

# DM research at SYRTE: an overview

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Paris-Tokyo seminar, March 5, 2021

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M. Abgrall, S. Bize, E. Cantin, L. Cros, F. Frank, J. Guéna, P-E Pottie, B. McAllister, O. Minazzoli, M. Tobar, Y. Stadnik

# Menu

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- Dark matter (DM) overview
- Ultralight dark matter and time/frequency metrology
- **DM interacting with standard model spins**
- **Non-universally coupled scalar field**
- **Atomic spectroscopy optical cavities and Universality of free fall**
- **Experiments at SYRTE and friends**
- Conclusion and Outlook

[Hees, Guéna, Abgrall, Bize, Wolf, PRL **117**, 061301, 2016]

[Hees, Minazzoli, Savalle, Stadnik, Wolf, PRD **98**, 064051, 2018]

[Alonso, Blas, Wolf, JHEP **69**, 2019]

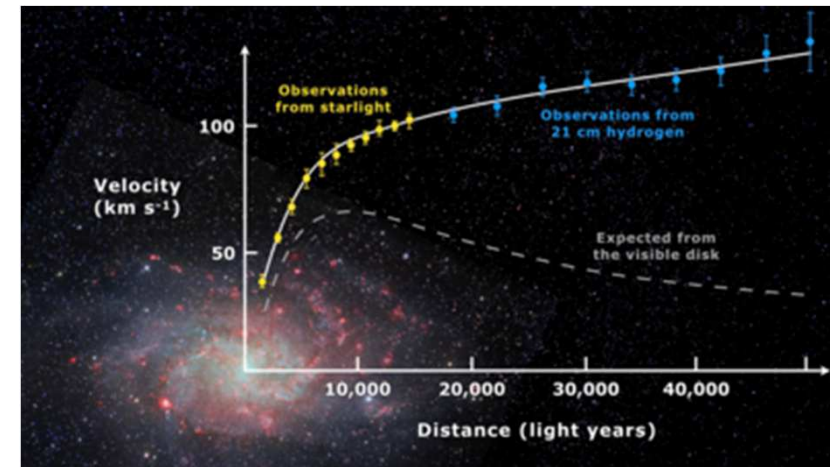
[Wolf, Alonso, Blas, PRD **99**, 095019, 2019]

[Roberts, et al., NJP **22**, 093010, 2020]

[Savalle E. et al., PRL **126**, 051301, 2021]

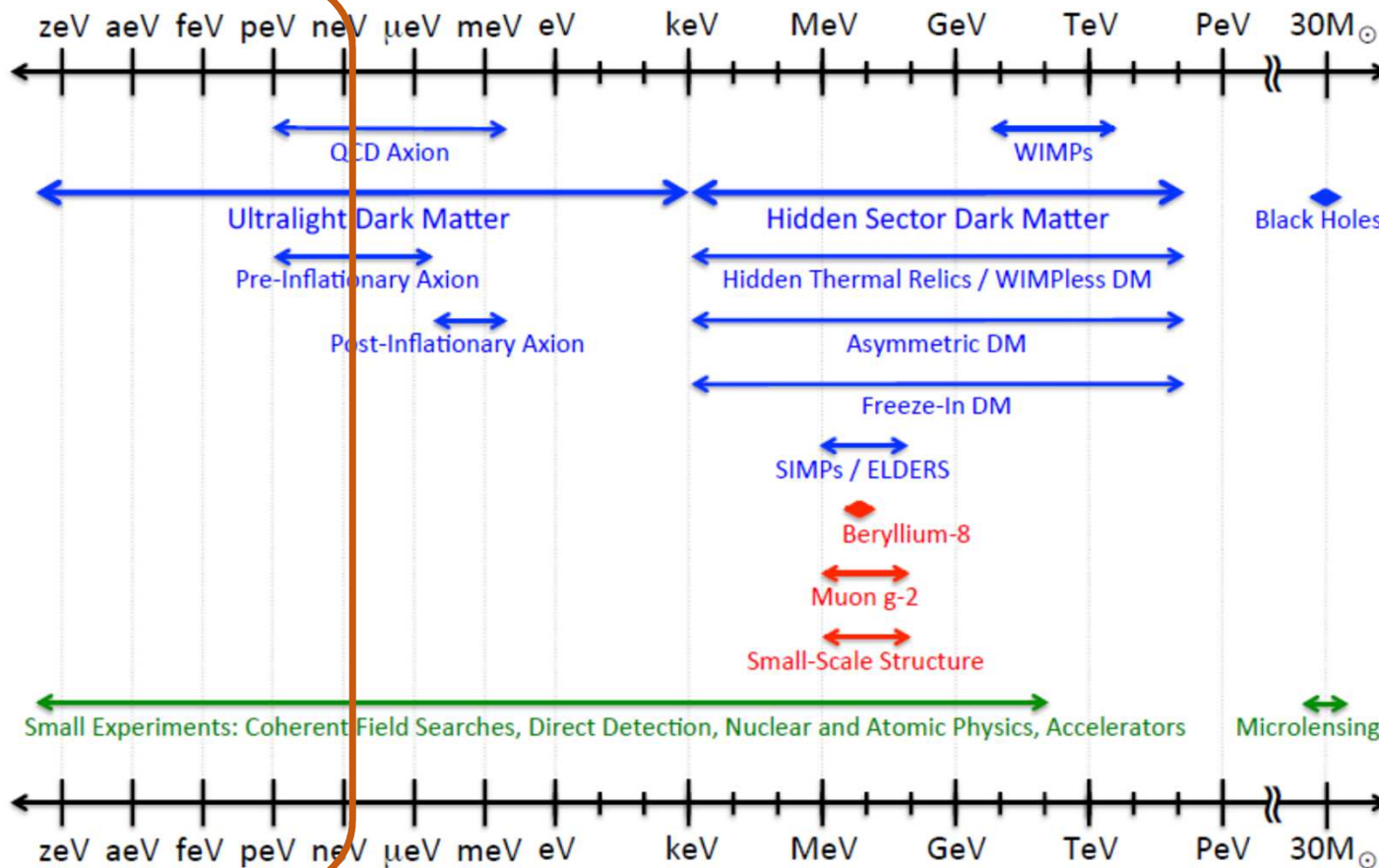
# Dark Matter (1)

- “Evidence” for DM is purely gravitational, but of several types e.g.:
  - Galaxy rotation curves
  - Gravitational lensing
  - Cosmic Microwave Background
  - Structure formation
  - ...
- We “know” that:
  - It is cold ( $v \ll c$ )
  - Forms a galactic halo
  - Has virialized in the galaxy ( $\delta v \approx 10^{-3} c$ ,  $\langle v \rangle \approx 0$ )
  - It’s energy density in the solar system is  $\approx 0.4 \text{ GeV/cm}^3$  and  $\langle v \rangle \approx 10^{-3} c$
- We hope that:
  - More gravitational evidence will be obtained to constrain its properties
  - DM interacts other than gravitationally with standard model fields
  - Someone will detect it locally
  - New physics will be learned



# Dark Matter (2)

## Dark Sector Candidates, Anomalies, and Search Techniques



From "US Cosmic Visions: New Ideas in Dark Matter 2017 : Community Report" arXiv:1707.04591

- Spans 90 orders of magnitude in mass !
- Here we will concentrate on low masses.
- In that region standard collisional (recoil based) detection techniques fail.

# Ultralight DM

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$$N_{occ} = \frac{n}{n_{\delta v}} \simeq \frac{3\pi^2 \hbar^3 \rho}{4m^4 \delta v^3}$$

$N_{occ} = 1$  in our galaxy for  $m \approx 10$  eV.

- For  $N_{occ} > 1$  the DM field can be treated as a classical field.
- It is likely to oscillate at its Compton frequency  $\omega = mc^2/\hbar$ .
- It may form “clumps” e.g. topological defects or relaxion stars/halos.
- For  $N_{occ} < 1$  it must be quantized i.e. treated as a particle.
- Fermions cannot have  $N_{occ} > g$  ( $g$  = number of internal degrees of freedom).
- Fermionic DM mass must be  $> eV$ .
- Bosonic DM can be treated as a classical field for mass below 10 eV or so.

# Observable effects

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1. DM fields interacting with the spin of the electrons or nuclei in the atoms.
  - ⇒ Effect on spin dependent atomic transition frequencies (Hyperfine transitions, Zeeman states, ...).
  
2. DM scalar field with non-universal scalar couplings to SM fields.
  - ⇒ Apparent violations of the equivalence principle
  - ⇒ Space-time variation of fundamental constants
  - ⇒ Change of atomic transition frequencies
  - ⇒ Change of Bohr-radius = length of solids

# Non-universally coupled scalar fields

[Damour & Donoghue 2010]  
[Stadnik & Flambaum 2014,2015]

$$S = \frac{1}{c} \int d^4x \frac{\sqrt{-g}}{2\kappa} [R - 2g^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi - V(\varphi)] \\ + \frac{1}{c} \int d^4x \sqrt{-g} [\mathcal{L}_{\text{SM}}(g_{\mu\nu}, \Psi) + \mathcal{L}_{\text{int}}(g_{\mu\nu}, \varphi, \Psi)]$$

$$\mathcal{L}_{\text{int}} = \frac{\varphi^i}{i} \left[ \frac{d_e^{(i)}}{4\mu_0} F^2 - \frac{d_g^{(i)} \beta_g}{2g_3} (F^A)^2 \right. \\ \left. - c^2 \sum_{w=e,u,d} (d_{m_w}^{(i)} + \gamma_{m_w} d_g^{(i)}) m_w \bar{\psi}_i \psi_i \right]$$

- $i = 1, 2$  for linear or quadratic coupling
- With five dimensionless coupling constants  $d_x^{(i)}$

# Variation of constants

$$\mathcal{L}_{\text{eff}}^{\text{EM}} = \underbrace{-\frac{e^2 c}{16\pi\hbar\alpha} F^2}_{\text{Electromagnetism from Standard Model}} + \underbrace{+d_e\varphi \frac{e^2 c}{16\pi\hbar\alpha} F^2}_{\text{Electromagnetism from scalar field}} \simeq \frac{-e^2 c}{16\pi\hbar\alpha(1+d_e\varphi)} F^2$$

$$\alpha_{EM}(\varphi) = \alpha_{EM} \left(1 + d_e^{(i)} \frac{\varphi^i}{i}\right)$$

$$m_w(\varphi) = m_w \left(1 + d_{m_w}^{(i)} \frac{\varphi^i}{i}\right)$$

$$\Lambda_3(\varphi) = \Lambda_3 \left(1 + d_g^{(i)} \frac{\varphi^i}{i}\right)$$

$i = 1, 2$

- Fundamental constants ( $\alpha$ ,  $\Lambda_3$ ,  $m_i$ ) are functions of  $\varphi$ , and vary if  $\varphi$  varies.
- Different atomic transitions depend differently on fundamental constants and thus their relative frequency varies with  $\varphi$ .
- The length of solids (e.g. optical cavities) is proportional to the Bohr radius ( $\propto 1/(m_e\alpha)$ ) and thus varies with  $\varphi$ .
- Light speed is unchanged (in geometric optics approximation)

[Damour & Donoghue 2010]

[Stadnik & Flambaum 2014,2015]

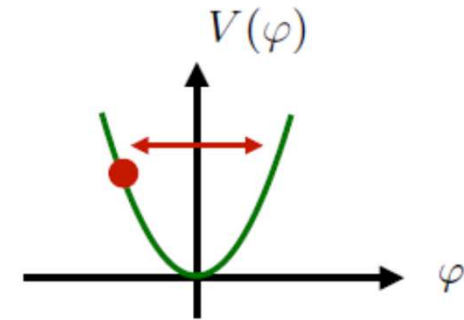


# Evolution of the galactic scalar field (2)

$$V(\varphi) = 2\frac{c^2}{\hbar^2}m_\varphi^2\varphi^2$$

- Assume a quadratic potential for  $\varphi$ .
- Varying Lagrangian with respect to  $\varphi$  gives a KG equation:

$$\frac{1}{c^2}\ddot{\varphi}(t, \mathbf{x}) - \Delta\varphi(t, \mathbf{x}) = -\frac{4\pi G}{c^2}f(d_j^{(i)})\rho_A(\mathbf{x})\varphi(t, \mathbf{x})^{i-1} - \frac{c^2 m_\varphi^2}{\hbar^2}\varphi(t, \mathbf{x})$$



$$\varphi^{(1)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) - s_A^{(1)} \frac{GM_A}{c^2 r} e^{-r/\lambda_\varphi}$$

$$\varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - s_A^{(2)} \frac{GM_A}{c^2 r} \right]$$

