

Research plan I: Optomechanical torsion pendulum

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Lab seminar 2022/09/30

Abstract

- Research plans
- Motivation
- Current status and future of the optomechanical torsion pendulum

My research plans

➤ Optomechanical torsion pendulum

- Research plan I, today's talk

➤ Sideband cooling of a macroscopic pillar to its ground state

- Research plan II, probably talking at my next term

➤ Demonstration of the long signal recycling cavity and search for high-frequency GWs

- After the next?

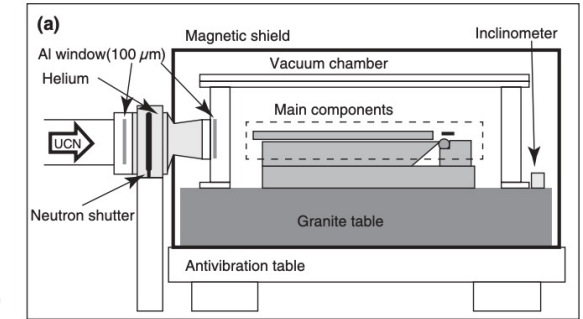
➤ Test of continuous spontaneous localization with a thin wire

- Future?

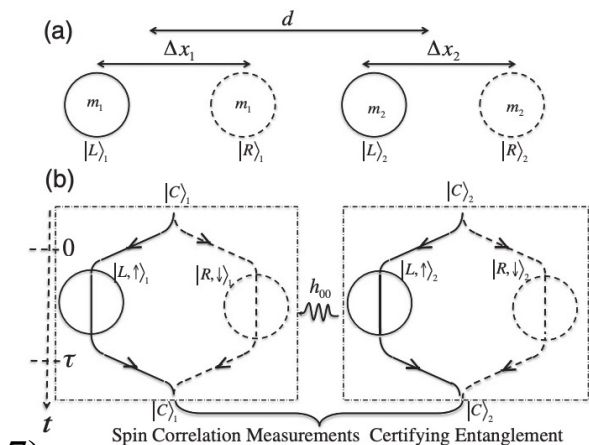
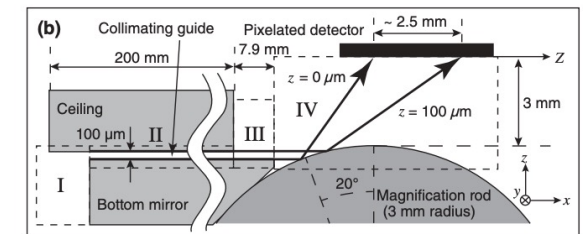
Motivation

- Quantum state in the classical gravity field?
 - Neutrons keep the quantum state in the Earth's gravity

PRL 112, 071101 (2014)



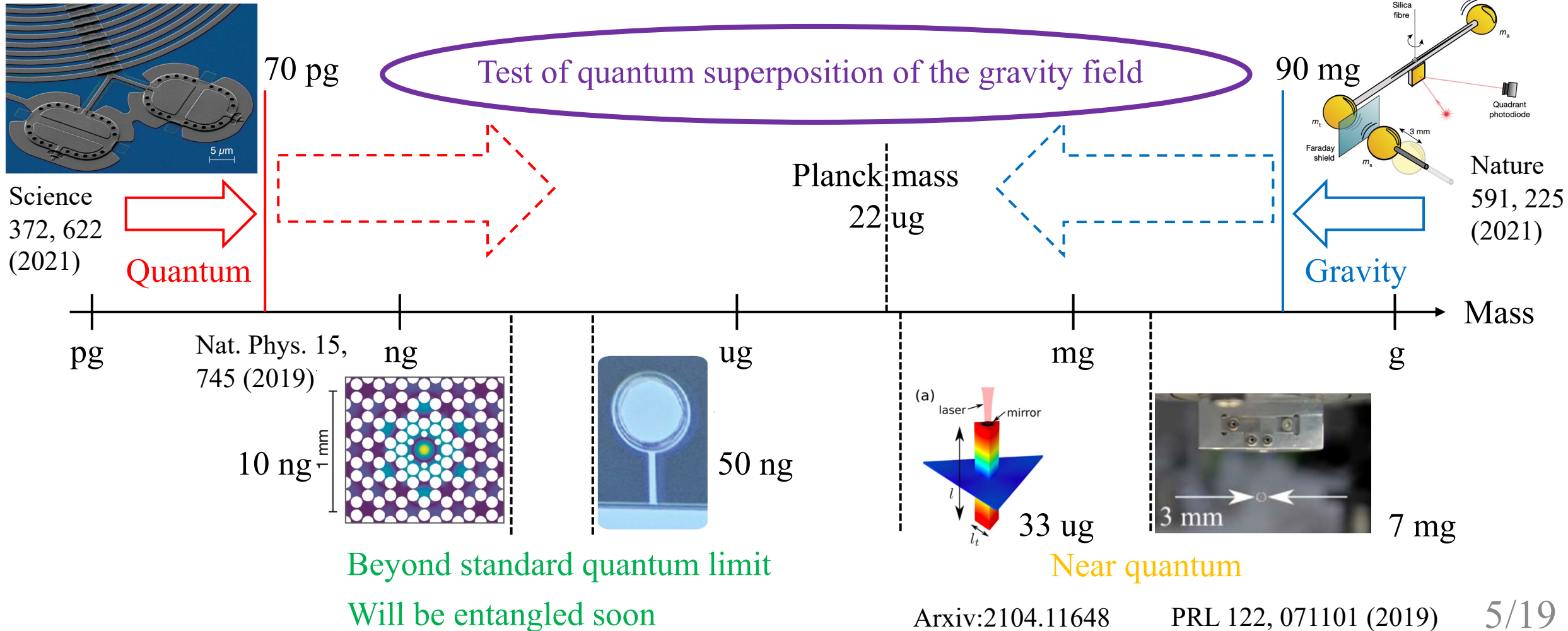
- Should gravity be quantized?
 - Theory of the quantum gravity has not been completed
 - Some experiments are proposed to test it (e.g. spin and matter-wave interferometer)
 - Some counter theories “gravitational decoherence” are also proposed (e.g. CSL, DP model)



PRL 119, 240401 (2017)

Quantum and gravity

➤ The massive quantum (70 pg) and the lightest gravity (90 mg)

