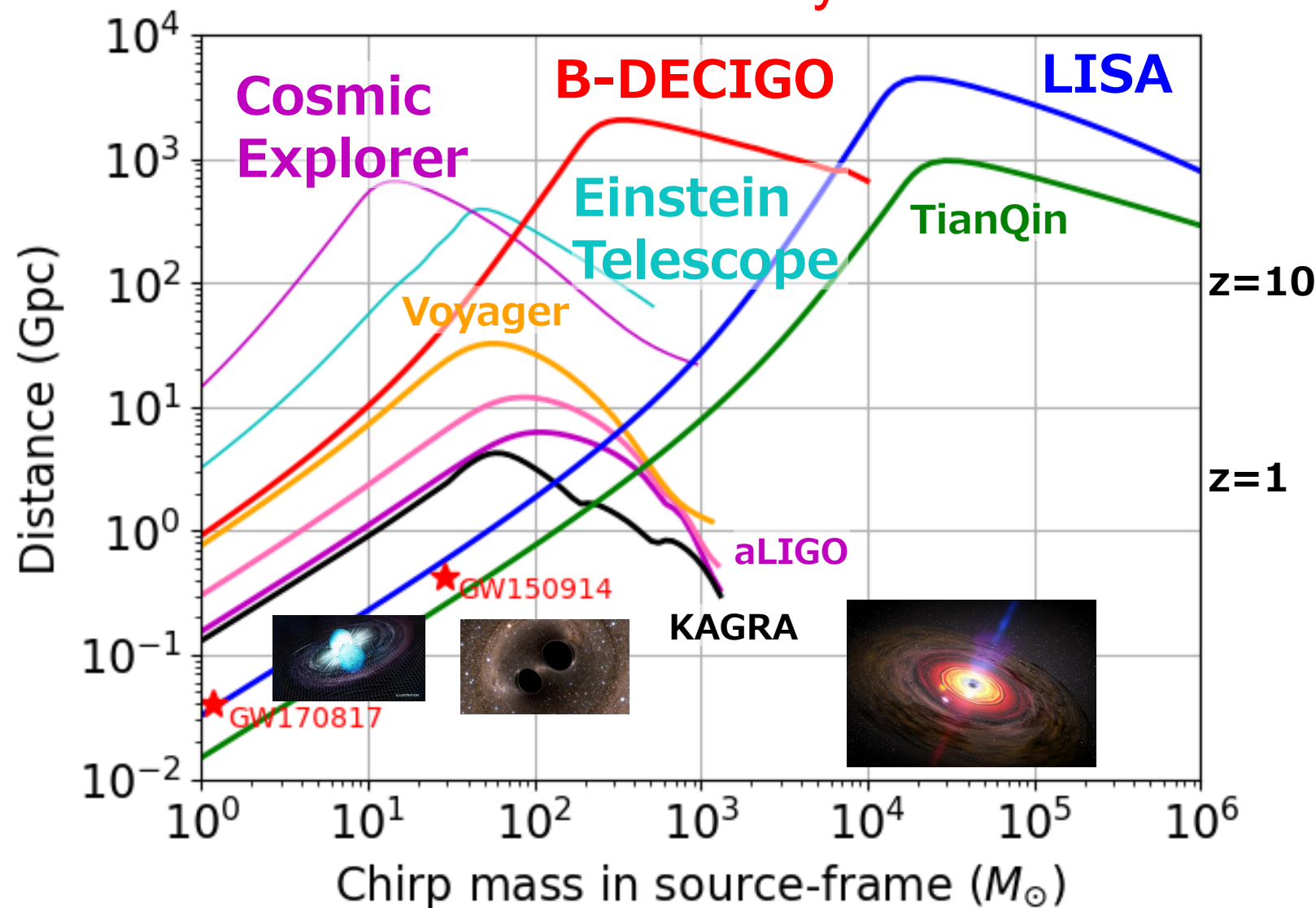
T. Ito+, [PASJ 77, 1080 \(2025\)](#)