- The solutions for a spherically symmetric mass distribution oscillate at  $\omega = m_\varphi c^2 / \hbar$
- The Yukawa term has range  $\lambda_\varphi = \hbar / (m_\varphi c)$
- $s_A$  are functions of  $d_j$  and the central body ( $GM_A/R_A$ )
- Linear ( $i=1$ ) solution is well known
- Quadratic ( $i=2$ ) solution is less common and has interesting phenomenology

[Hees, Minazzoli, Savalle, Stadnik, Wolf, PRD **98**, 064051, 2018]

# Link to Dark Matter

$$\rho_{\bar{\varphi}} = \frac{c^2}{4\pi G} \frac{\omega^2 \varphi_0^2}{2} = \frac{c^6}{4\pi G \hbar^2} \frac{m_\varphi^2 \varphi_0^2}{2}$$

- The cosmological density (+) and pressure (-) of  $\varphi$  are given by  $\frac{c^2}{8\pi G} \left( \dot{\varphi}^2 \pm \frac{V(\varphi)c^2}{2} \right)$ .
- The oscillating part of  $\varphi(t)$  has zero average pressure and is therefore a candidate for Dark Matter.
- Equating its average density at spatial infinity with the DM density ( $\approx 0.4 \text{ GeV/cm}^3$ ) fixes the amplitude  $\varphi_0$ .
- The oscillation translates into an oscillation of the fundamental constants that can be searched for in a 6 parameter space ( $m_\varphi, d_x$ ).
- The mass  $m_\varphi$  is given by the frequency of oscillation, the coupling constants  $d_x$  by the amplitude.

[Stadnik & Flambaum 2014, 2015]

[Arvinalaki, Huang, Van Tilburg 2015]

# Evolution of the galactic scalar field (2)

Coherence time:

$$\hbar\omega = mc^2 + \frac{mv^2}{2} \Rightarrow \frac{\delta\omega}{\omega} \approx \frac{v\delta v}{c^2} \approx 10^{-6}$$

for  $\delta v \approx v \approx 10^{-3} c$  in the virialized galaxy

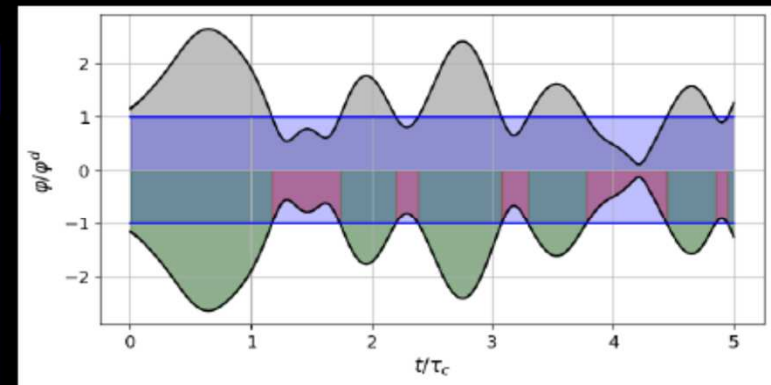
$$\delta\omega \tau_{coh} = 2\pi$$

- In our Cs/Rb experiment [Hees et al. 2016] ( $f < 5.7 \times 10^{-4}$  Hz) this gives  $\tau_{coh} > 55$  years.
  - In the DAMNED experiment [Savalle et al. 2021] ( $f = [10:200]$  kHz) this gives  $\tau_{coh} = [5:100]$  s.
- The velocity distribution is stochastic and that needs to be taken into account either by decreased sensitivity [Centers et al. arXiv:1905.13650] or by modelling the full stochastic evolution.

## Stochastic scalar field

$$\varphi = \varphi_0 \sum_{j=1}^{N_j} \alpha_j \sqrt{f_{DM}(\omega_{\varphi_j}) \Delta\omega} \cos(\omega_{\varphi_j} t + \delta_j)$$

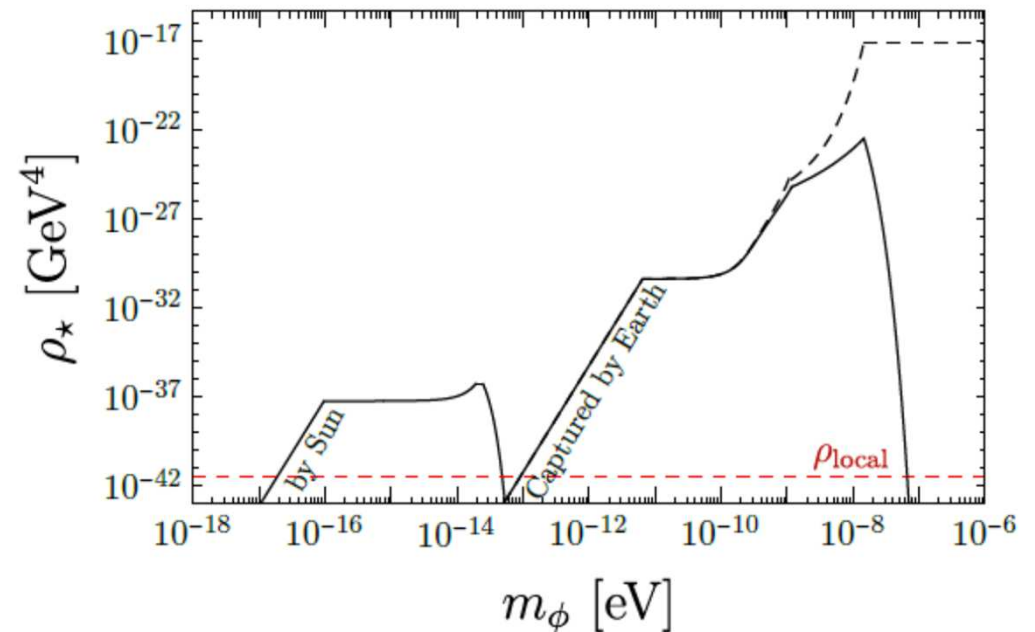
J. W. Foster et al. - PRD (2018)



SYRTE

# Scalar field transient “clumps” (2)

- Other self potentials than quadratic are possible.
- The scalar field may form objects (boson stars) or halos around standard matter objects (e.g. Earth, Sun), or topological defects (e.g. domain walls)
- The resulting field may still oscillate at its Compton frequency ( $\omega = m_\phi c^2 / \hbar$ ).
- This could lead to an overdensity around massive objects like the Earth, or to transient local variations of the scalar field.
- It may also modify the coherence properties of the field (e.g. much longer coherence time)



[Derevianko, A. & Pospelov, M., Nature Physics, **10**, 933, 2014]

[Banerjee, A.; Budker, D.; Eby, J.; Kim, H. & Perez, G., Communications Physics **3**, 1, 2020]

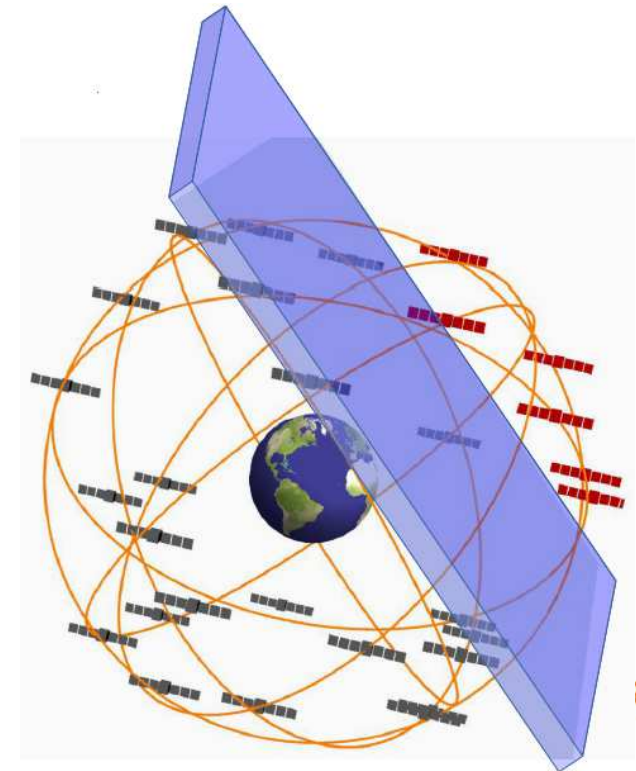
# Dark activities at SYRTE

## Theory:

- Extensive study/review of equivalence principle violating scalar DM, scalar coupling, atomic transitions/free fall tests [Hees 2018]
- Study of interactions with atomic spins: scalar/fermion/vector boson DM, with axial/tensor coupling, contact interaction/mediator. Effect in atomic clocks and co-magnetometers [Alonso 2019, Wolf 2019].

## Experiments:

- Rb/Cs dual cold atom clock, long term comparison [Hees 2016]
- The DAMNED experiment [Savalle 2021]... see Etienne's talk
- Europe-wide comparison of optical clocks to search for transients [Roberts 2020]
- The GASTON project (GALileo Survey of Transient Objects Network), searching for transients using the clocks on board the Galileo satellite constellation [ESA contract, ongoing].





# Atomic Spectroscopy

- Different atomic transition frequencies depend differently on fundamental constants.
- Comparison of two atomic transition frequencies ( $Y=X_A/X_B$ ) is a direct measure of the scalar field. Can be used to search for the space-time variation of  $\varphi(t, \mathbf{x})$ .

$$\frac{Y(t, \mathbf{x})}{Y_0} = K + \left( \kappa_{X_A}^{(i)} - \kappa_{X_B}^{(i)} \right) \varphi^i(t, \mathbf{x})$$

The sensitivity coefficients  $\kappa_X^{(i)}$  involve the coupling constants  $d_j^{(i)}$  and are obtained from atomic and nuclear structure calculations (Flambaum and co-workers [2006, 2008, 2009]).

$$\varphi^{(1)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) - s_A^{(1)} \frac{GM_A}{c^2 r} e^{-r/\lambda_\varphi}$$

$$\varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - s_A^{(2)} \frac{GM_A}{c^2 r} \right]$$

Can search for both, oscillations and spatial dependence in the field of body A (e.g. Earth)

# Tests of the Universality of Free Fall

- Two bodies of different composition will couple differently to  $\varphi(t, \mathbf{x})$ .
- They will experience a differential acceleration as a function of  $\varphi(t, \mathbf{x})$ :

$$[\Delta a]_{X-Y} = - \left( \alpha_X^{(i)} - \alpha_Y^{(i)} \right) \varphi^{i-1} [c^2 \nabla \varphi + v \dot{\varphi}]$$

The sensitivity coefficients  $\alpha_X^{(i)}$  are composition dependent and involve the coupling constants  $d_j^{(i)}$ . They are derived in [Damour & Donaghue 2010].



$$\varphi^{(1)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) - s_A^{(1)} \frac{GM_A}{c^2 r} e^{-r/\lambda_\varphi}$$

$$\varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - s_A^{(2)} \frac{GM_A}{c^2 r} \right]$$

Can search for both, oscillations and spatial dependence in the field of body A (e.g. Earth)