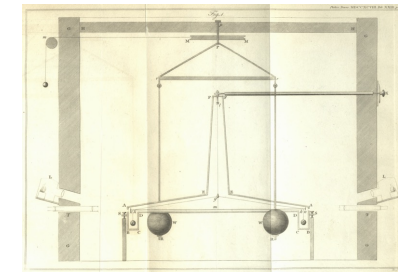


Torsion pendulum

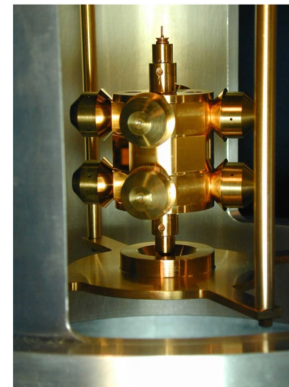
- Very sensitive to tiny force
 - Ultra-small restoring torque: $K \propto \phi^4$
 - Suspension with an O(um) diameter wire leads to O(mHz) resonant frequency

- Gravity measurement

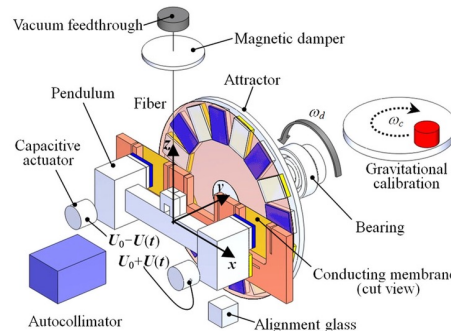
- Cavendish's experiment (G measurement)
- Equivalence principle
- Inverse law



Philos. Trans. R. Soc. London (1798)



CQG 29, 184002 (2012)



PRL 116, 131101 (2016)

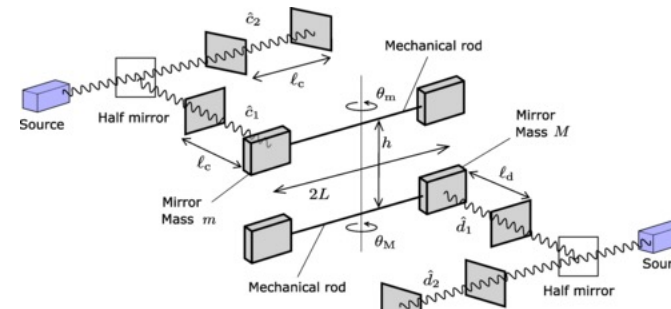
Optomechanical torsion pendulum

➤ Theoretical proposal

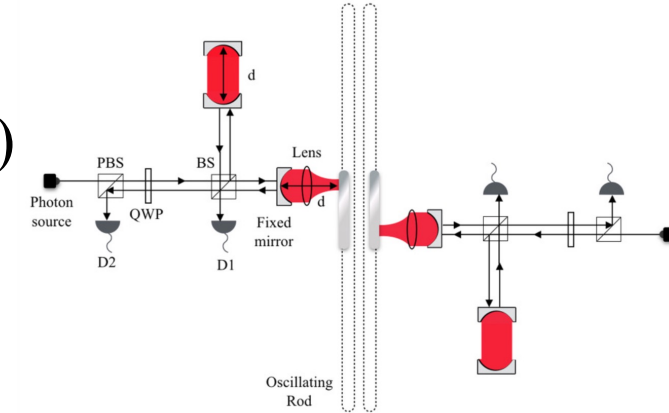
- Quantum Cavendish (superposition of the torsion pendulum)
- Test of gravity-induced entanglement

➤ Experiment

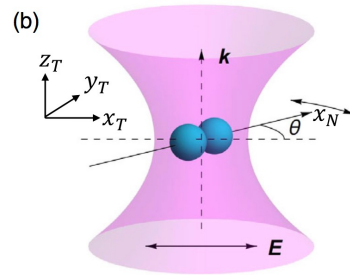
- GHz nano-rotor
- Um-pg-torque sensor
- Mm-mg-scale paddle



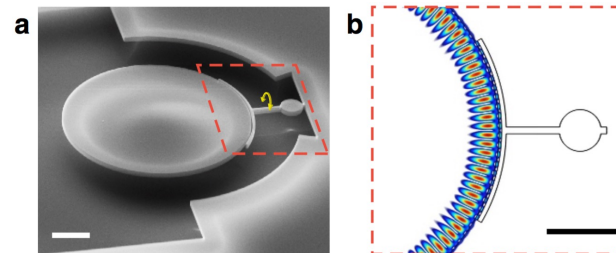
PRD 102, 106021 (2020)



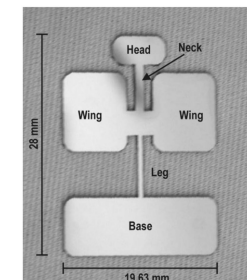
PRA 98, 043811 (2018)



PRL 121, 033603 (2018)



Nat. Comm. 7, 13165 (2016)



Rev. Sci. Instrum.
78, 025101 (2007)

My work

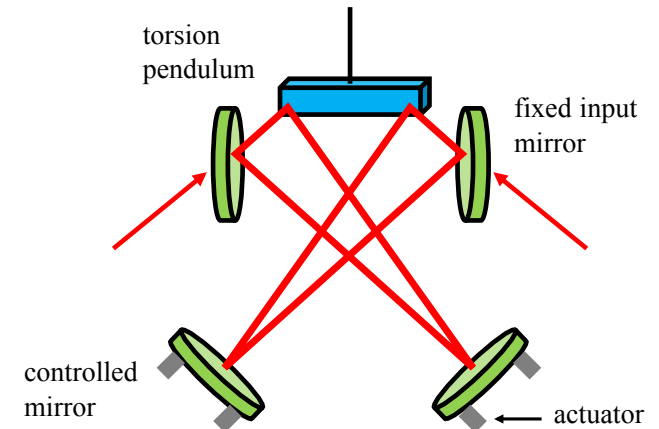
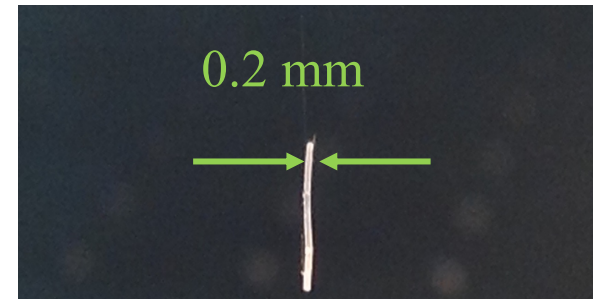
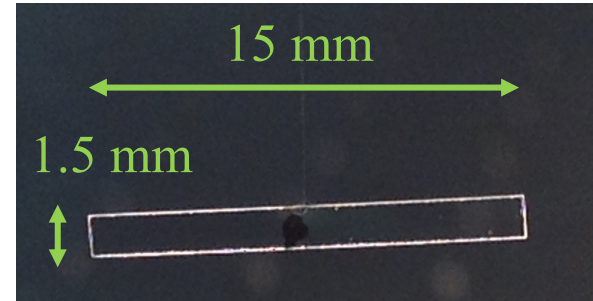
- 10-mg bar mirror suspended by a carbon fiber (6μm diameter)
- Triangle cavities avoid the angular instability as similar to Matsumoto-san's triangle cavity
- Low suspension thermal noise because of the low resonant frequency