➤ LIFE

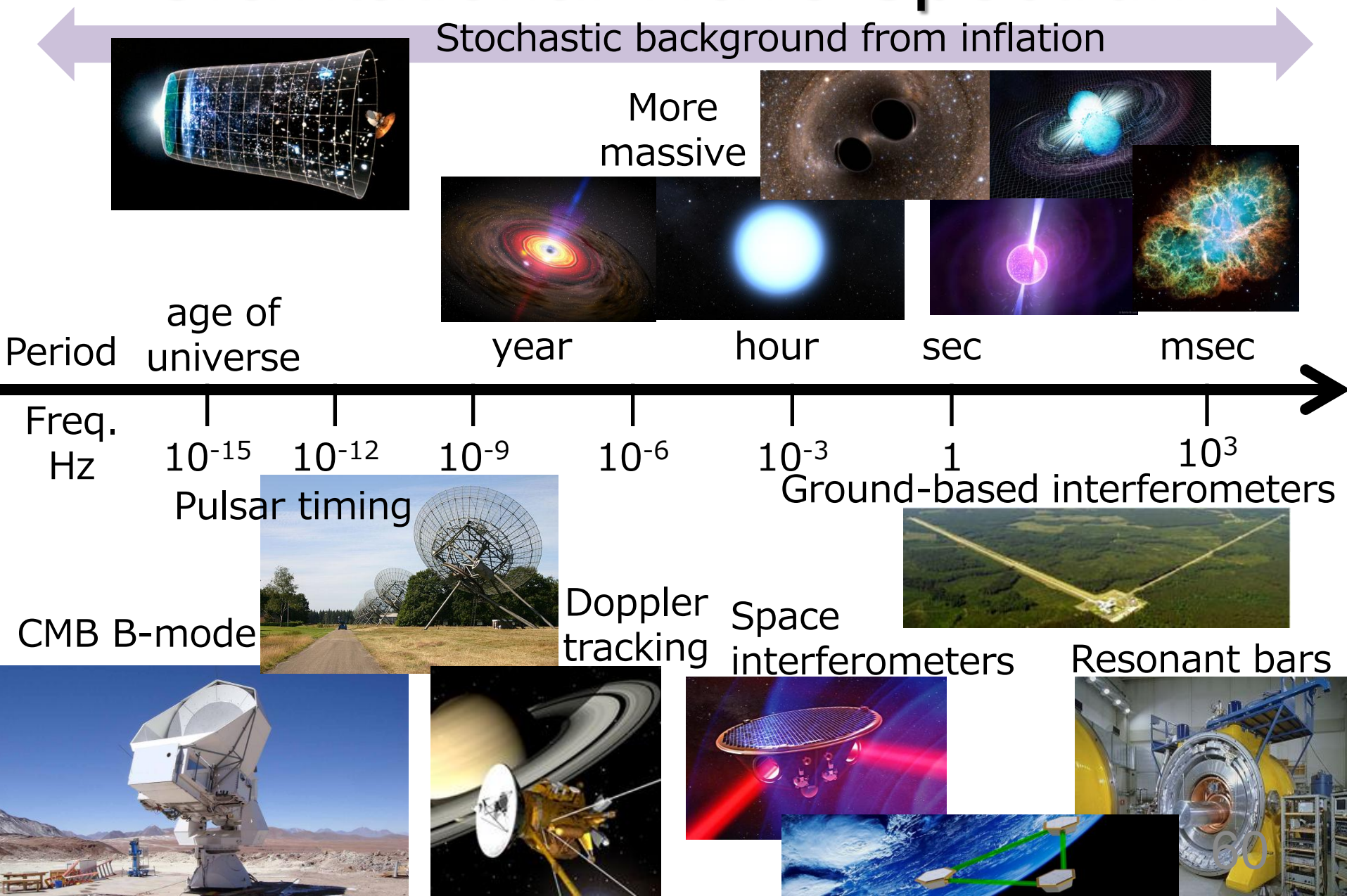


Astrophysical Reach to Binaries

- Covers **entire universe by 2030s**



Gravitational Wave Spectrum

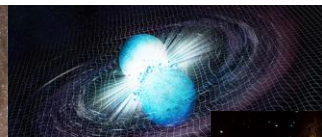


Gravitational Wave Spectrum

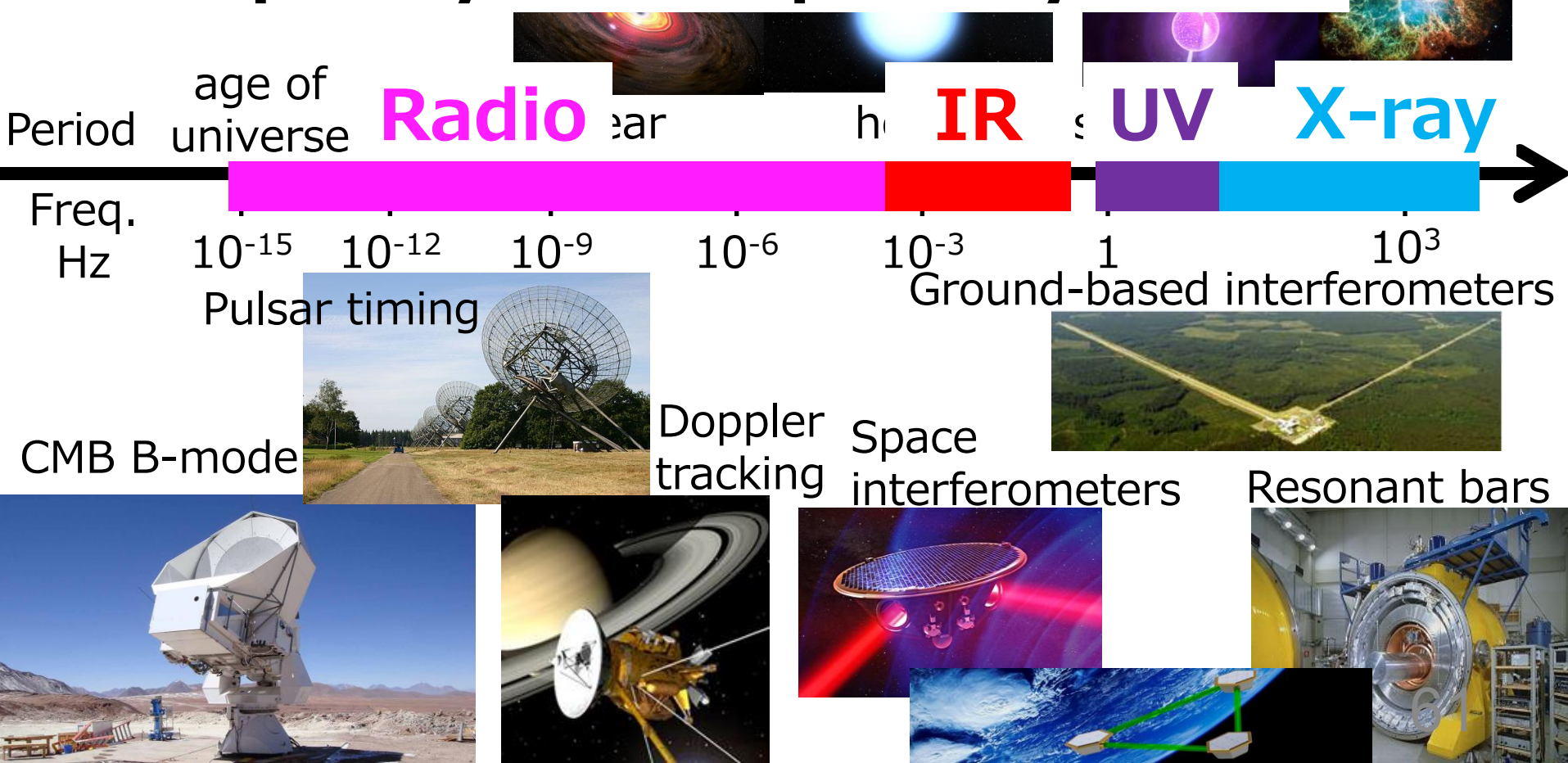
Stochastic background from inflation



More massive



If frequency is multiplied by 10^{15} ...

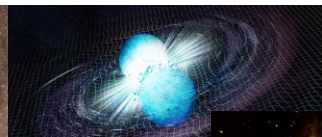


Gravitational Wave Spectrum

Stochastic background from inflation



More massive

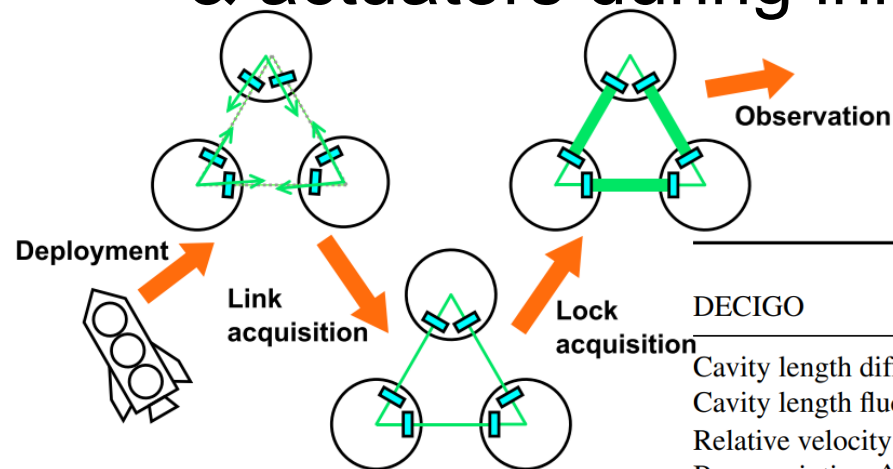


If frequency is multiplied by 10^{15} ...



But wait... Is DECIGO Feasible?

- Common misunderstanding: “Forming an optical cavity between satellites sounds impossible”
→ It is hard, but possible by using multiple sensors & actuators during initial acquisition sequence