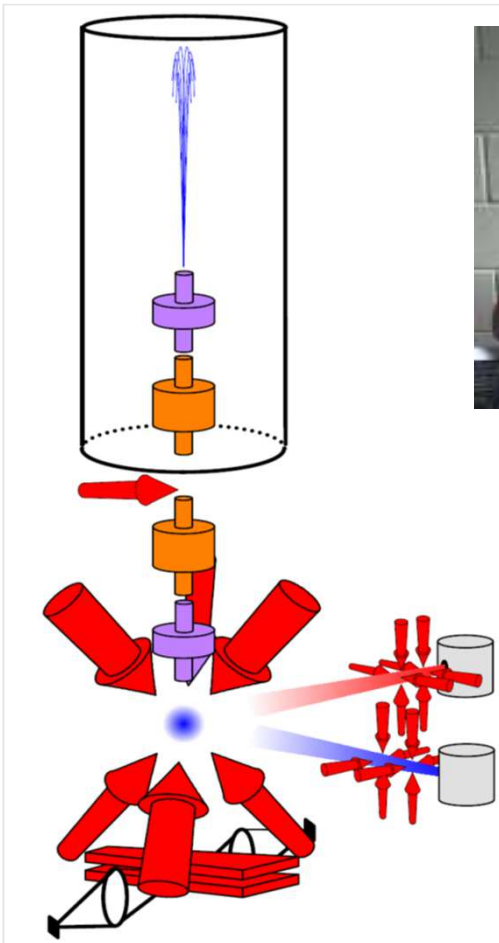


# Summary so far

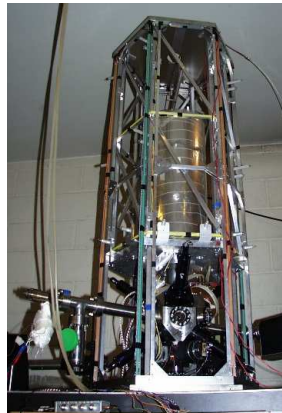
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- If light ( $m_\phi < 10$  eV) a massive scalar field will behave classically and oscillate at frequency  $f = m_\phi c^2 / h$
- It could be coupled to SM fields (standard matter) in which case it will lead to a violation of the equivalence principle. This can be searched for by:
  - atomic spectroscopy
  - tests of the universality of free fall
- In both cases the phenomenology includes oscillations related to DM and spatial dependence due to the presence of e.g. the Earth.

# The SYRTE dual Rb-Cs fountain FO2



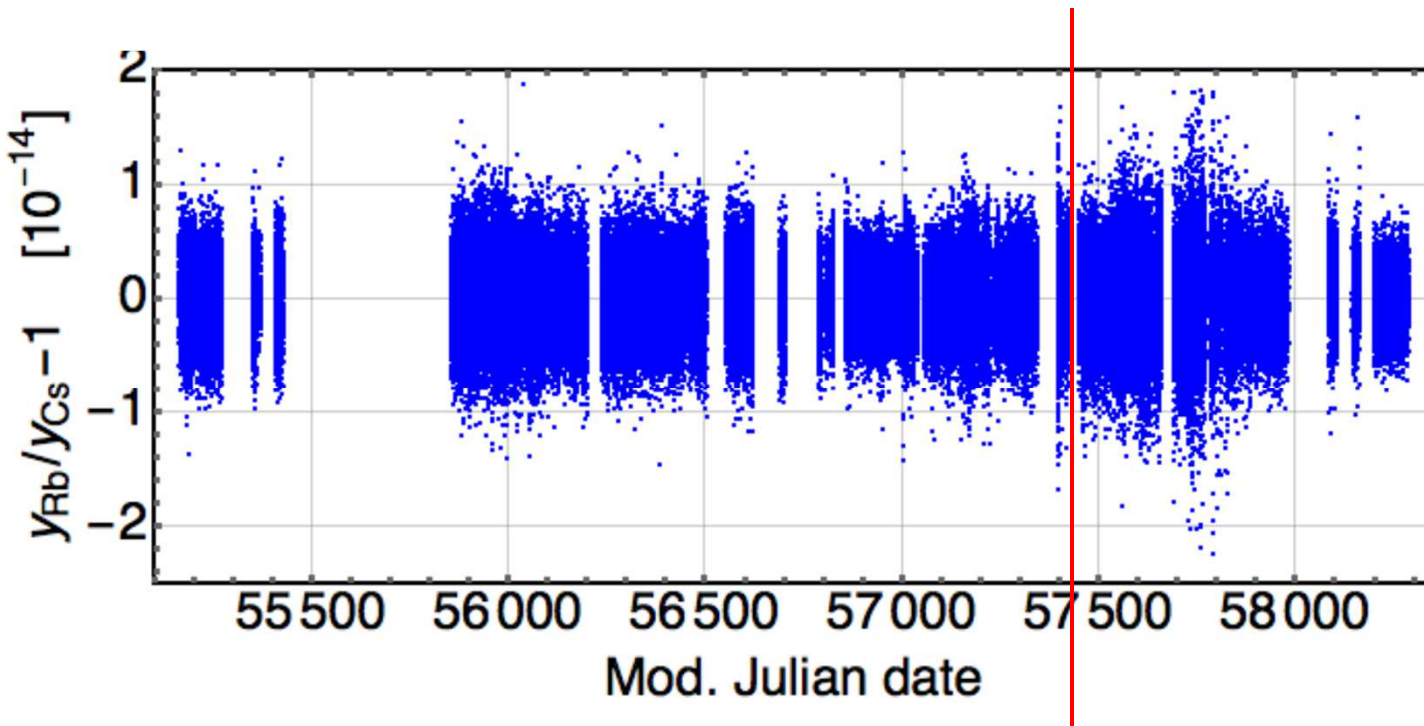
André Clairon  
1947 - 2015



- Built in early 2000s by André Clairon and co-workers.
- Operates simultaneously on laser cooled ( $\mu\text{K}$ )  $^{87}\text{Rb}$  and  $^{133}\text{Cs}$  since 2008 (common mode systematics).
- Most accurate and stable Rb/Cs frequency ratio measurement world-wide (and longest duration).
- Contributes continuously to TAI with both Rb and Cs
- Previously used to constrain linear drifts of fundamental constants, and variations proportional to  $U/c^2$  i.e. annual variations [Guéna, PRL 2012]+updates.
- All systematics are evaluated and corrected during operation.

[Guéna et al. 2010, 2012, 2014]

# FO2 Rb/Cs raw data

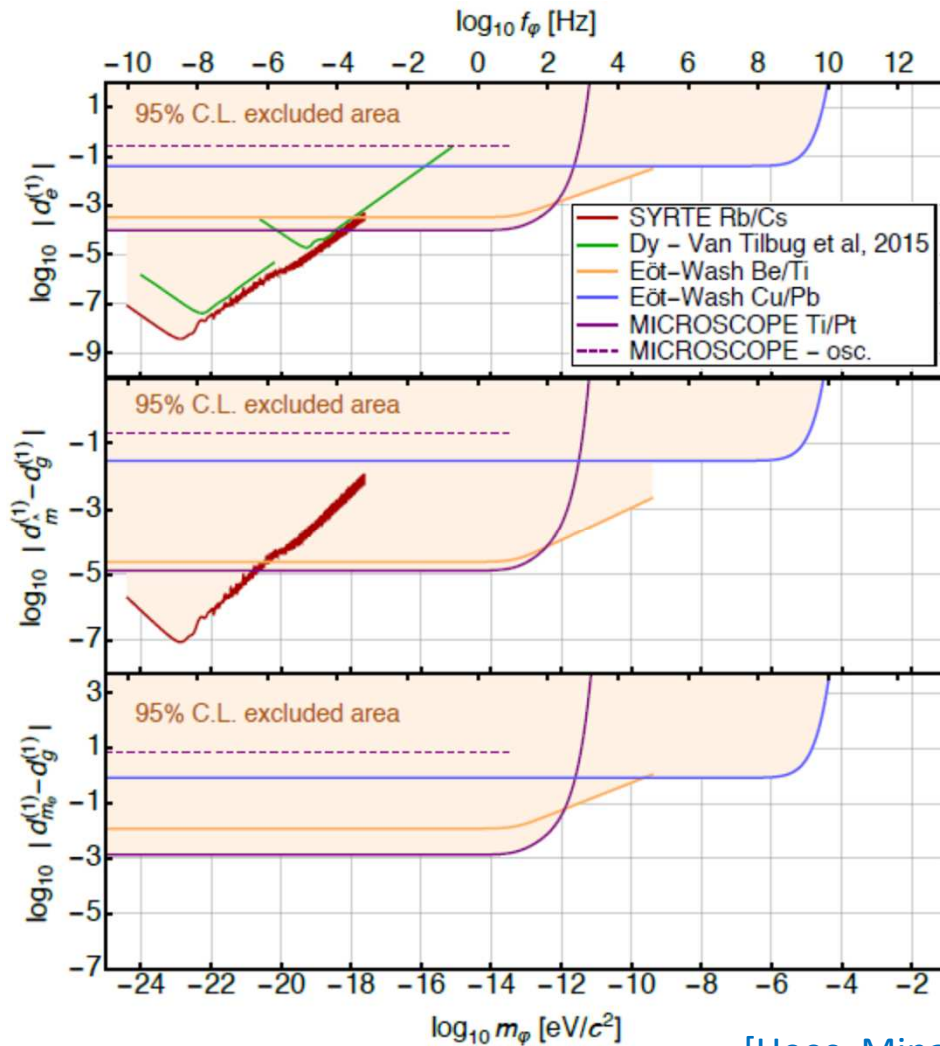


- Nov 2009 – May 2018
- Averaged to 100 points/day
- 144000 points in total
- $\approx 45\%$  duty cycle with gaps due to maintenance and investigation of systematics
- Standard deviation =  $3 \times 10^{-15}$

$$y(t) = \frac{f(t)}{f_0}$$

Update of [Hees, Guéna, Abgrall, Bize, Wolf, PRL **117**, 061301, 2016]

# Constraints for linear coupling

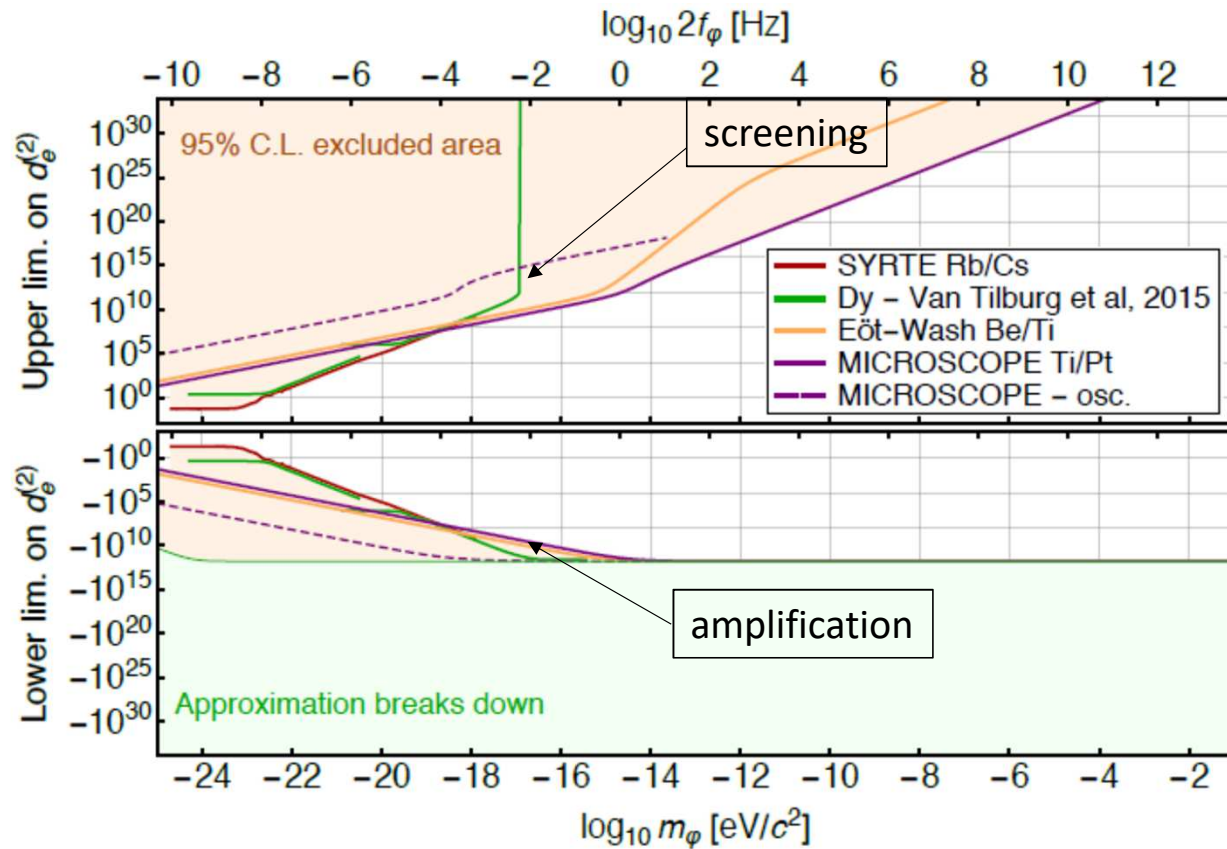


- Here we compare bounds assuming that “all other coefficients = 0”.
- UFF tests are more sensitive at higher masses, spectroscopy at lower masses.
- UFF are limited by Yukawa range for higher masses.
- Could also search for harmonic signal in UFF (limited by sampling rate).
- Generally, one could imagine varying distance (satellite tests) to better explore the spatial dependence.