$$S_{\tau}^{th}(\omega) = 4k_B T l \frac{\omega_m^2}{Q_m \omega}$$

Resonant frequency: quadratic

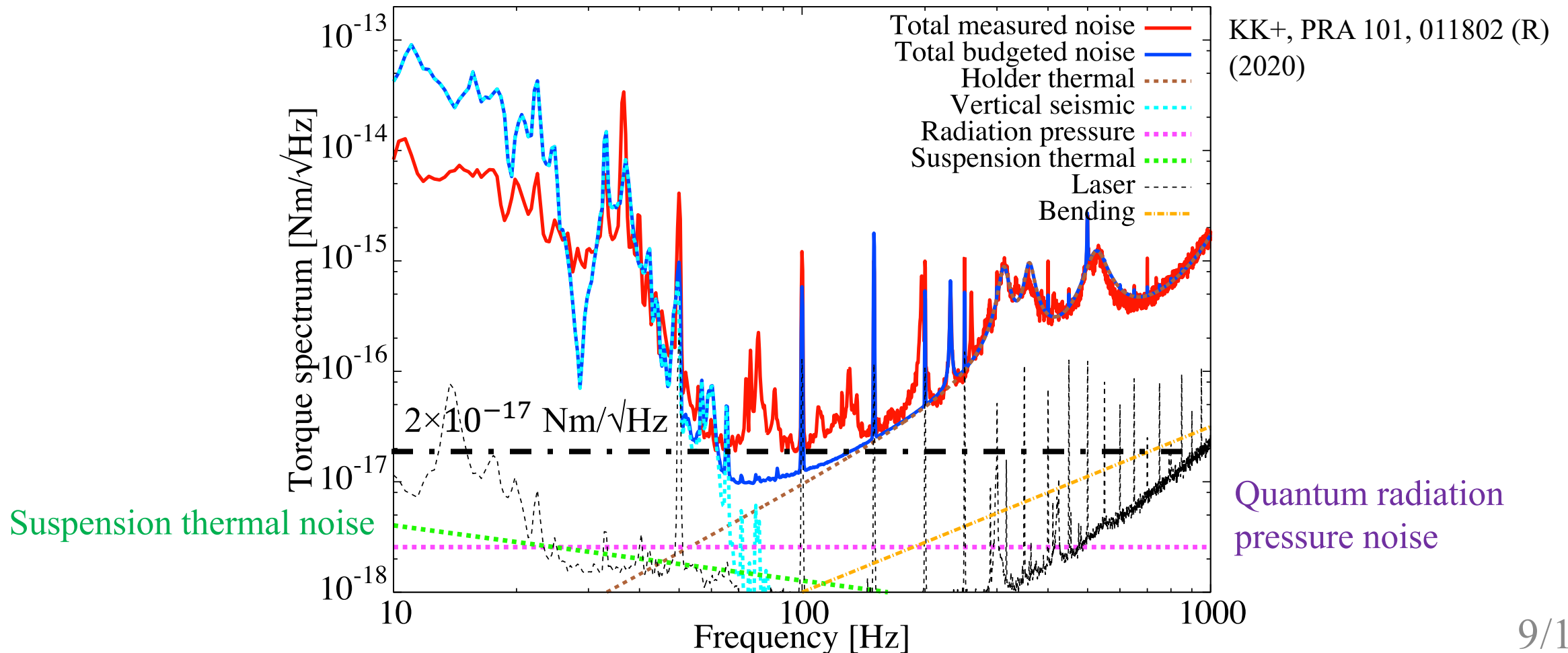
Q-value: linear

- Subtracting two signals to measure rotational mode and reduce noises from translational mode