YM+, [CQG 42, 225027 \(2025\)](#)

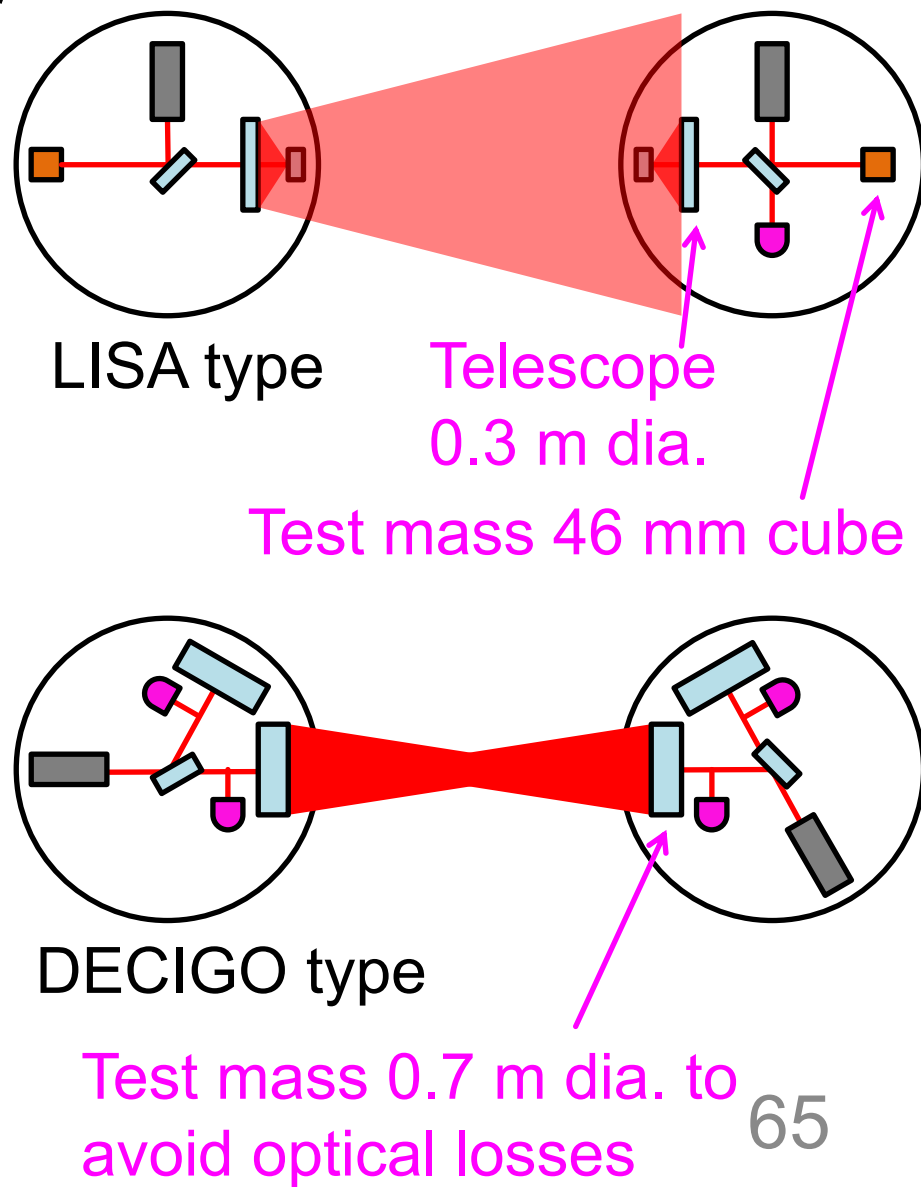
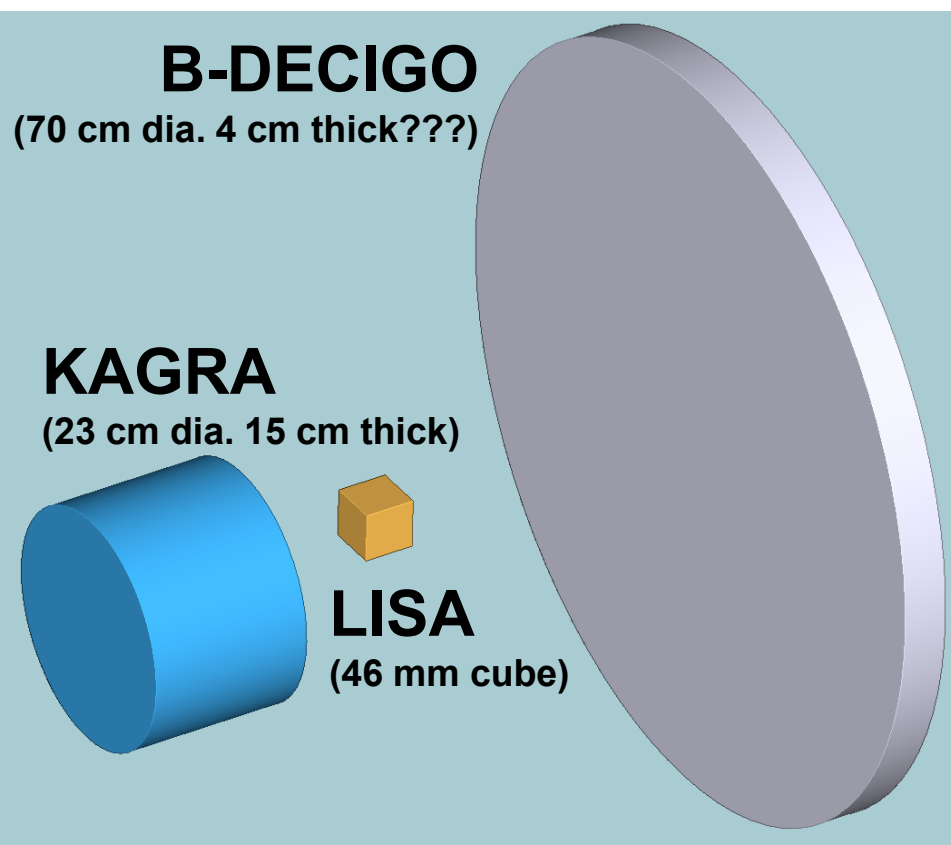
	Deployment goal	Link acquisition goal	Lock acquisition goal
DECIGO			
Cavity length difference ΔL	2 km	same	same
Cavity length fluctuations δL_{rms}	—	34 cm	0.5 nm
Relative velocity between mirrors v	—	$1.2 \mu\text{m s}^{-1}$	23 nm s^{-1}
Beam pointing $\Delta\theta_{\text{beam}}$	3 mrad	$0.46 \mu\text{rad}$	—
Mirror relative alignment $\Delta\theta$	—	$0.23 \mu\text{rad}$	0.035 nrad
B-DECIGO			
Cavity length difference ΔL	40 m	same	same
Cavity length fluctuations δL_{rms}	—	3.4 cm	0.1 nm
Relative velocity between mirrors v	—	$0.12 \mu\text{m s}^{-1}$	23 nm s^{-1}
Beam pointing $\Delta\theta_{\text{beam}}$	3 mrad	$1.5 \mu\text{rad}$	—
Mirror relative alignment $\Delta\theta$	—	$0.73 \mu\text{rad}$	0.35 nrad