$$\varphi^{(1)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) - s_A^{(1)} \frac{GM_A}{c^2 r} e^{-r/\lambda_\varphi}$$

[Hees, Minazzoli, Savalle, Stadnik, Wolf, PRD **98**, 064051, 2018]

# Constraints for quadratic coupling



- Only  $d_e$  here. Graphs for other coefficients look similar.
- Constraints are much less stringent. They are compatible with “natural” values (whatever that means...).
- Either “screening” or “amplification” by the central mass can occur.

$$\varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - s_A^{(2)} \frac{GM_A}{c^2 r} \right]$$

[Hees, Minazzoli, Savalle, Stadnik, Wolf, PRD **98**, 064051, 2018]

# DARk Matter from Non Equal Delays (DAMNED)

- Presently running and being optimized at SYRTE – Paris Observatory
- Based on ultra-stable optical cavity
- Aiming at high frequency (10-100 kHz i.e. DM mass around  $10^{-10}$  eV)
- Shot noise limited just above the cavity noise.

$$\Delta\phi(t) = \omega_0 T_0 + 2 \frac{\omega_0}{\omega_m} \left( \frac{\delta T}{T_0} + \frac{\delta\omega}{\omega_0} \right) \sin\left(\frac{\omega_m T_0}{2}\right) \sin(\omega_m t + \Phi)$$

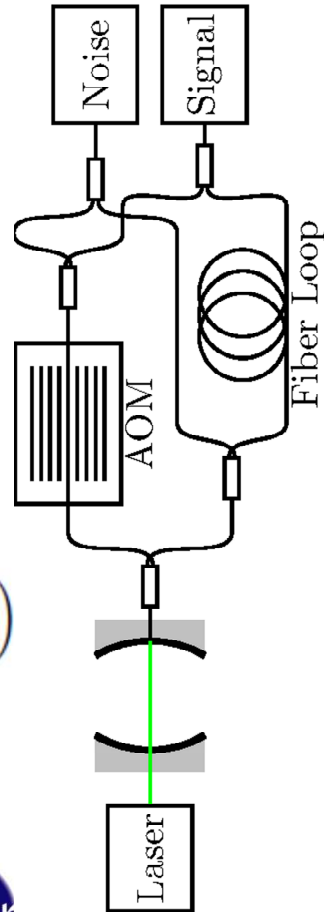
$$\left( \frac{\delta T}{T_0} + \frac{\delta\omega}{\omega_0} \right) \simeq \underbrace{\frac{\omega_0}{n_0} \frac{\partial n}{\partial \omega}}_{\approx 10^{-2}} \left( d_{m_e}^{(1)} - d_e^{(1)} - \frac{1}{2} \left( d_{m_g}^{(1)} - d_g^{(1)} \right) + 0.024 \left( d_{m_q}^{(1)} - d_g^{(1)} \right) \right) \varphi_0 + \mathcal{O}\left(10^{-4} \varphi_0 d_i^{(1)}\right)$$

Fibre delay

Cavity frequency

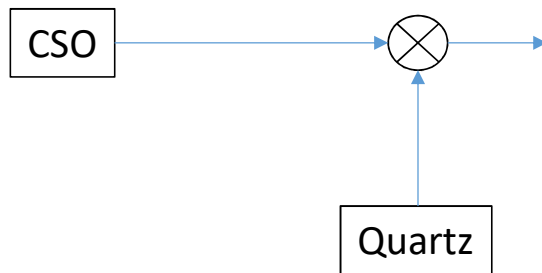
[Braxmaier et al., PRD **64**, 042001, 2001]

[Pustaka et al., arXiv:1809.02863, 2018]



# Quartz vs Cryogenic-Cavity

- Presently being set up at UWA.
- Based on high performance quartz crystal and cryogenic sapphire resonator.
- Aiming at high frequency (10-100 kHz and above i.e. DM mass  $\geq 10^{-10}$  eV).



$$\propto \left( \frac{\delta\alpha}{\alpha} + \frac{1}{2} \frac{\delta(m_e/\Lambda_3)}{m_e/\Lambda_3} - 0.024 \frac{\delta(m_q/\Lambda_3)}{m_q/\Lambda_3} \right) \sin(\omega_m t + \Phi)$$

$$\propto \left( d_e^{(1)} + \frac{1}{2} (d_{m_e}^{(1)} - d_g^{(1)}) - 0.024 (d_{m_q}^{(1)} - d_g^{(1)}) \right) \varphi_0 \sin(\omega_m t + \Phi)$$

# Conclusion and Outlook

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## Conclusion:

- Ultralight ( $10^{-23} - 10^4$  eV) dark matter is an active field, both theoretically and experimentally
- Could be detected in high precision atomic devices (clocks, magnetometers, ...)
- More generally, if DM interacts with SM fields you might have effects in many high precision experiments (e.g. equivalence principle tests, time/frequency metrology, ...).

## Outlook:

- New experiments are being designed targeting specific regions of parameter space
- Theoretical work develops new models, and helps identifying potential effects on high precision experiments
- This seems just the beginning...



**Thank you for your attention!**

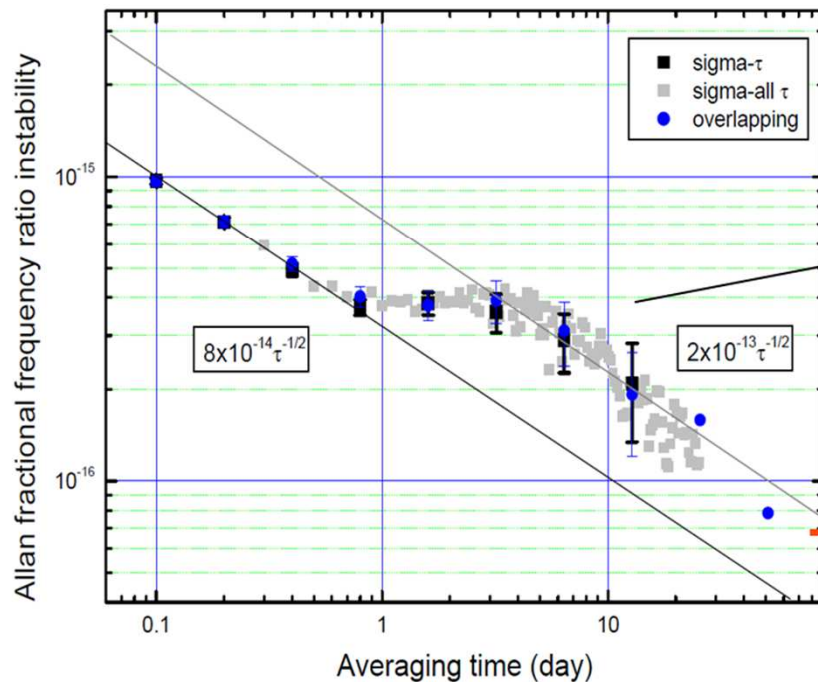
# Backup Slides

# Noise model

## FO2-Rb/Cs comparison over 6 months

Allan standard deviation of the Rb/Cs frequency ratio

effective duration 130 days



Bump well understood: correction of collision shift by HD/LD measurements interleaved introduce another timescale at 5 days

Resolution below  $10^{-16}$

- Noise level is a function of Fourier frequency:

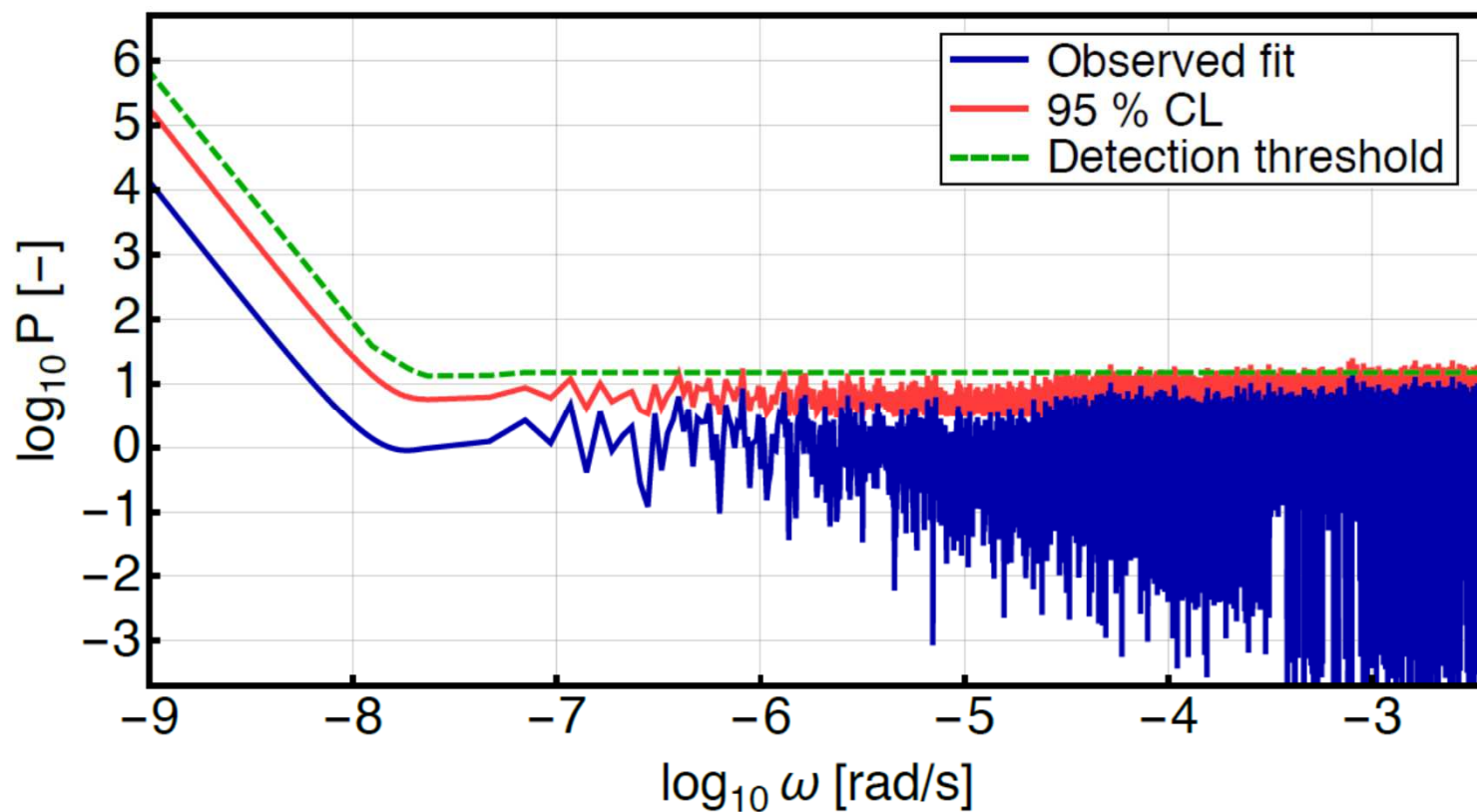
$$\sigma_o^2(\omega) = 4.6 \times 10^{-29}, \quad \text{for } \omega \leq 9.0 \times 10^{-6} \text{ rad/s}$$