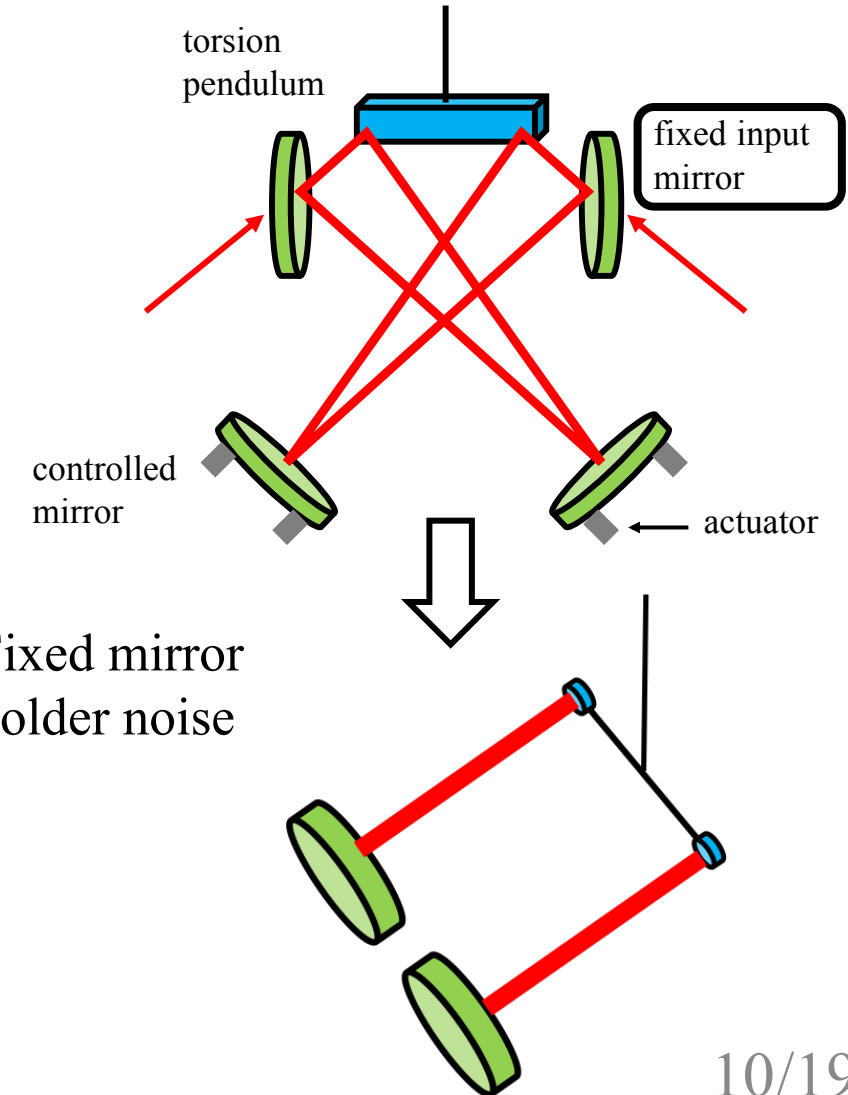
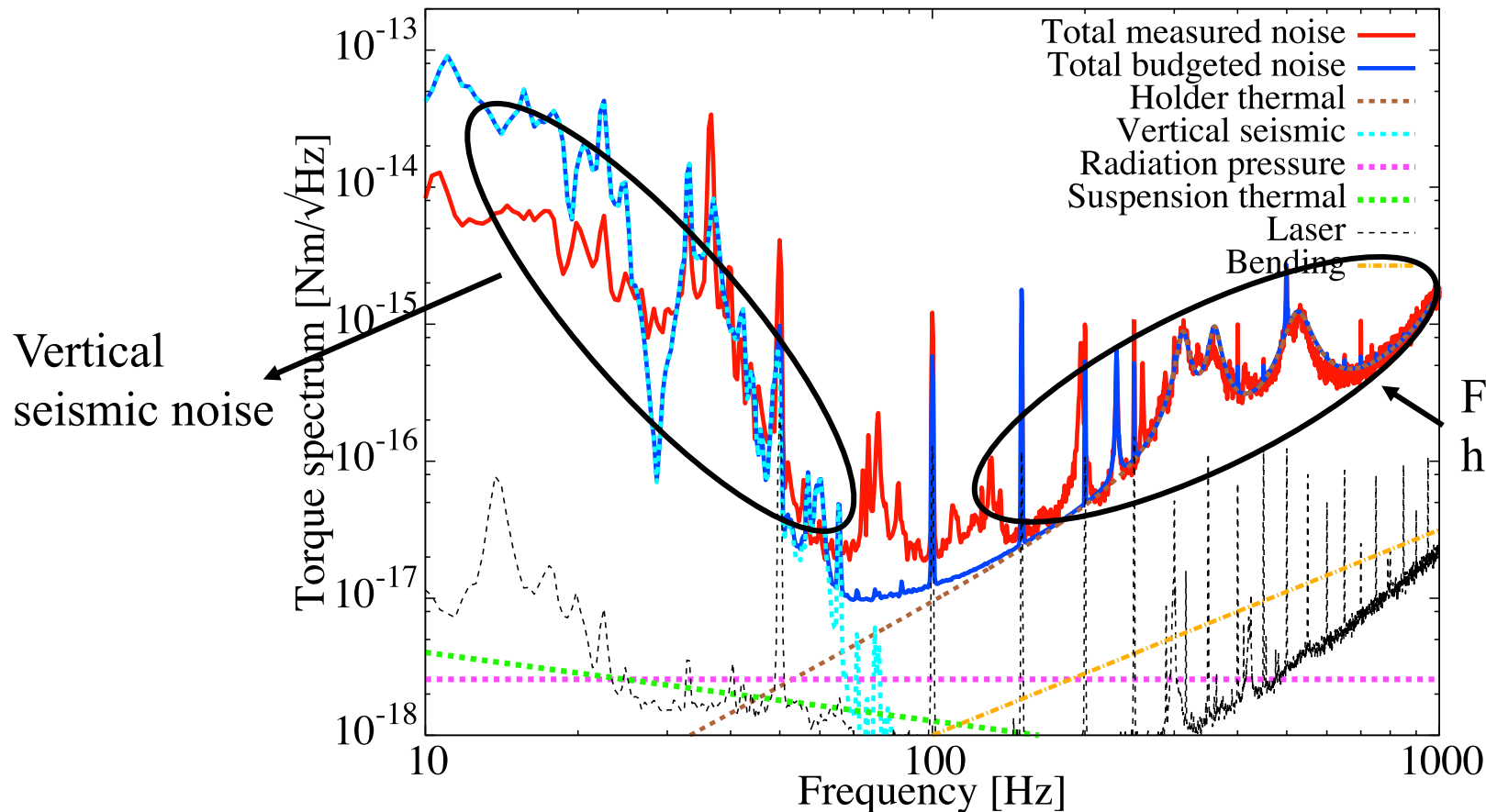
Result

➤ Best sensitivity of 20 aNm/ $\sqrt{\text{Hz}}$ in mg-scale torque sensors



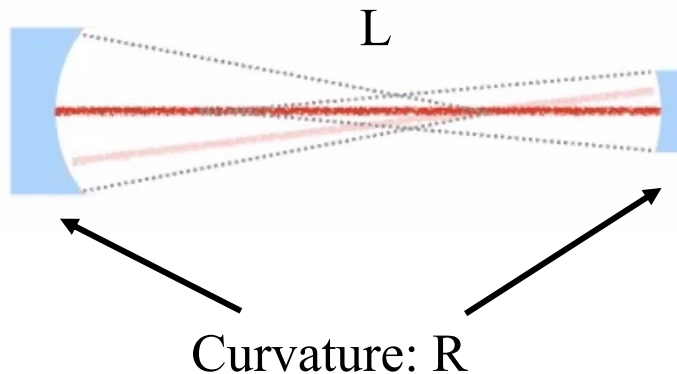
Improvement

- Removing the fixed mirror to eliminate the holder noise and reduce the vertical coupling