Design Comparison

	LISA	TianQin	B-DECIGO
Arm length	2.5e6 km	1.7e5 km	100 km
Interferometry	Optical transponder	Optical transponder	Fabry-Pérot cavity (F=100)
Laser frequency stabilization	Reference cavity, 1064 nm (~3 W)	Reference cavity, 1064 nm	Iodine, 515 nm (~1 W)
Orbit	Heliocentric	Geocentric, facing J0806.3+1527	Geocentric (TBD)
Flight configuration	Constellation flight	Constellation flight	Formation flight
Test mass	1.96 kg (46 mm cube of Au-Pt alloy)	2.45 kg (50 mm cube of Au-Pt alloy)	30 kg (70 cm dia, 4 cm thick Fused Silica???)
Force noise req.	8e-15 N/rHz Achieved PRL 120, 061101 (2018)	7e-15 N/rHz CQG 33, 035010 (2016)	1e-16 N/rHz

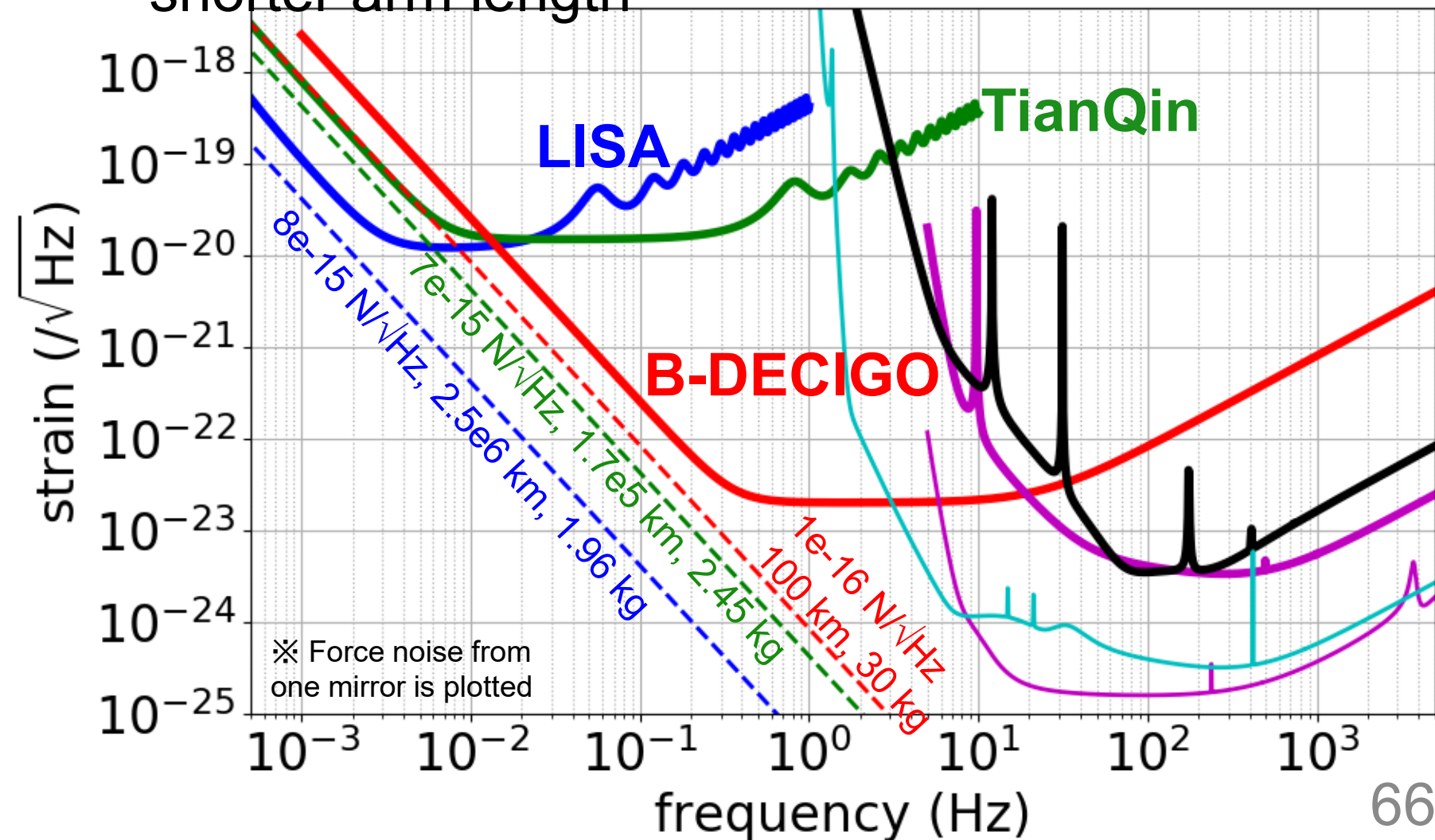
Tough Part is the Large Mirrors

- Shorter arms and larger mirrors are required for reflecting all the light to form optical cavities