$$\sigma_o^2(\omega) = 9.3 \times 10^{-30}, \quad \text{for } \omega \geq 4.5 \times 10^{-5} \text{ rad/s}$$

$$\sigma_o^2(\omega) = 4.2 \times 10^{-34} / \omega, \quad \text{otherwise,}$$

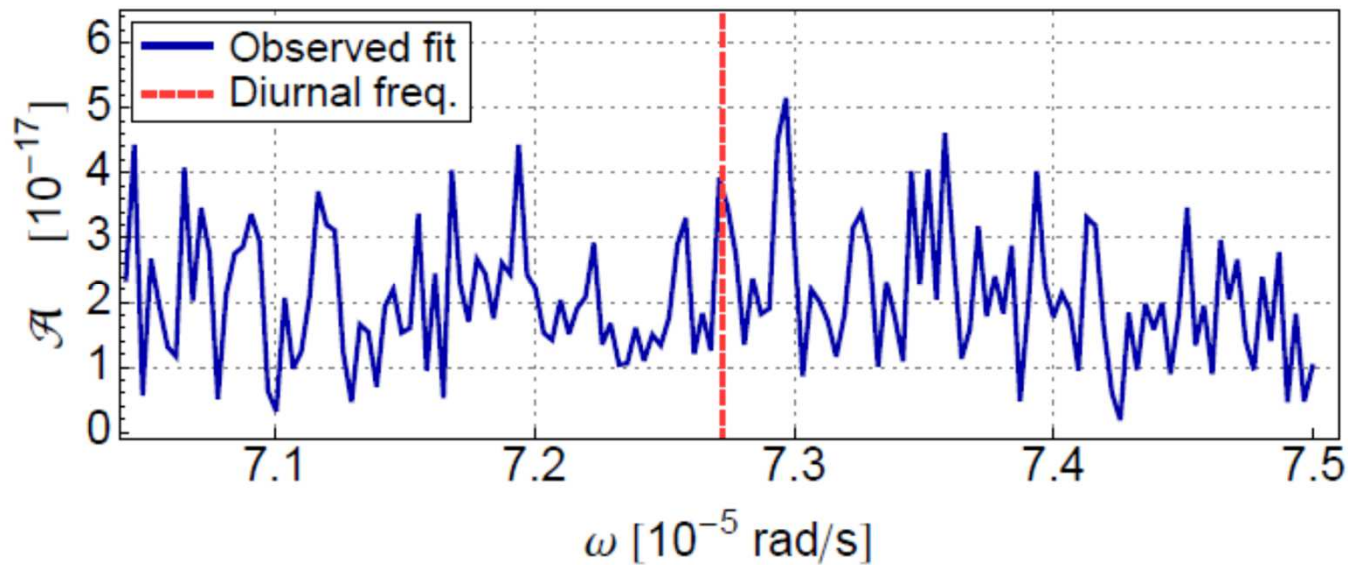
See Guéna et al., *Metrologia*, **51**, 108, (2014) for details

# Normalized power



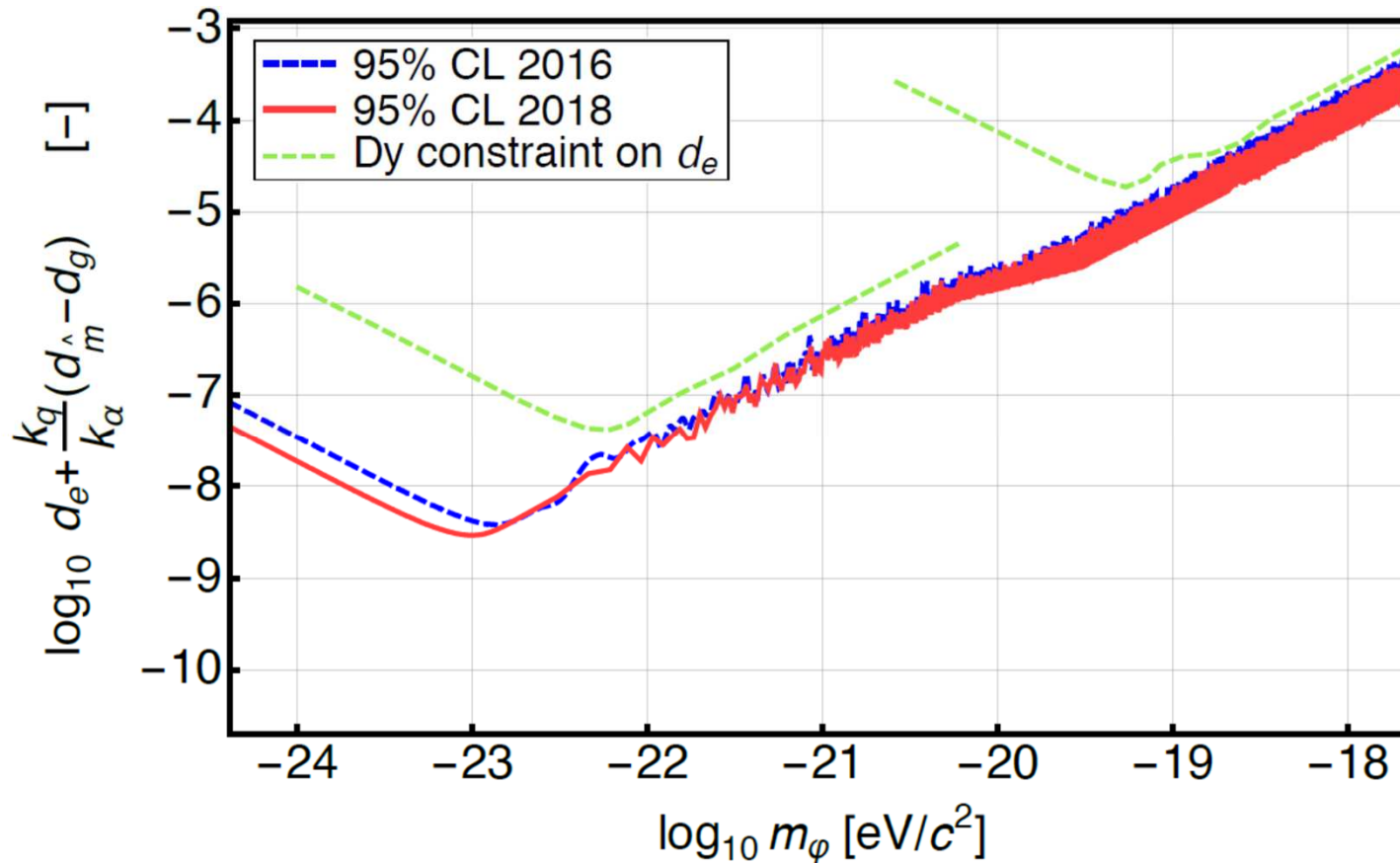
- Fit  $A + C_{\omega} \cos(\omega t) + S_{\omega} \sin(\omega t)$  to data for each independent  $\omega$ .
- Search for a peak in normalized power  $P_{\omega} = \frac{N}{4\sigma_0^2(\omega)} (C_{\omega}^2 + S_{\omega}^2)$ .
- Use different methods (LSQ + MC, Bayesian MCMC) to determine confidence limits.

# Systematic Effects



- Detailed and repeated analysis of systematic effects (Guéna 2012, 2014) estimates uncertainty on absolute determination of Rb and Cs hyperfine frequency to  $3.2 \times 10^{-16}$  and  $2.1 \times 10^{-16}$ .
  - The uncertainty on the difference is expected to be significantly less due to common mode.
  - Periodic variations at any frequency are again expected to be below that level.
  - No evidence for systematic effect at most likely frequency (diurnal).
- ⇒ Our results are limited by statistics rather than systematic uncertainties.

# Constraints for linear coupling



- Rb/Cs comparison is sensitive to the combination  $d_e + 0.043(d_{\hat{m}} - d_g)$ .
- Additional data has (40% increase in duration) has only small effect, mainly at low mass.

# Limits on mass range

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A lower limit on plausible DM masses is obtained by requiring that  $\lambda = h/mv <$  smallest dwarf galaxy ( $\approx 1$  kpc  $\approx 3 \times 10^{19}$  m). With  $v \approx 10^{-3} c$  this gives a minimum mass of about  $10^{-23}$  eV.

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- Our upper limit is due to our data being averaged to 100 points/day, imposing a Nyquist limit at  $5.8 \times 10^{-4}$  Hz corresponding to  $m \approx 2.4 \times 10^{-18}$  eV.
- But our basic measurement cycle time is 2 s, so we will analyze some high frequency data to extend our search up to  $10^{-15}$  eV.
- It is possible to search at even higher masses, at the expense of sensitivity [see e.g. Kalaydzhyan & Yu, PRD 2017]. Limited when DM coherence time  $= h/mv^2$  (assuming virialized DM) becomes shorter than clock cycle (2 s). Then  $m \leq 2 \times 10^{-9}$  eV.

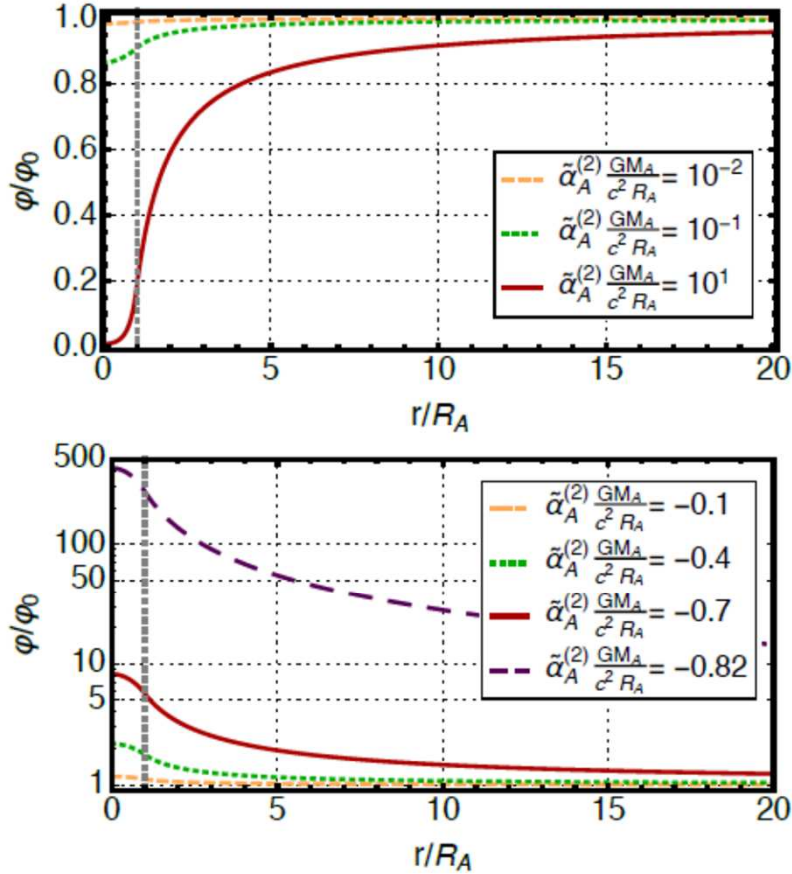


FIG. 2. Evolution of the scalar field around a homogeneous spherically symmetric body. The different curves show the impact of the values of  $\tilde{\alpha}^{(2)}$ . In particular, in the limit of large positive couplings, the scalar field tends to vanish inside the body and the scalar field diverges for negative values of  $\tilde{\alpha}^{(2)}$ .