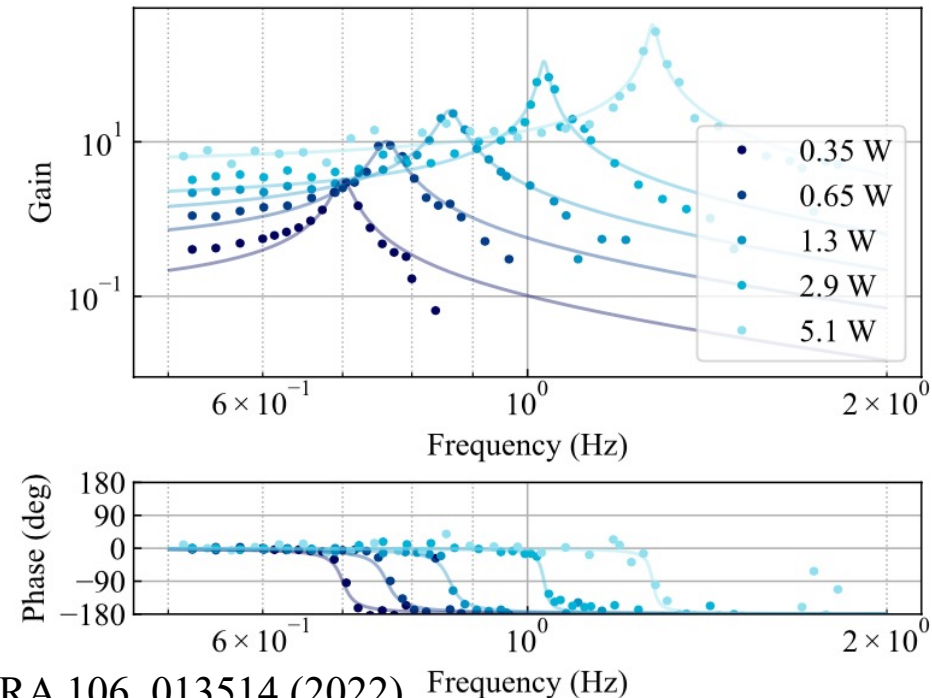


Angular stability

- Demonstration of the angular stability even in the linear cavity
- Two curved mirrors
 - The curvature smaller than the cavity length leads to the angular stability
 - Larger power increases the resonant frequency of the rotational mode



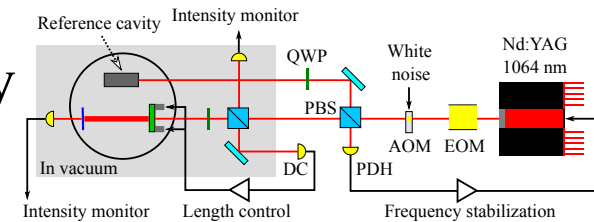
$R < L$: stable



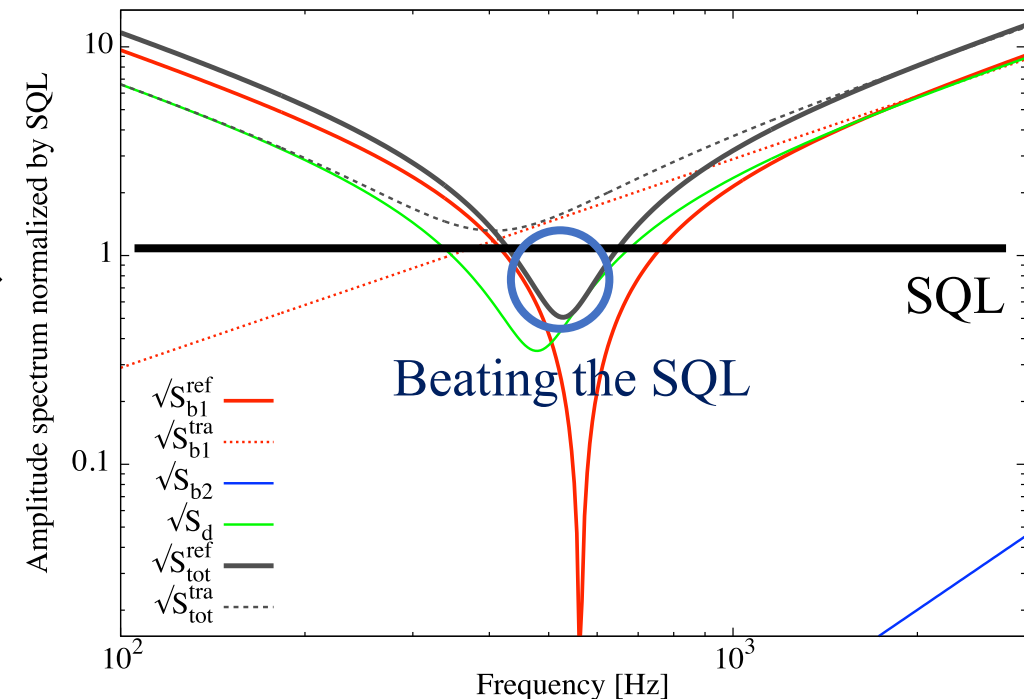
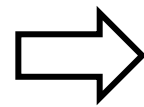
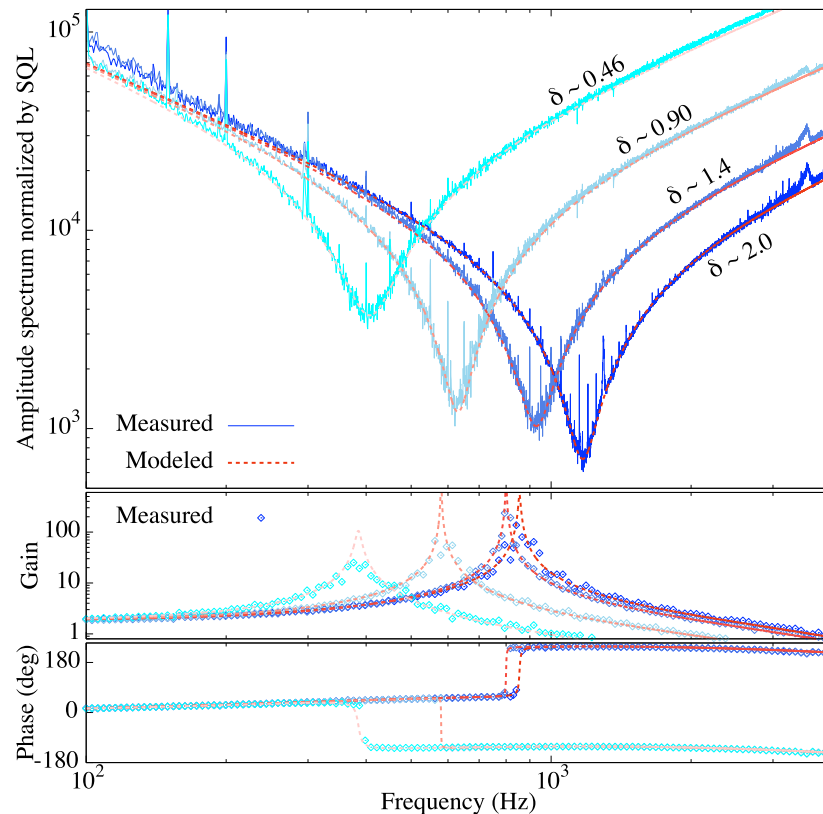
New back-action evasion