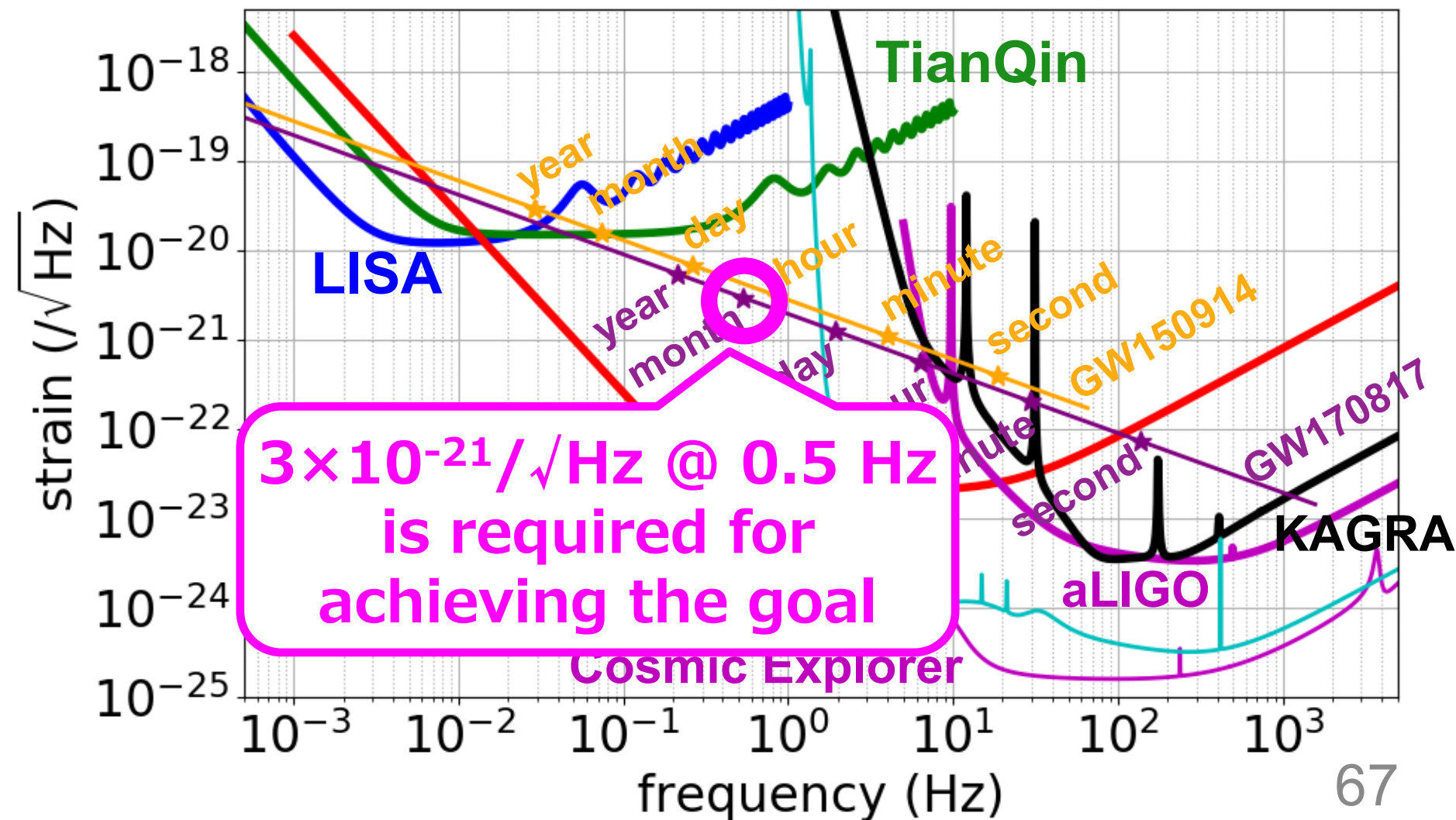
Stringent Force Noise Requirement

- B-DECIGO requirement is most stringent due to shorter arm length



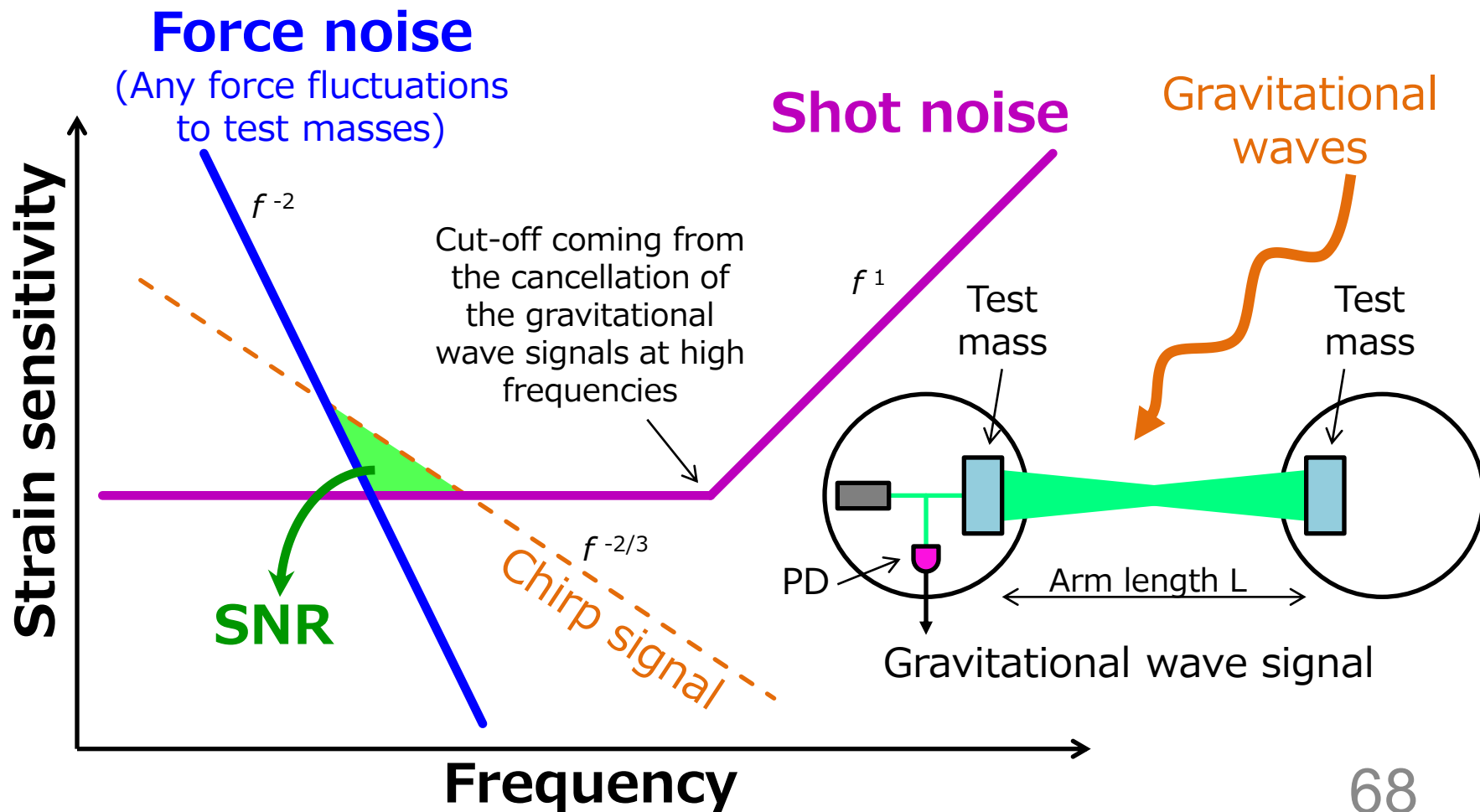
Let's Start from the Minimum Goal

- **Minimum goal:** Observe GW170817-like binary a month before the merger (or GW150914-like binary an hour before the merger)



Sensitivity of Space Detectors

- Can be modeled with **force noise** and **shot noise**



Equations for the Noises

- Force noise**

$$h_f = \frac{n_f}{m\omega^2 L}$$

Force noise spectrum n_f (indicated by an arrow from the text to n_f)

Mass of test mass m (indicated by an arrow from the text to m)

GW frequency ω (indicated by an arrow from the text to ω)

Arm length L (indicated by an arrow from the text to L)

※LISA Pathfinder achieved $4 \times 10^{-15} \text{ N}/\sqrt{\text{Hz}}$ @ 1 mHz

→ From n_f , requirement on mL is derived

- Shot noise**

$$h_{\text{shot}} = \frac{1}{2\pi L} \sqrt{\frac{hc\lambda}{2P} \frac{\pi}{2\mathcal{F}}}$$

Laser wavelength λ (indicated by an arrow from the text to λ)

Arm length L (indicated by an arrow from the text to L)

Input power P (indicated by an arrow from the text to P)

Finesse $\mathcal{F}$ (indicated by an arrow from the text to $\mathcal{F}$)

※ $\mathcal{F}=2/\pi$ for Michelson

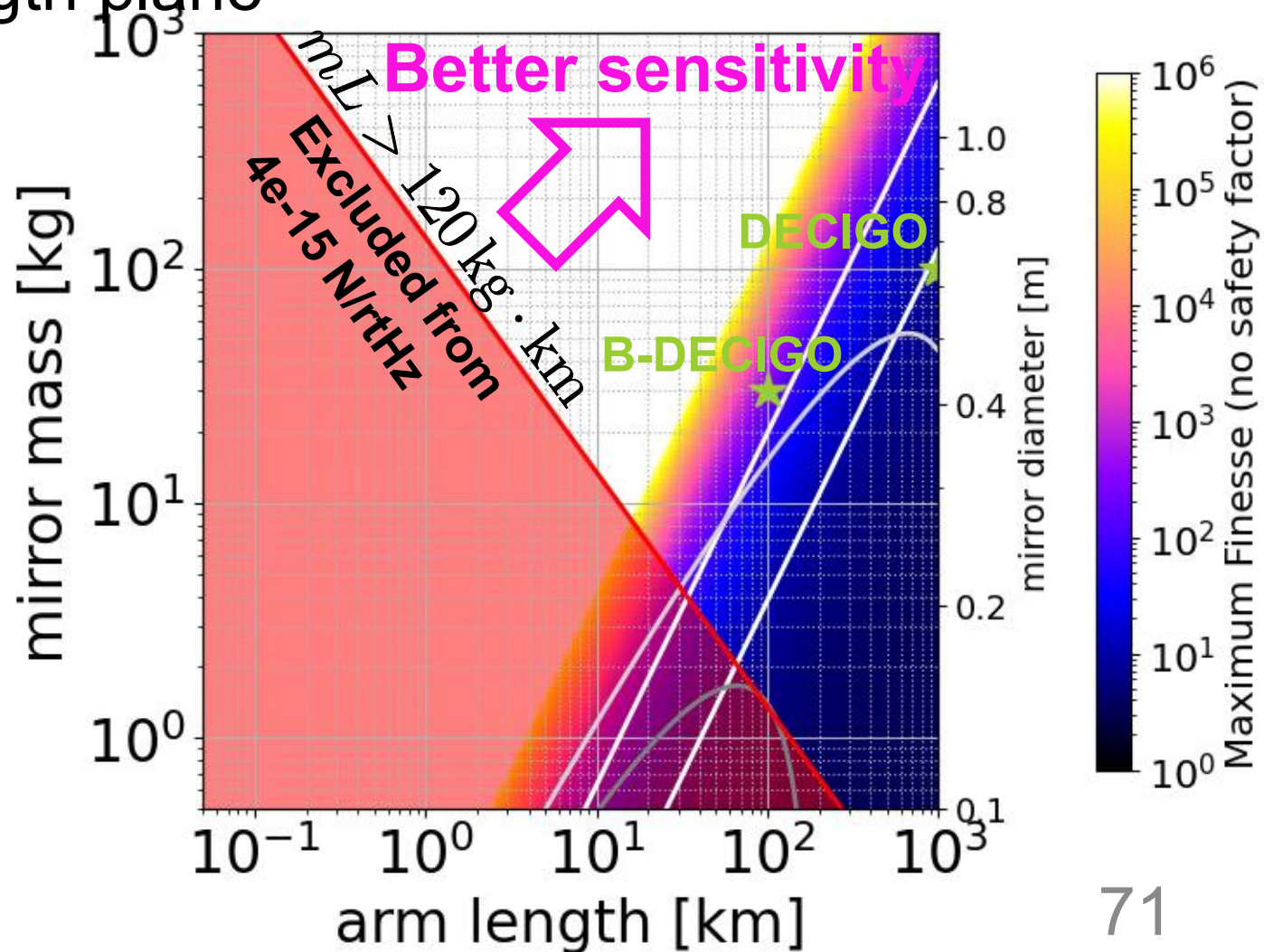
→ From laser wavelength and power, requirement on $L\mathcal{F}$ is derived

Requirement on Basic Parameters

- To Achieve $3 \times 10^{-21}/\sqrt{\text{Hz}}$ @ 0.5 Hz goal
- If the **force noise** is $4 \times 10^{-15} \text{ N}/\sqrt{\text{Hz}}$
 $mL > 120 \text{ kg} \cdot \text{km}$
$$h_f = \frac{n_f}{m\omega^2 L}$$
- If the laser is 515 nm and 10 mW, **shot noise** gives
 $L\mathcal{F} > 180 \text{ km}$
$$h_{\text{shot}} = \frac{1}{2\pi L} \sqrt{\frac{hc\lambda}{2P}} \frac{\pi}{2\mathcal{F}}$$
- **kg-class** test masses and **km-class** arm length are required
- Forming an optical cavity is not required if
 $L > 180 \text{ km}/(\pi/2) = 114 \text{ km}$