$$\varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - s_A^{(2)} \frac{GM_A}{c^2 r} \right]$$

$$s_A^{(2)} = \tilde{\alpha}_A^{(2)} J_{\text{sign}[\tilde{\alpha}_A^{(2)}]} \left( \sqrt{3} \left| \tilde{\alpha}_A^{(2)} \right| \frac{GM_A}{c^2 R_A} \right), \quad (23)$$

which depends on the sign of  $\tilde{\alpha}_A^{(2)}$  through

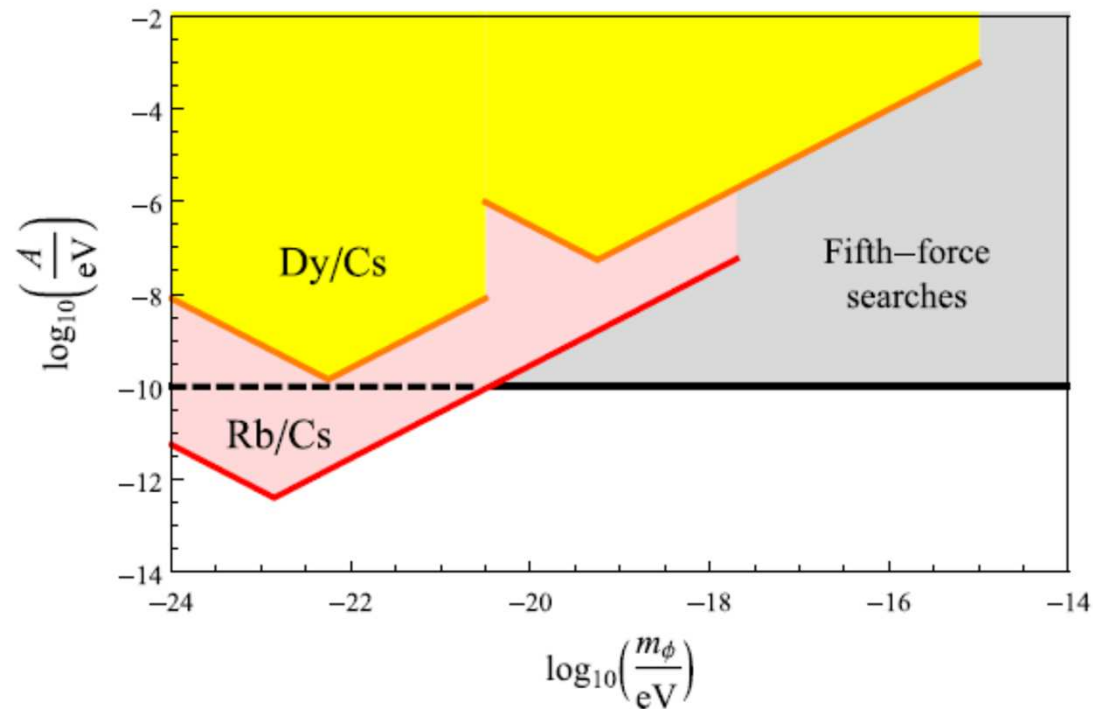
$$J_+(x) = 3 \frac{x - \tanh x}{x^3}, \quad (24a)$$

$$J_-(x) = 3 \frac{\tan x - x}{x^3}. \quad (24b)$$

$$\lim_{d_j \rightarrow +\infty} \varphi^{(2)}(t, \mathbf{x}) = \varphi_0 \cos(\omega t + \delta) \left[ 1 - \frac{R_A}{r} \right]$$



# Higgs portal



$$\mathcal{L}_{\text{int,eff}}^{\text{Higgs}} = \frac{A\langle h \rangle}{m_h^2} \phi \left( \sum_f g_{hff} \bar{f} f + \frac{g_{h\gamma\gamma}}{\langle h \rangle} F_{\mu\nu} F^{\mu\nu} \right), \quad (7)$$

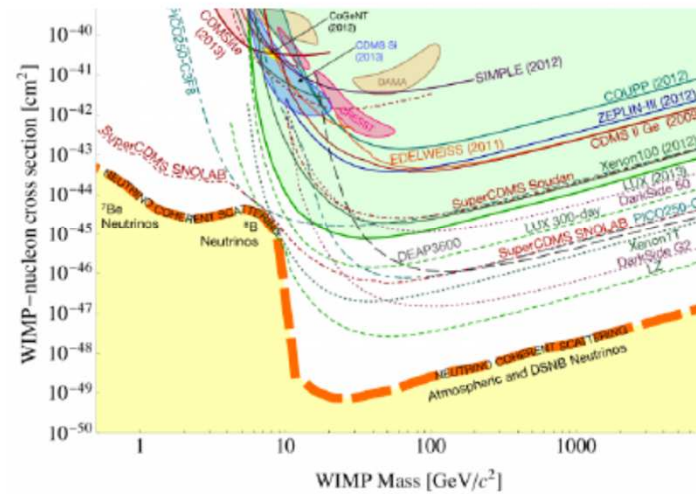
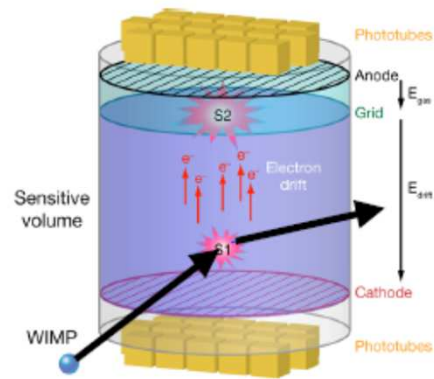
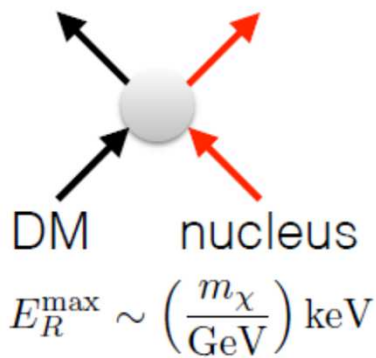
where  $m_h = 125$  GeV is the mass of the Higgs boson,  $g_{hff} = m_f / \langle h \rangle$  for couplings of the Higgs to elementary fermions (leptons and quarks),  $g_{hNN} = b m_N / \langle h \rangle$  with  $b \sim 0.2\text{--}0.5$  [24] for couplings of the Higgs to nucleons, and  $g_{h\gamma\gamma} \approx \alpha / 8\pi$  for the radiative coupling of the Higgs to the electromagnetic field

[From Stadnik & Flambaum, PRA **94**, 022111 (2016)]

# 'Traditional' DM searches

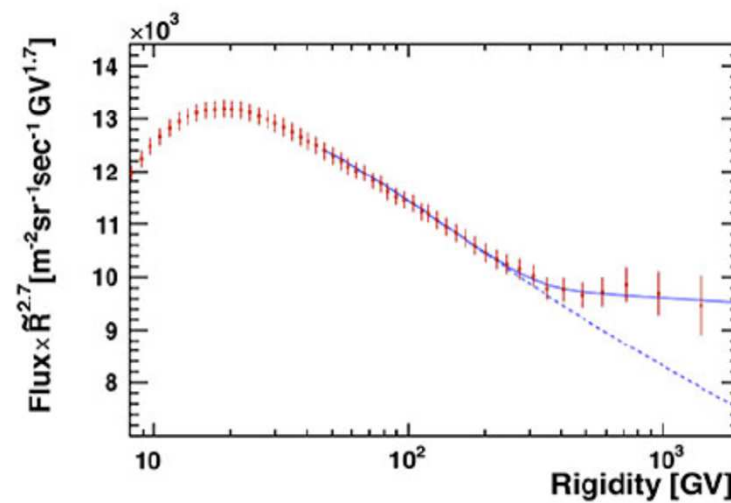
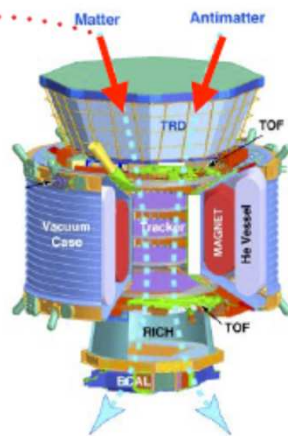
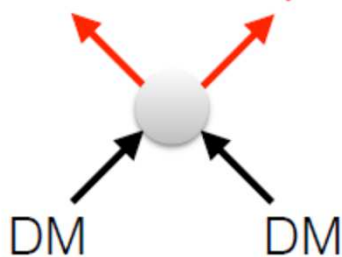
Direct: e.g. Xenon 100

scattering

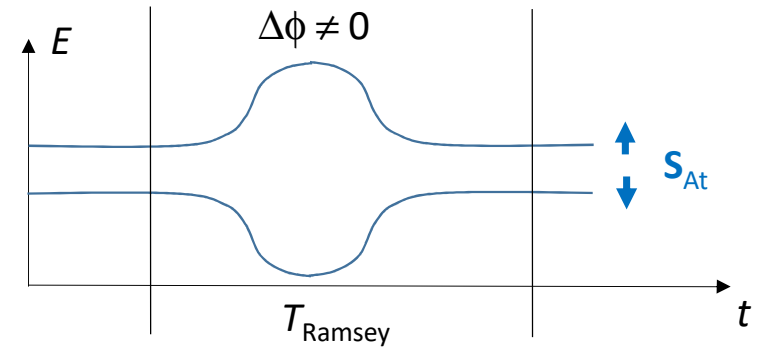
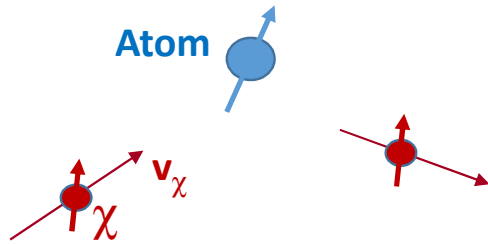


Indirect: e.g. AMS02

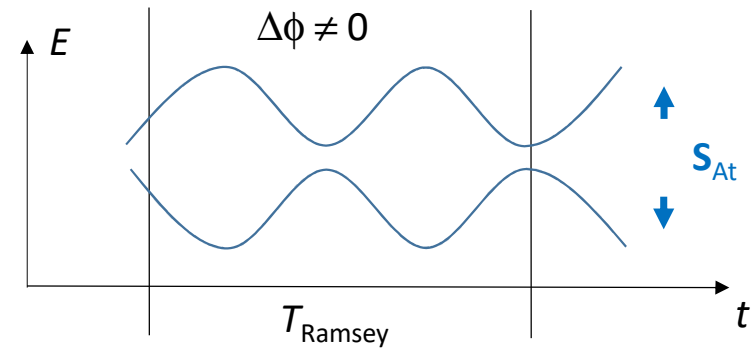
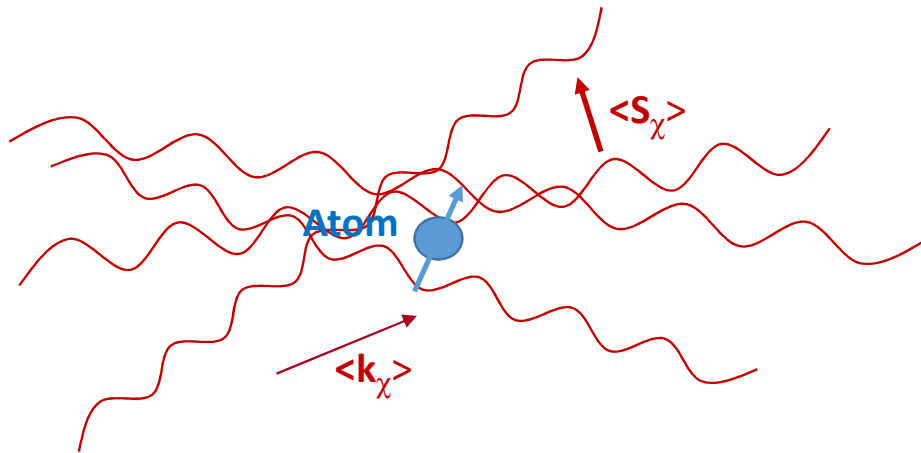
annihilation