➤ Demonstration of reducing back-action (radiation pressure) noise

- Just measuring amplitude of reflected light from the cavity
- The amplitude fluctuation is cancelled at the specific frequency



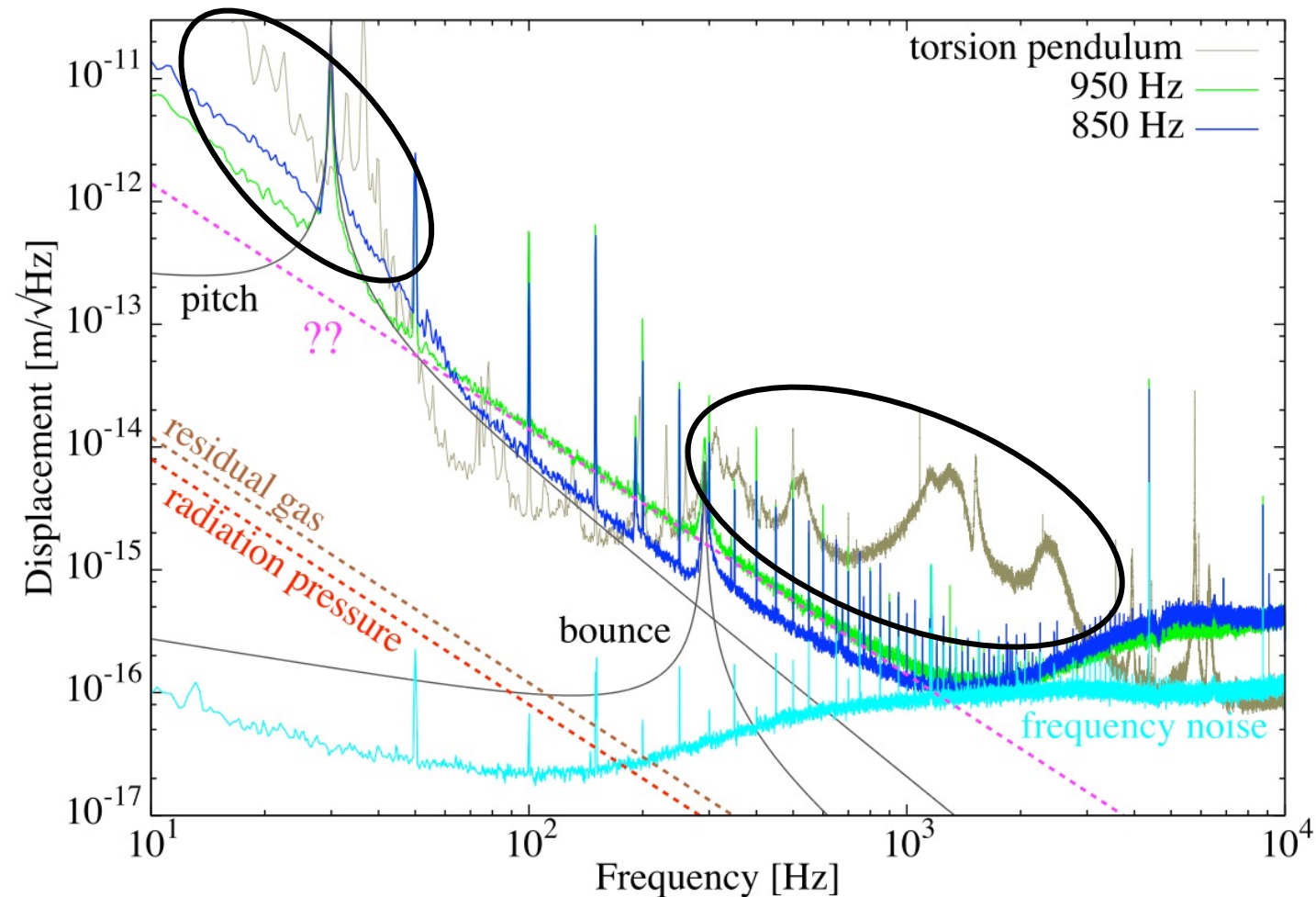
KK+, PRA 104, L031501 (2021)



Discussion on the noise

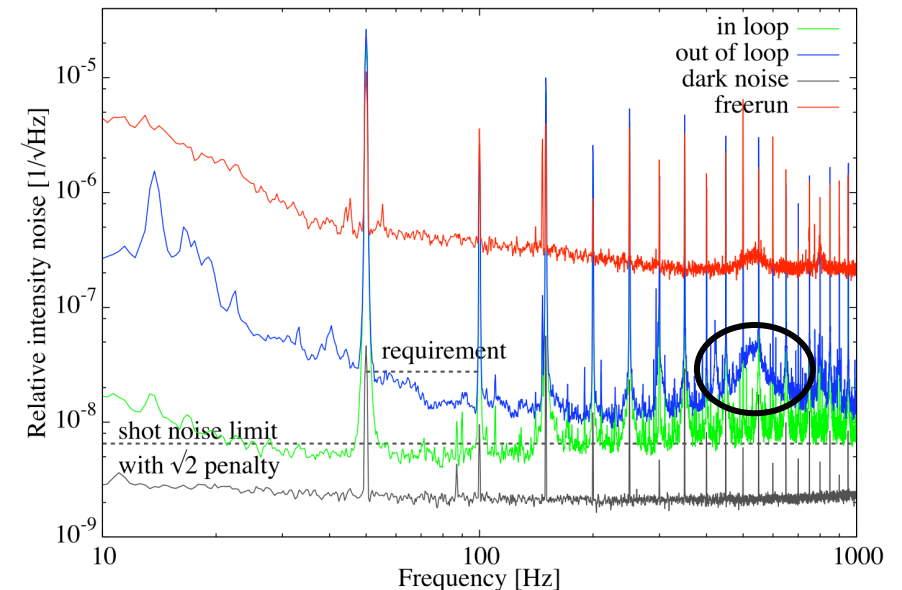
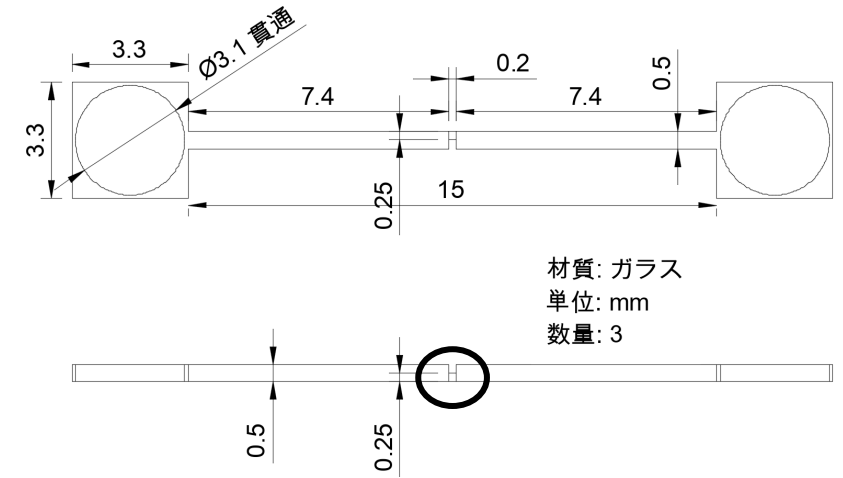
➤ Comparing the linear cavity and the torsion pendulum triangular cavity