Mirror Size and Arm Length

- Force noise requirement gives allowed region in mass-length plane

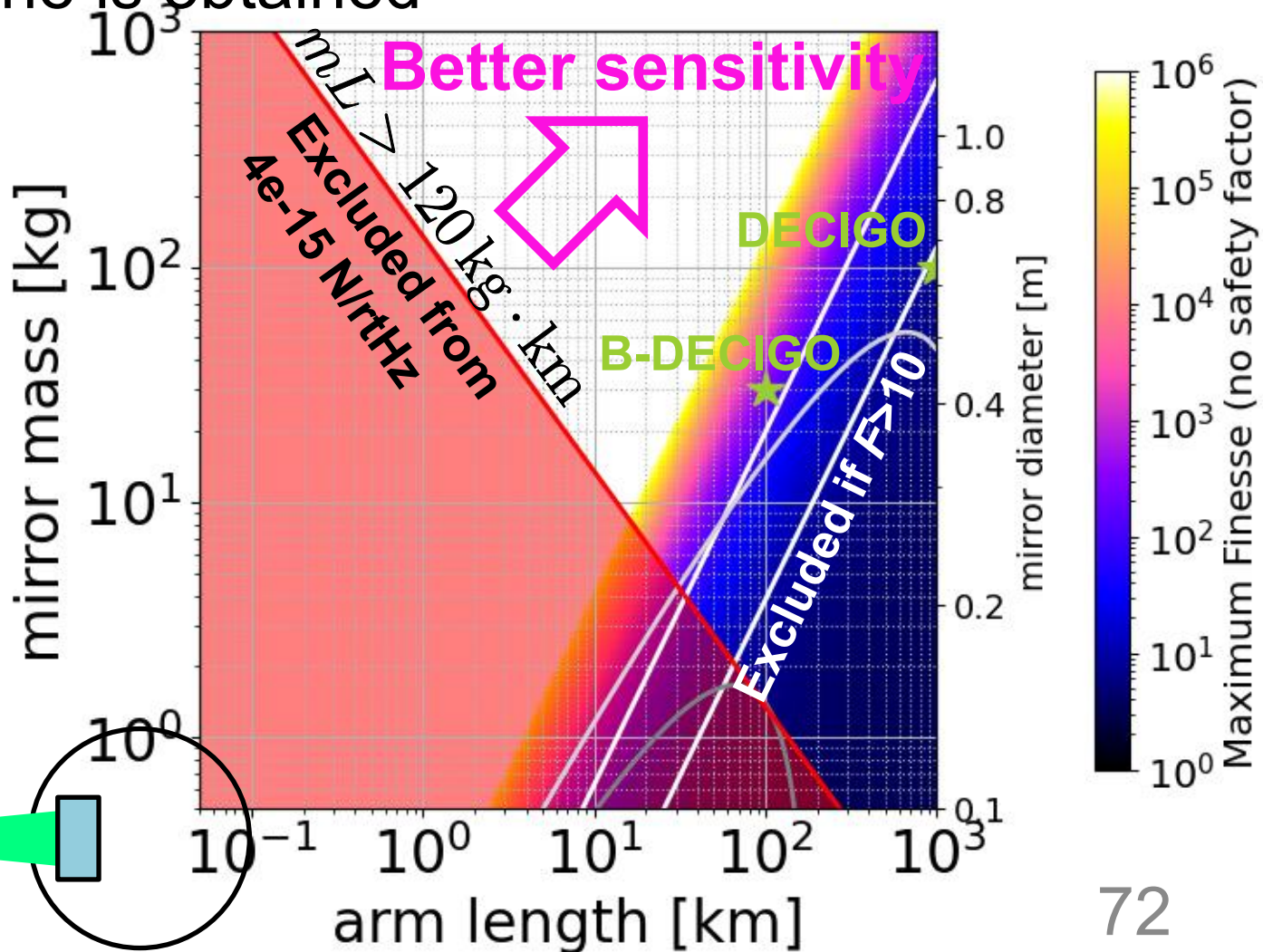


Mirror Size and Arm Length

- From **diffraction losses**, allowed region in mass-length plane is obtained

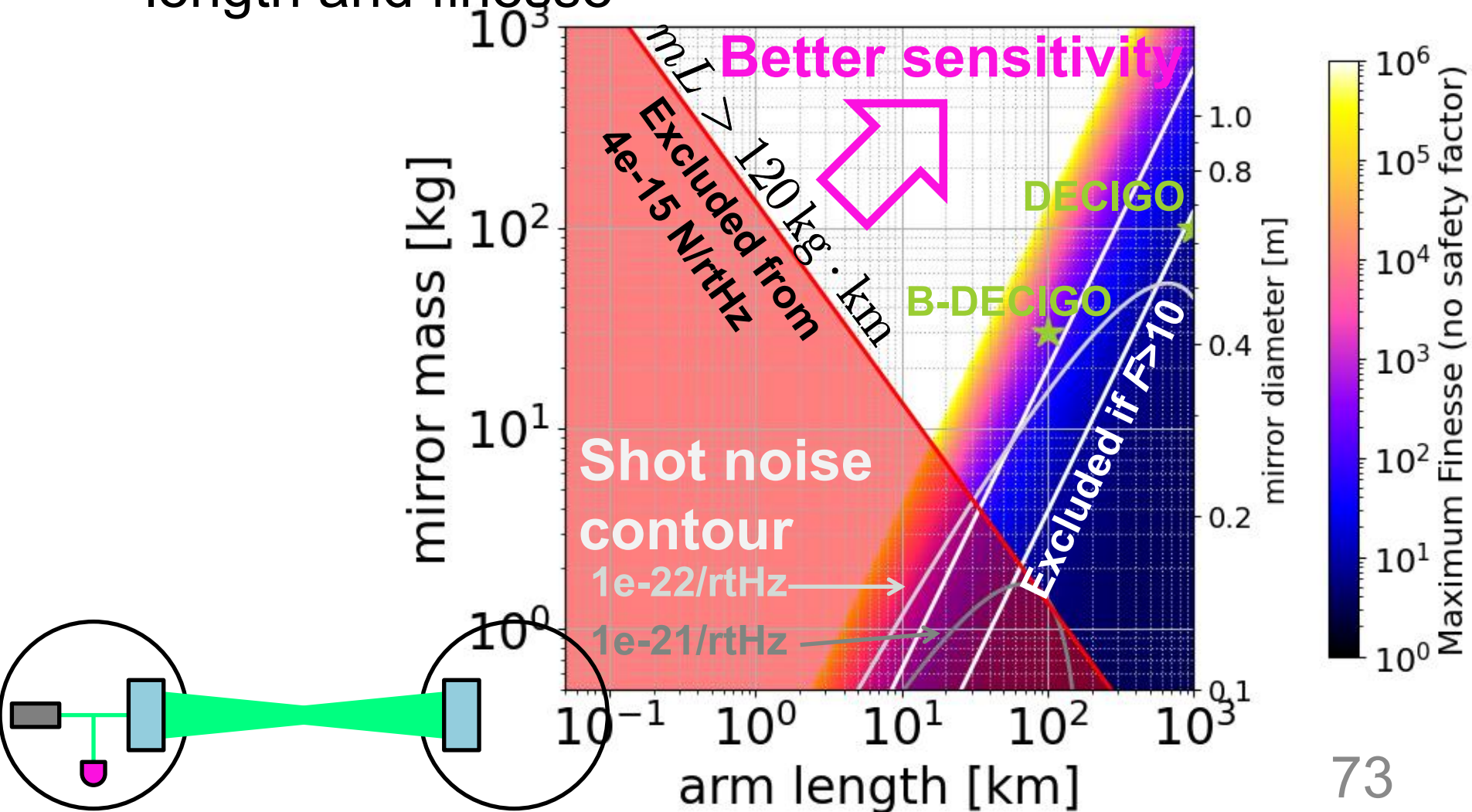
Assuming

- fused silica density,
- aspect ratio $2r/t=3$
- g-factor $g=-0.65$



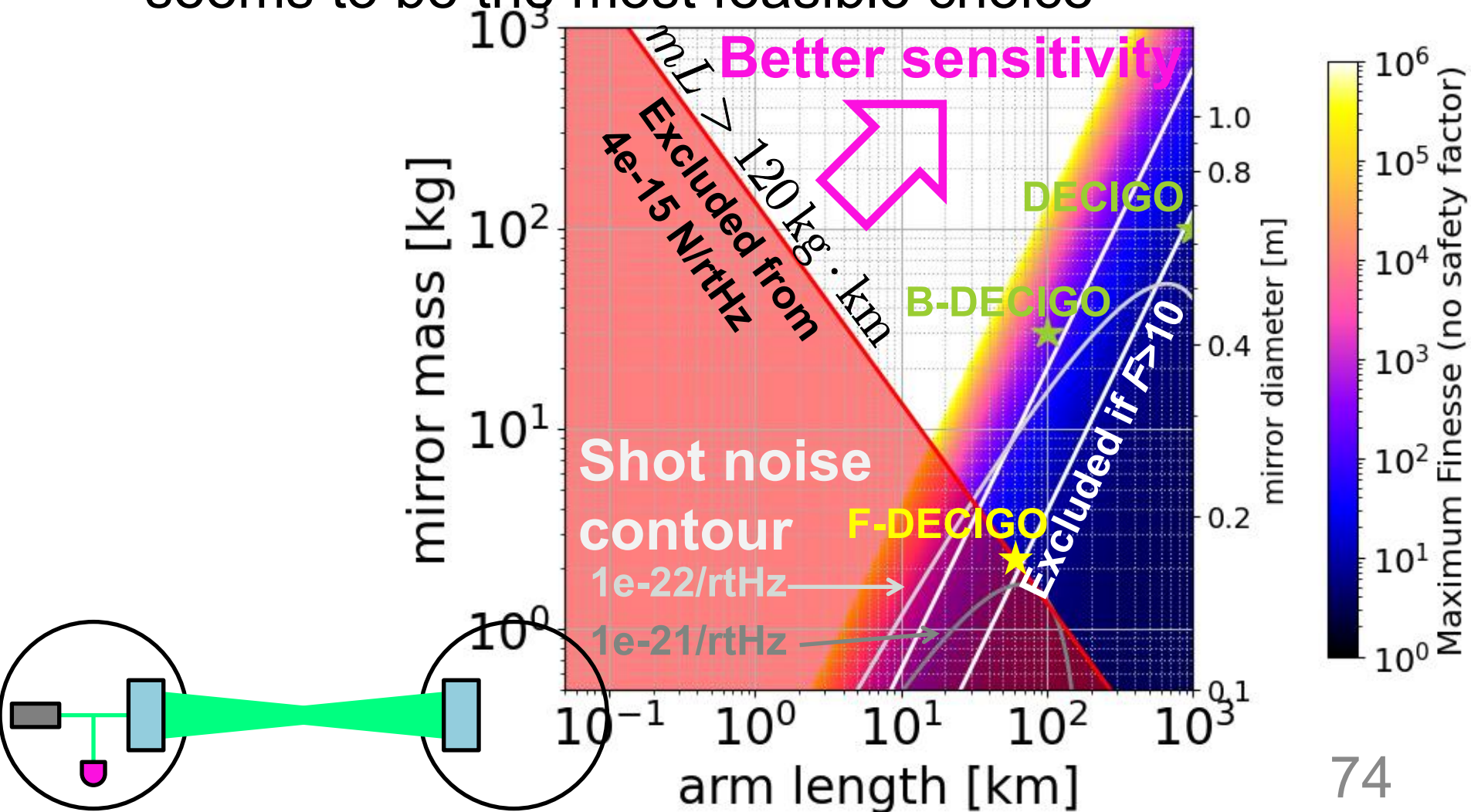
Mirror Size and Arm Length

- **Shot noise** can also be calculated from the arm length and finesse



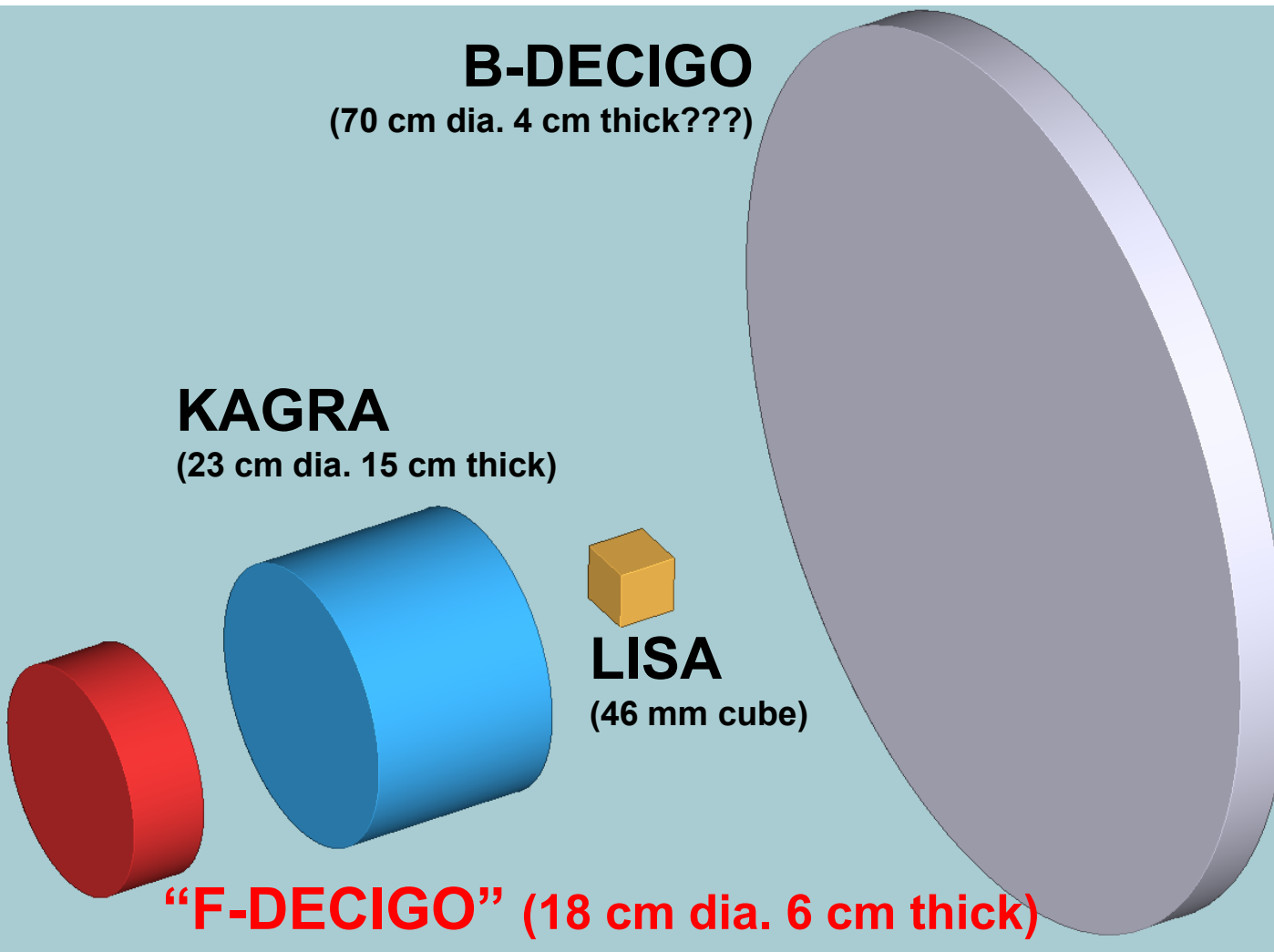
Mirror Size and Arm Length

- Arm length of **60 km**, mass of **2 kg**, Finesse of **10** seems to be the most feasible choice



Mirror Size and Arm Length

- Arm length of **60 km**, mass of **2 kg**, Finesse of **10** seems to be the most feasible choice