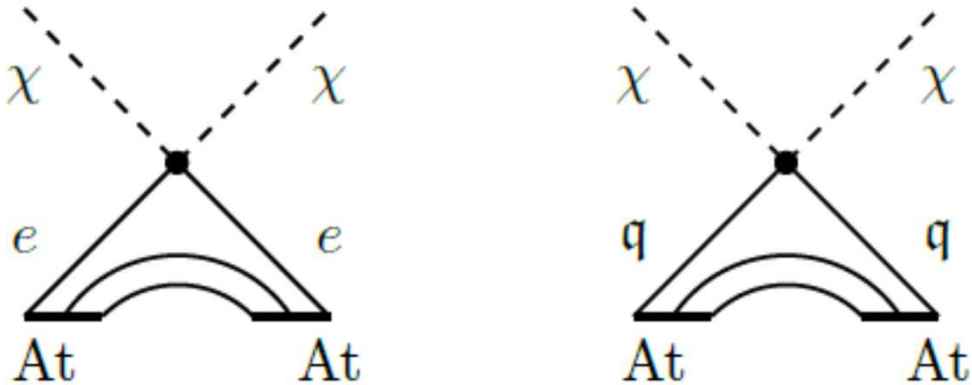
# DM interacting with SM spins



- $m_\chi \ll m_{\text{At}} \Rightarrow$  no momentum exchange
- “See” effects proportional to  $\mathbf{S}_{\text{At}} \cdot \mathbf{S}_\chi$  or  $\mathbf{S}_{\text{At}} \cdot \mathbf{v}_\chi$
- When varying  $\mathbf{S}_{\text{At}}$  (e.g. using a magnetic field) the effect is modulated



# Interaction types



- Example: EFT model with contact interaction
- Generalized to a model with a dynamical mediator.
- Also considered 3-point interactions with axial scalar (axion) or axial vector boson.

see [Alonso, Blas, Wolf, arXiv:1810.00889] for details.

$$L_{\text{int}} = - \int d^3x \left( G_e^{\mathcal{I}} \bar{e} \Gamma^{\mathcal{I}} e \mathcal{J}_\chi^{\mathcal{I}} + \sum_{q=u,d} G_q^{\mathcal{I}} \bar{q} \Gamma^{\mathcal{I}} q \mathcal{J}_\chi^{\mathcal{I}} \right) \equiv - \int d^3x \sum_{\psi} G_{\psi}^{\mathcal{I}} \mathcal{J}_{\psi}^{\mathcal{I}} \times \mathcal{J}_{\chi}^{\mathcal{I}}$$

Leads to  $\mathbf{S}_{\text{At}} \cdot \mathbf{S}_{\chi}$  or  $\mathbf{S}_{\text{At}} \cdot \mathbf{v}_{\chi}$

$\mathcal{I}$	$\psi = e, u, d$	DM	Scalar	Fermion	Vector Boson
<i>Ax. vector</i>	$\mathcal{J}_{\psi} : \bar{\psi} \gamma^{\mu} \gamma_5 \psi$	$\mathcal{J}_{\chi} :$	$i\chi^{\dagger} \partial_{\mu} \chi + \text{h.c.},$	$\bar{\chi} \gamma_{\mu} \chi,$ $\bar{\chi} \gamma_{\mu} \gamma_5 \chi,$	$i\chi_{\nu}^{\dagger} \partial_{\mu} \chi^{\nu} + \text{h.c.}$
<i>Tensor</i>	$\mathcal{J}_{\psi} : \bar{\psi} \sigma^{\mu\nu} \psi$	$\mathcal{J}_{\chi} :$	-	$\bar{\chi} \sigma^{\mu\nu} \chi,$	$\chi_{\alpha}^{\dagger} (\Sigma_{\mu\nu})^{\alpha}_{\beta} \chi^{\beta}.$

# Observables (ex. hyperfine atomic clock)

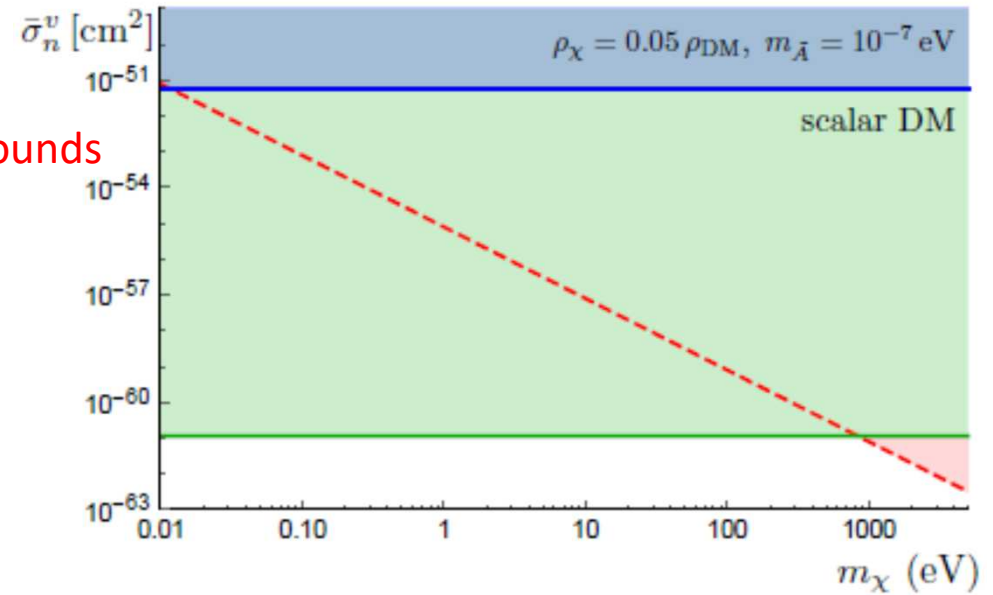
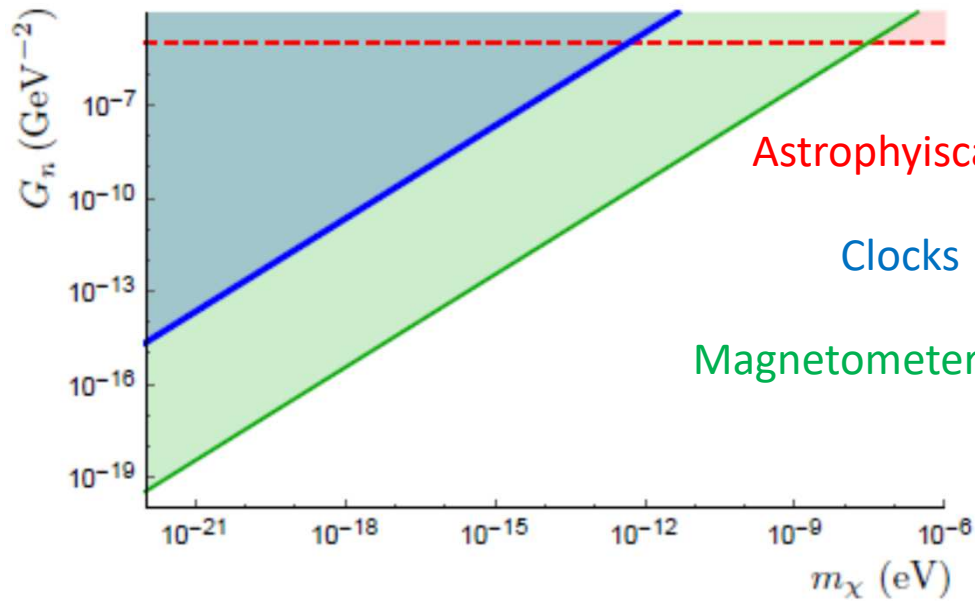
Consider hyperfine transition in Rb or Cs clocks. The effect is akin to frequency shifts due to collisions with background gases [Gibble, PRL **110**, 180802, 2013]. For a detailed derivation see [Wolf, Alonso, Blas, arXiv:1810.01632]:

$$\delta\omega \simeq \frac{2\pi\rho_\chi\hbar}{m_\chi^2} \text{Re}[f_1(0) - f_2(0)]$$

$f_i(0)$  = forward scattering amplitudes in the two clock states  $|1\rangle$  and  $|2\rangle$ :

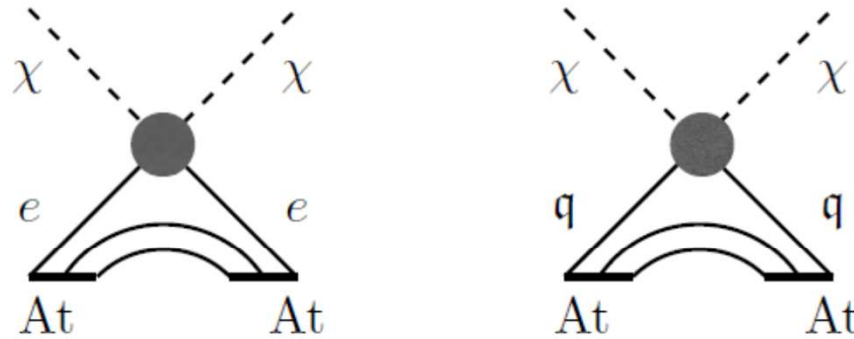
- $f_1(0) - f_2(0)$  depends **linearly** on  $G_{e/q}\mathbf{S}_{\text{At}}\cdot\mathbf{S}_\chi$  or  $G_{e/q}\mathbf{S}_{\text{At}}\cdot\mathbf{v}_\chi$
- When operating the clock on spin polarized states (using a quantization magnetic field  $\mathbf{B}$ ) the frequency shift varies as the orientation of  $\mathbf{B}$  varies.
- Additionally, may have modulations at Compton frequency of  $m_\chi$ .
- To control magnetic field fluctuations use differential measurement between different species e.g. Rb and Cs in clocks (see later) or He and Xe in magnetometers.

# Sensitivity estimate examples



- Coupling to neutron.
- Sensitivity estimates, not bounds!
- Assume  $\mu\text{Hz}$  uncertainty for Rb/Cs hyperfine clocks, sub-nHz for He/Xe magnetometers.
- Provides an indication of parameter space that can be explored.

## DM-atom scattering: effective vertex



$$|\text{Rb}_\lambda^F\rangle = \sum_{\lambda_e, \lambda_I} |e_{\lambda_e}^{5s}\rangle \otimes |\text{Ncl}_{\lambda_I}^I\rangle \langle 1/2, \lambda_e, I, \lambda_I | F, \lambda \rangle$$

$$L_{\text{int}} = - \int d^3x \left( G_e^{\mathcal{I}} \bar{e} \Gamma^{\mathcal{I}} e \mathcal{J}_\chi^{\mathcal{I}} + \sum_{q=u,d} G_q^{\mathcal{I}} \bar{q} \Gamma^{\mathcal{I}} q \mathcal{J}_\chi^{\mathcal{I}} \right)$$

$\downarrow$  DM current ← ←

$\langle N | \bar{q} \Gamma^{\mathcal{I}} q | N \rangle$  (known)

All possible interactions  $\vec{S}_e \cdot \vec{v}_\chi, \vec{S}_e \cdot \vec{S}_\chi, \vec{S}_N \cdot \vec{S}_\chi, \dots$

## Making the calculation

$$\langle \mathbf{P}', \mathbf{p}' | H_{\text{int}} | \mathbf{P}, \mathbf{p} \rangle = (2\pi)^3 \delta^{(3)}(\mathbf{P}' - \mathbf{P}) \mathcal{T}(\mathbf{p}', \mathbf{P}', \mathbf{p}, \mathbf{P})$$

$$f(\mathbf{p}', \mathbf{p}) = -\frac{\mu}{2\pi} \mathcal{T}(\mathbf{p}', \mathbf{p})$$