- No mirror holder noise
- Much lower vertical seismic noise
- Adjustment of the beam spot will improve the noise more
- The dependence of f^{-2} is mysterious



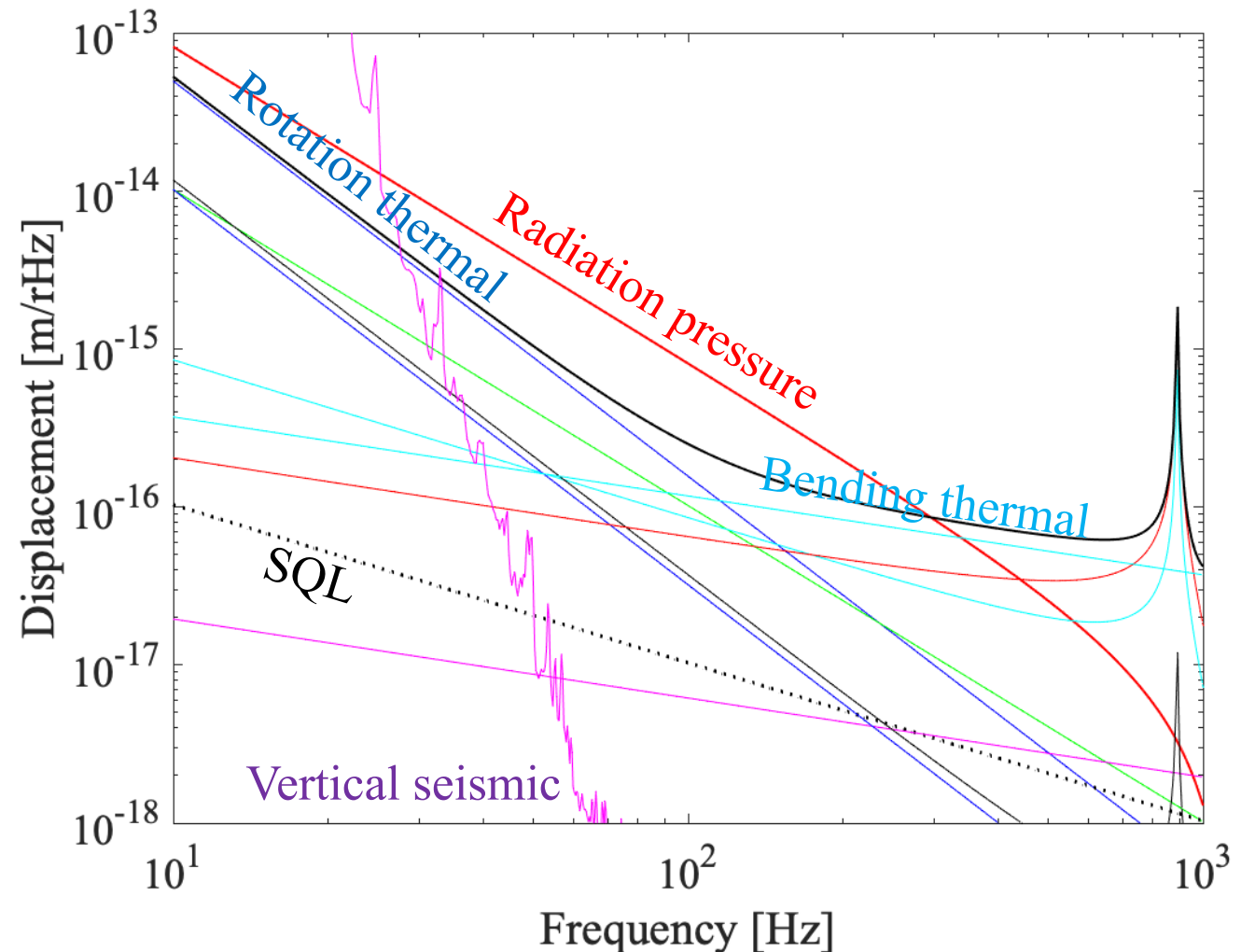
Planned improvement

- New torsion pendulum: dumbbell type
 - Spacer with two holes for the curved mirror at each edge (Opto-science and NSC)
 - Optical contact with the curved mirror and the rectangular solid (Sigma-koki)
 - Suspending at the center of mass to reduce the pitch coupling
- Intensity stabilization
 - Additional noise from the AOM driver
 - Electrically noisy
 - Replacing the AOM with the EOAM



Design sensitivity

- Radiation pressure dominant from 30 Hz to 300 Hz
- Vertical seismic noise will limit at low frequencies
- Bending thermal noise will limit at high frequencies