60 km & 2 kg “F-DECIGO” Concept

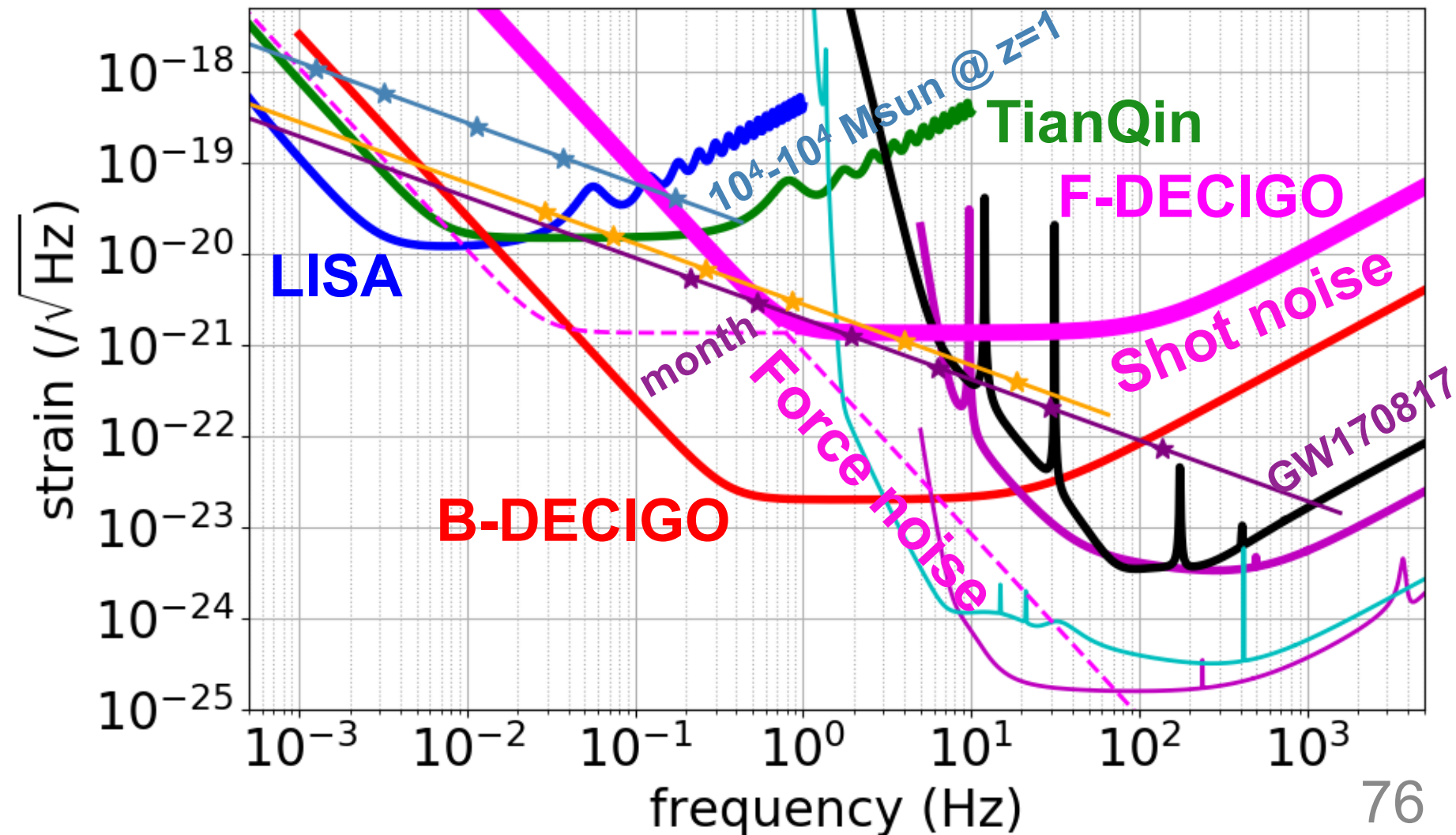
- Barely meets the goal

Proposed in 2019

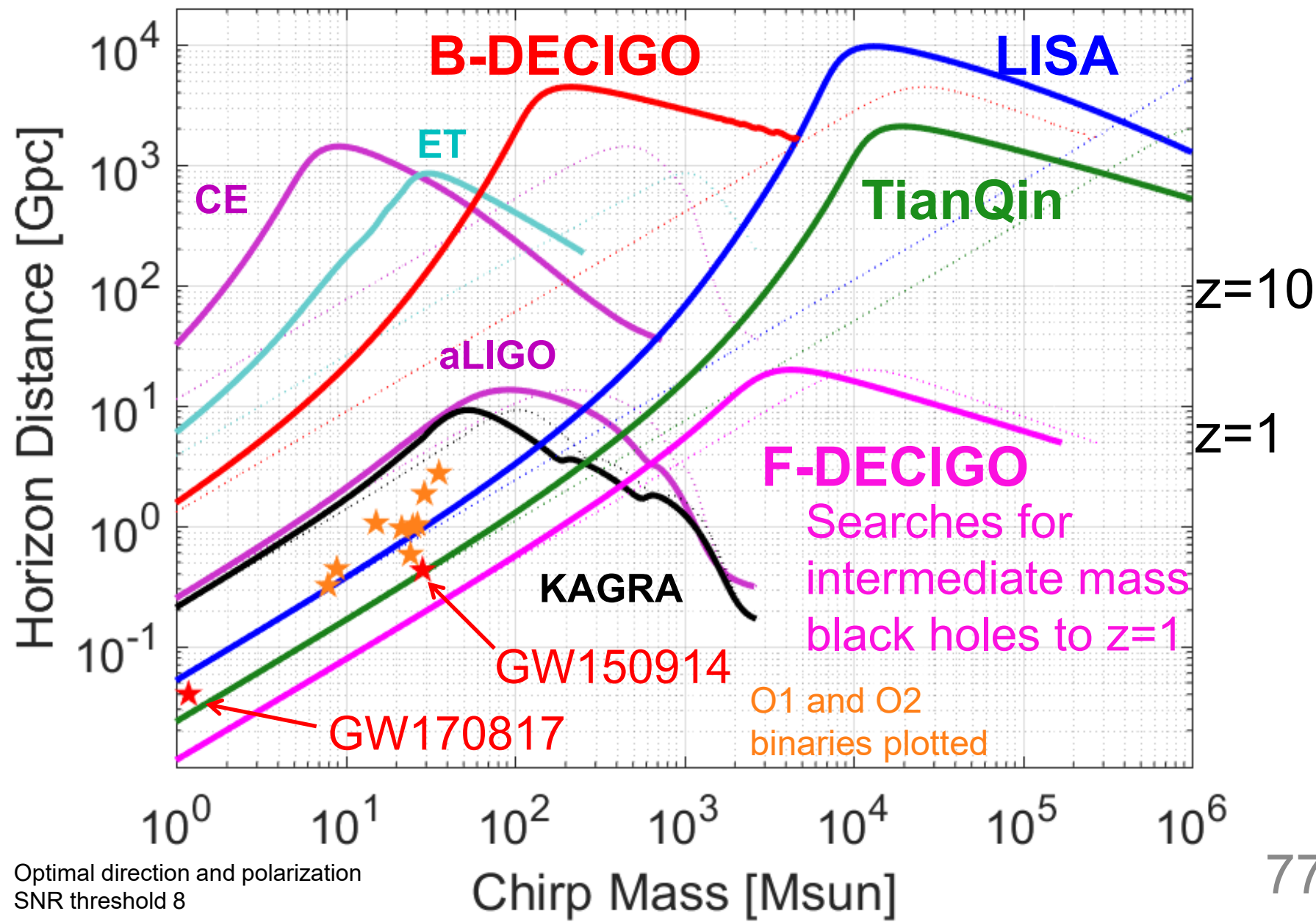
[日本物理学会2019年秋季大会](#) @山形大学

[第18回DECIGO Workshop](#) @京都大学

Later FF-DECIGO → SILVIA

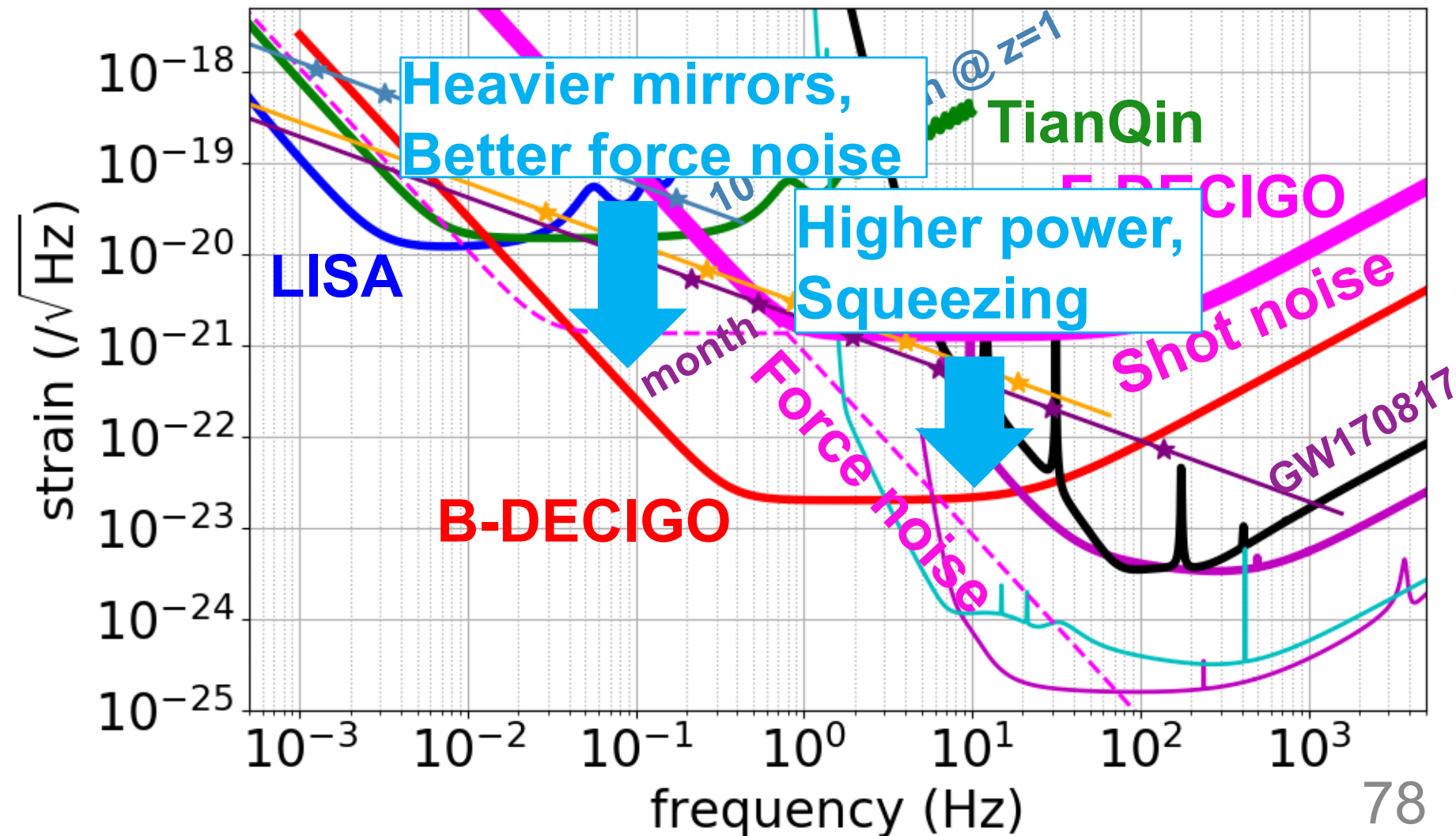


Horizon Distance



Beyond F-DECIGO Concept

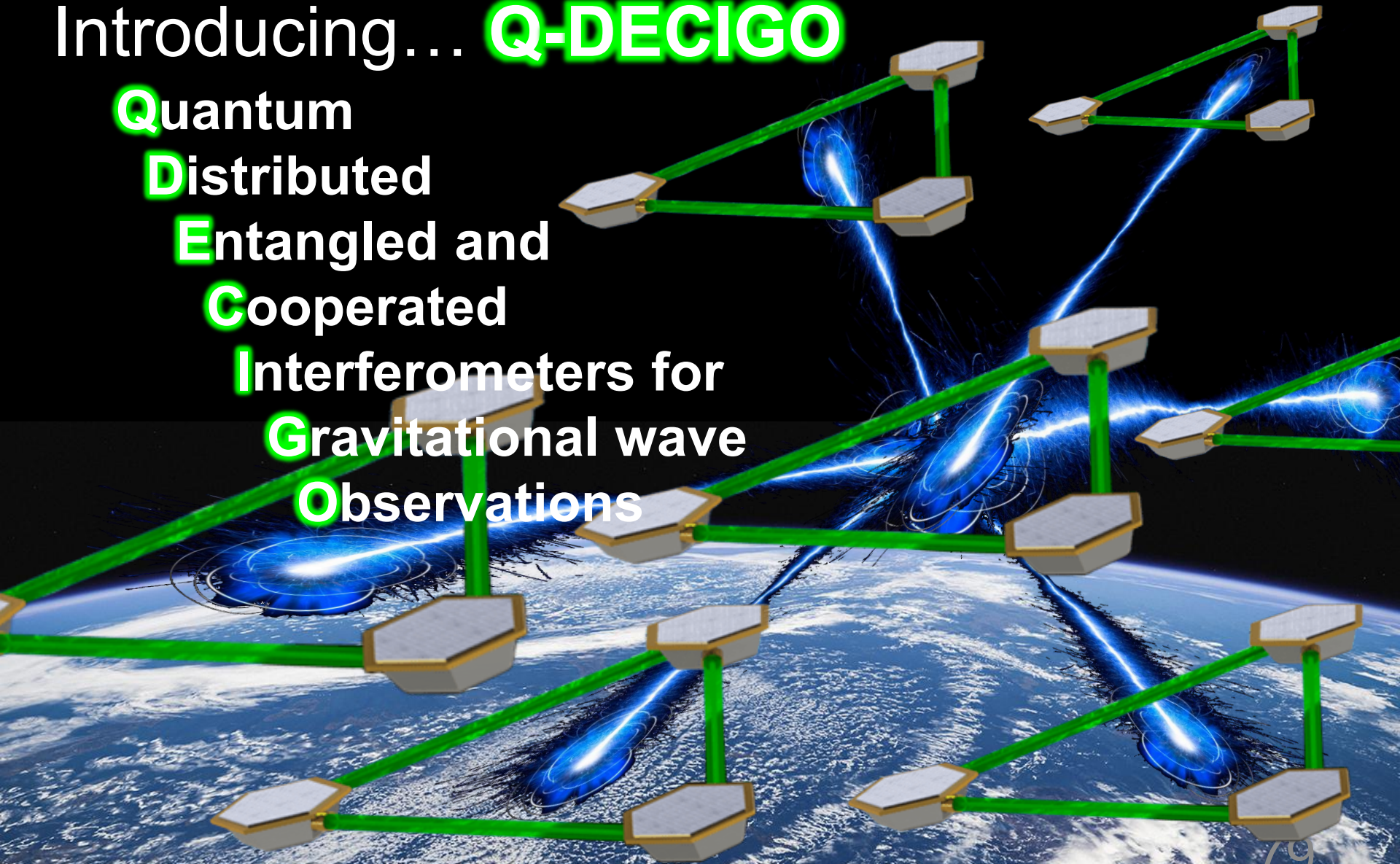
- Heavier mirrors are required for better range



Not Satisfied?