Single DM particle-atom interaction

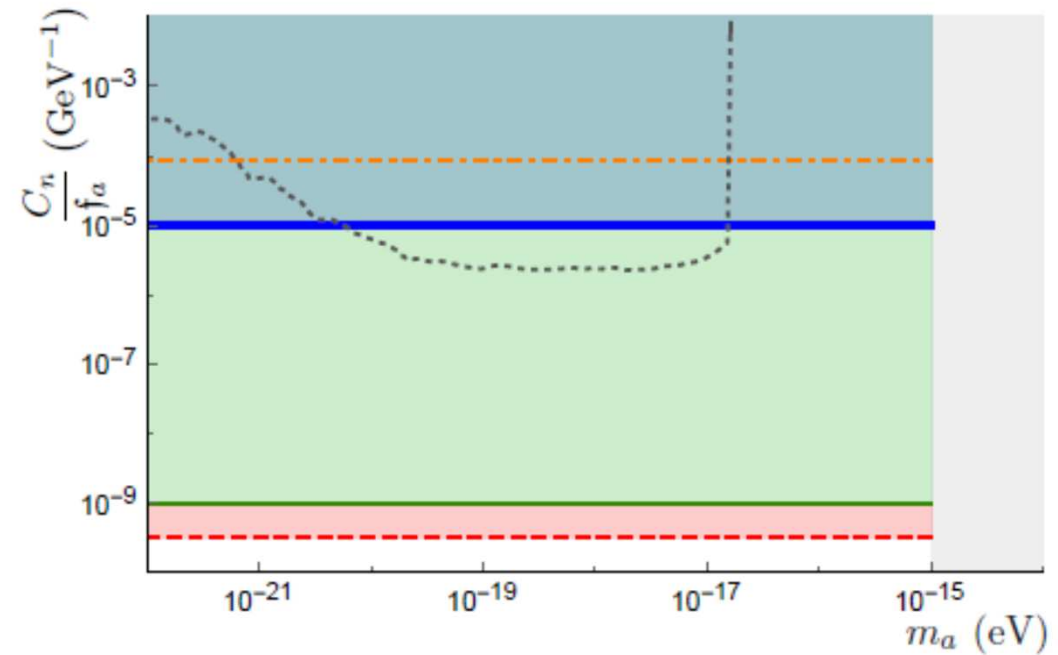
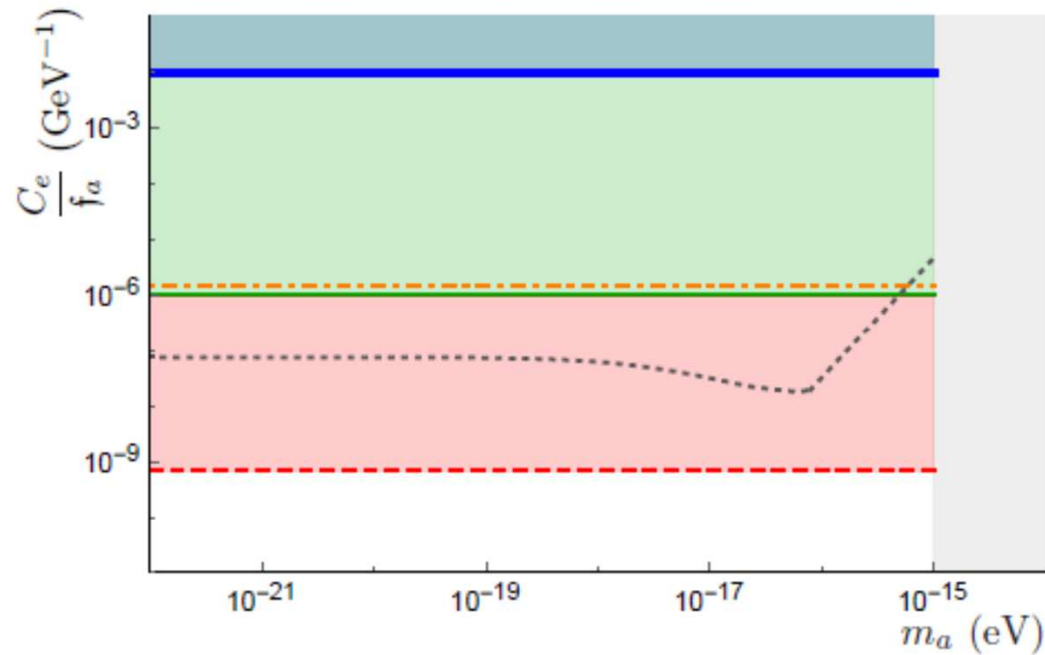
$$f_1(0) - f_2(0) = \frac{m_\chi}{\pi} \left( G_N \mathbf{g}_{\text{Ncl}}^N - G_e \right) \vec{J}_\chi \cdot \frac{\vec{\lambda}}{F}$$

atomic form factors       $\vec{v}_\chi$        $\vec{S}_\chi$



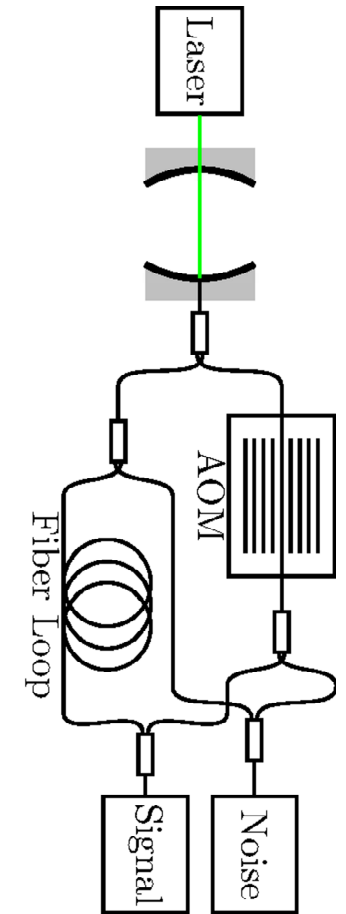
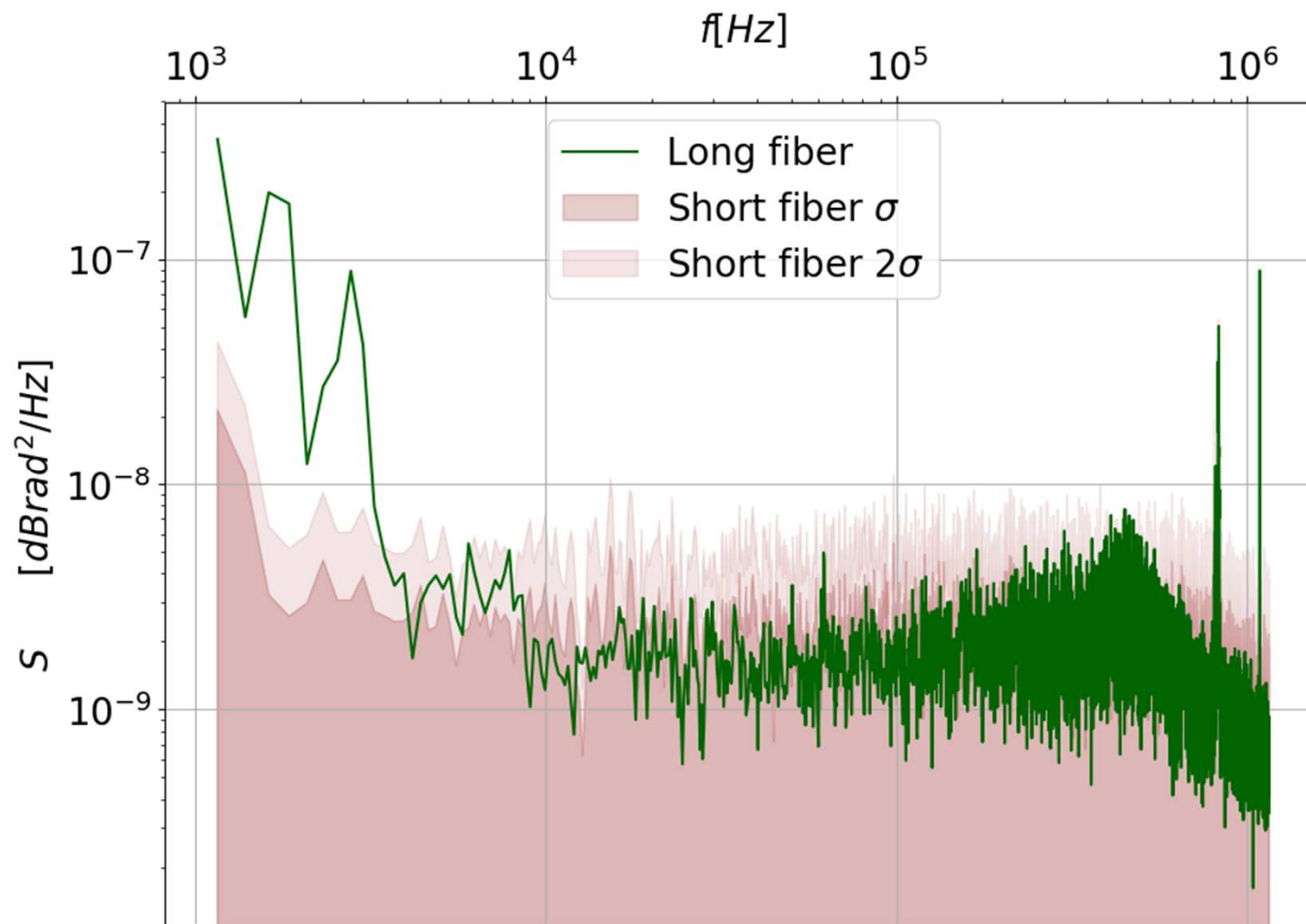
## Axion field coupling to electron or nucleon

$$H_a = -\frac{C_\psi \sqrt{2\rho_\chi}}{f_a} \vec{\lambda}_\psi \cdot \vec{v} \cos(m_a t + \phi_0)$$

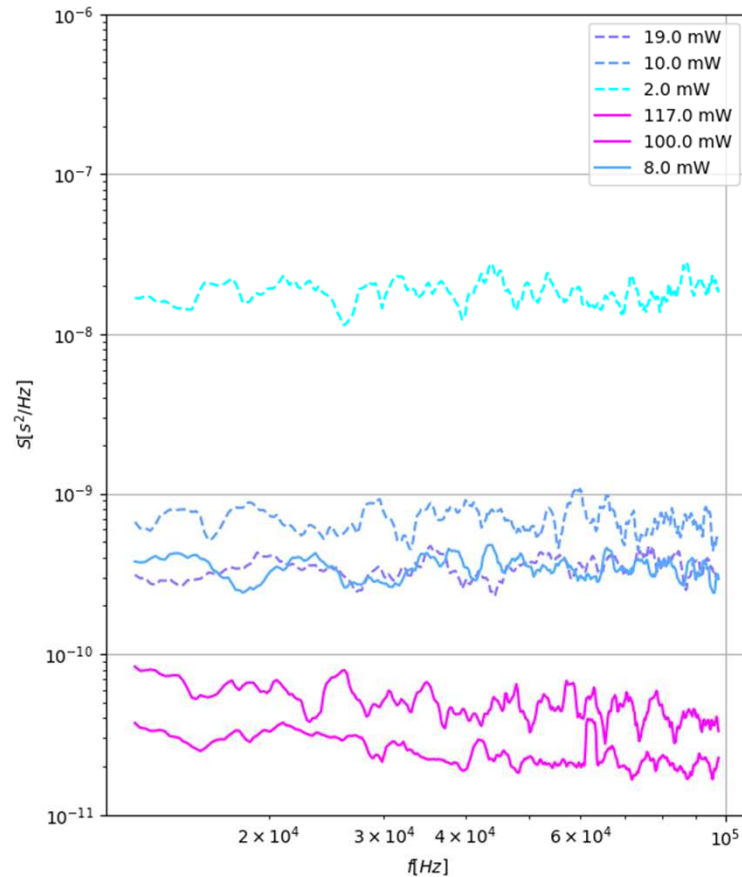


- Much lower mass region than many other axion experiments (e.g. ADMX)
- Not quite able to reach astrophysical (stellar cooling) bounds
- Price to pay is that QCD axion is much lower ( $C_n/f_a \approx 10^{-24}$  @  $10^{-15}$  eV)

# DARK Matter from Non Equal Delays (DAMNED)



# DARk Matter from Non Equal Delays (DAMNED)



Short fibre noise vs. Power on diode