Interesting note

- Giving analytical expressions of the radiation pressure noise in the amplitude measurement of reflection

$$S_F^{rad} \simeq \frac{8\hbar\omega_L}{c^2} \frac{P_{in}}{T_{loss}^2} \quad (\omega \ll \omega_{opt})$$

$$S_{b_1}^{ref} = \frac{(\kappa^2 + \Delta^2)\{\Delta\iota - [(\kappa - 2\kappa_{in})^2 + \Delta^2]\omega^2\}^2}{16\iota\kappa_{in}(\kappa - \kappa_{in})^2\Delta^2\omega^2},$$

$$S_{b_1}^{tra} = \frac{\kappa_{in}(\kappa^2 + \Delta^2)\omega^2}{\iota\Delta^2},$$

$$S_{b_2} = \frac{\kappa_{in}\omega^4}{\iota(\kappa^2 + \Delta^2)},$$

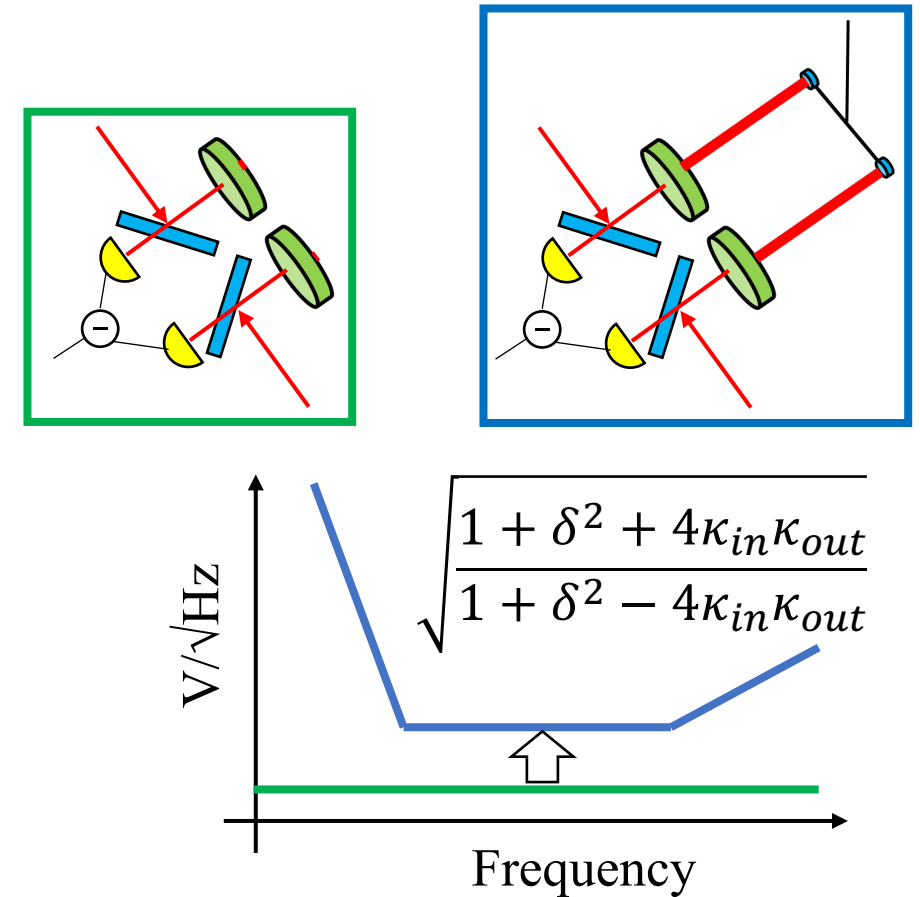
- Depending only on the optical loss at low frequencies

$$S_d = \frac{[\Delta\iota - (\kappa^2 + \Delta^2 - 2\kappa\kappa_{out})\omega^2]^2}{4\iota\kappa_{out}\Delta^2\omega^2} + \frac{\kappa_{out}\omega^2}{\iota},$$

- Large T_{in} (smaller finesse) leads to the soft optical spring and the test mass moves more easily
- Larger finesse means the stiff spring, in the end, the displacement does not change
- T_{loss} determines how over-coupled the cavity is, so that the slope of the cavity resonance fringe changes linearly in the amplitude (quadratic in the power spectrum)

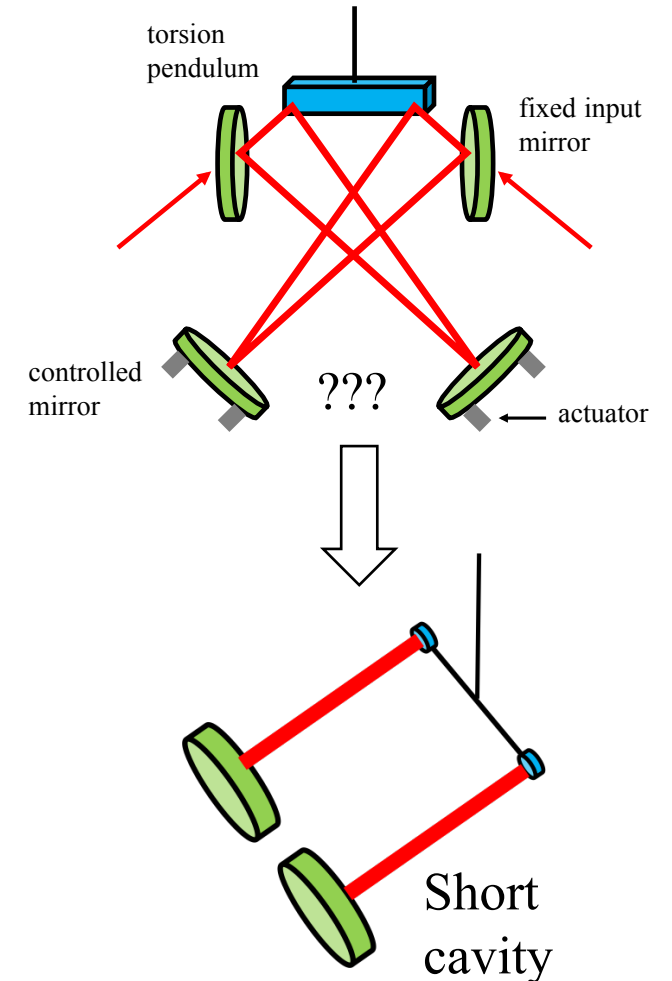
Measured spectrum

- Targeting frequency is around 100 Hz, which is much smaller than the optical spring frequency ~ 1 kHz
- Feedback only around the optical spring and small openloop gain at 100 Hz (error signal measurement)
- Slight increasing from the shot noise without the cavity
 - A factor of ~ 1.3 with $\kappa_{in} = 0.9, \delta = 1/\sqrt{3}$



Recent consideration

- Is the negative g-factor necessary?
- It is necessary for the simple pendulum cavity
- In the case of the torsion pendulum, the optical springs at the edges overwhelm the anti torque spring
- Short cavity (positive g-factor) is still acceptable so that the frequency noise can be reduced?



Summary

- My research plans including the optomechanical torsion pendulum
- Motivation of the macroscopic quantum state
- Current status and future plan toward observation of the quantum radiation pressure fluctuation