Introducing... **Q-DECIGO**

Quantum
Distributed
Entangled and
Cooperated
Interferometers for
Gravitational wave
Observations

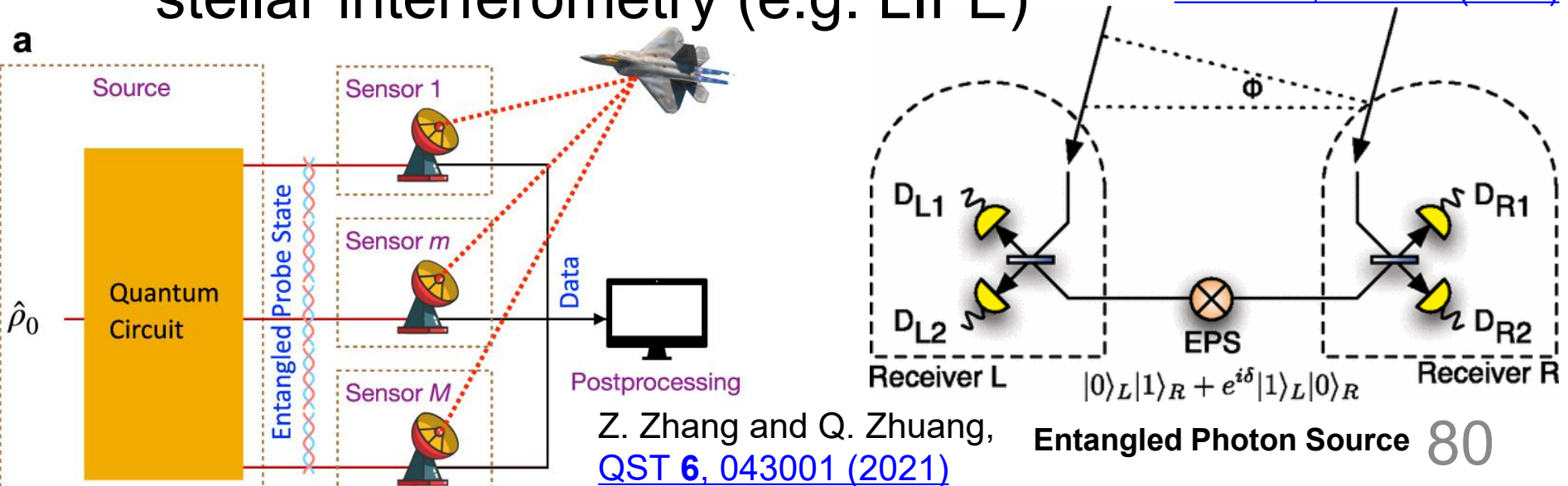


Distributed Quantum Sensing

- By entangling sensing nodes, Heisenberg scaling is possible ($\propto N$ instead of standard quantum limit scaling $\propto \sqrt{N}$)
- ~ 100 of feasible F-DECIGO would make B-DECIGO sensitivity
- Can also be applied to long baseline stellar interferometry (e.g. LIFE)

Caveat: Will not work on classical force noise.
Have heavier reference proof mass?

D. Gottesman+,
[PRL 109, 070503 \(2012\)](#)

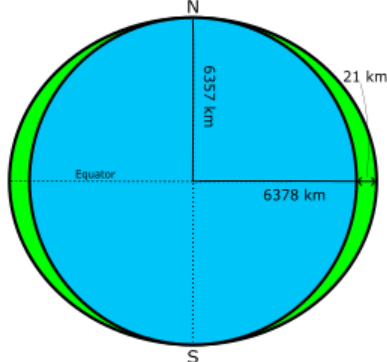


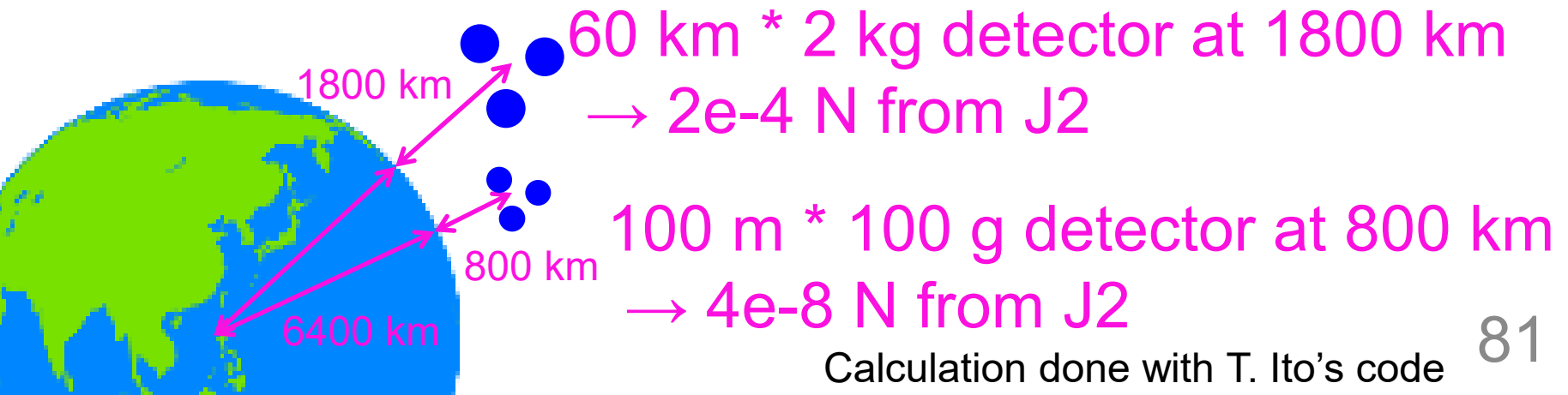
Q-DECIGO Orbit

- If geocentric orbit, relative force from Earth **J2 term** is proportional to mL

$$f_{J_2} = ma_{J_2} \sim \frac{3J_2 G M_E R_E^2}{2(R_E + H)^5} mL$$

J2 coefficient Earth mass Mirror mass Arm length
 Earth radius Orbital altitude





J2 Term and Sensitivity

- If orbital **altitude** and **actuator dynamic range** is given, achievable strain sensitivity can be calculated

$$h = \frac{\delta f}{m\omega^2 L} = \frac{f_{J_2}/D_R}{m\omega^2 L} \sim \frac{3J_2GM_E R_E^2 / \overset{\text{dynamic range}}{D_R}}{2\omega^2 (R_E + H)^5}$$

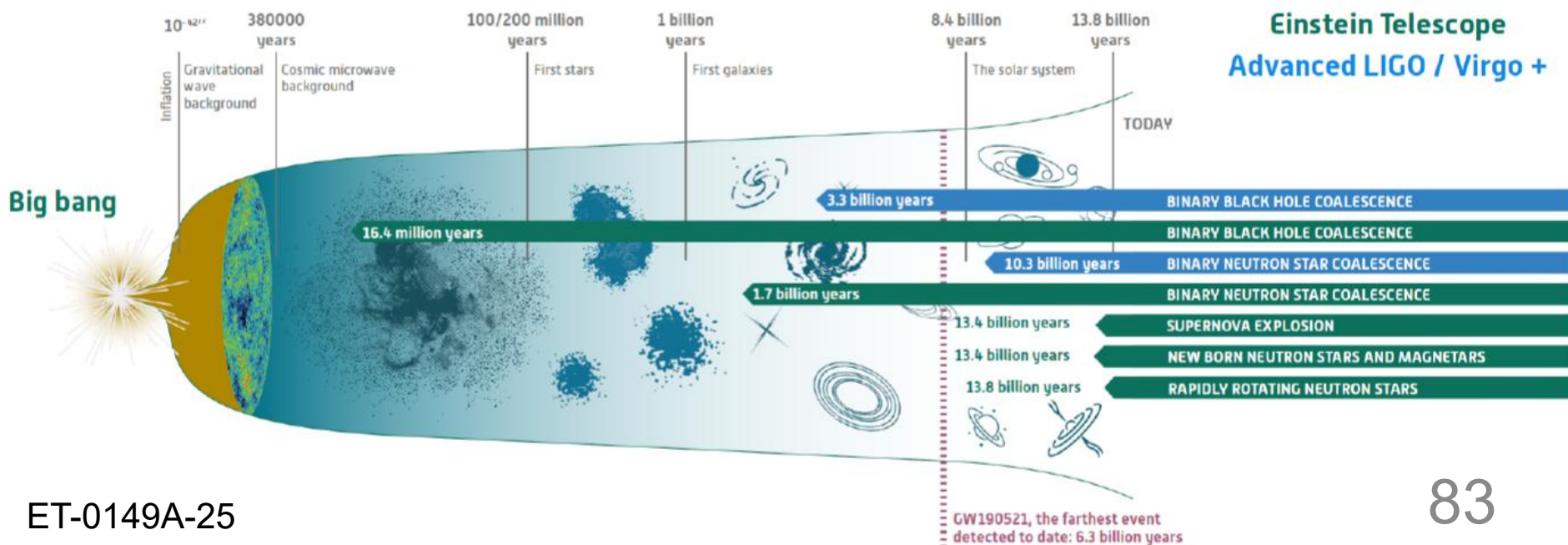
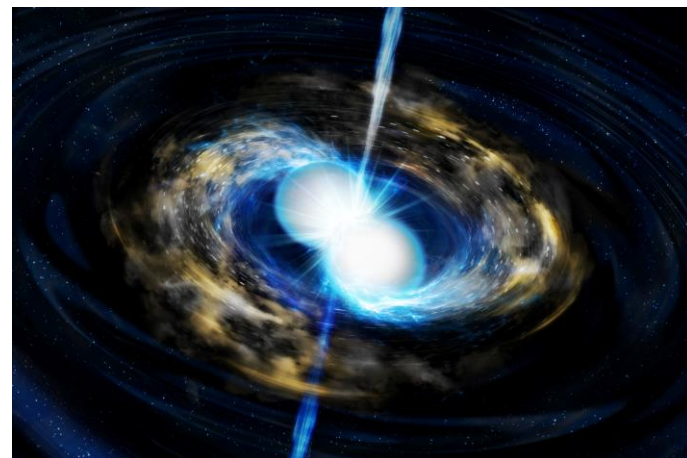
$$< 3 \times 10^{-21} / \sqrt{\text{Hz}} @ 0.5 \text{ Hz}$$

This requires altitude **higher than 3.3e7 m**
 with dynamic range 10^7 rtHz
 (**Geosynchronous orbit** 3.6e7 m will do)

- This cannot be avoided by increasing mL
 → **Low Earth orbit won't work**. Back-linked?

Summary

- The future is bright and loud!
- The future is yours to shape!



Assignment for Dec 5

- Describe your overall impressions of the lectures and list up the topics you want to study further.
- You may also answer from the Google Form below <https://forms.gle/6AwJ48XcpWQXqMon9>

Don't forget to put
your name and
student#

You may answer in
any language

