

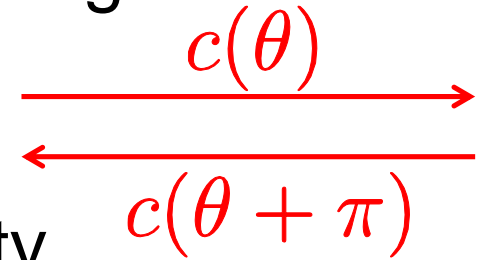
# Higher Order Test of Lorentz Invariance with an Optical Ring Cavity

Yuta Michimura

Department of Physics, University of Tokyo

# Summary

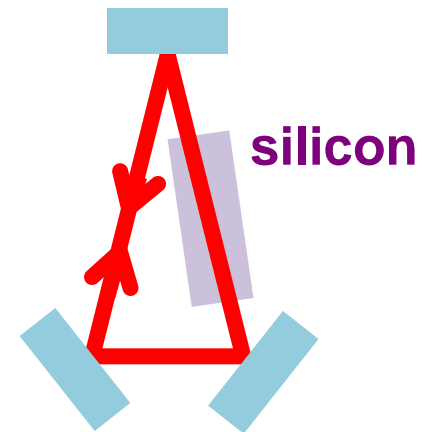
- compared the speed of light propagating in opposite directions



- using a double-pass optical ring cavity

- put **new limits** on higher order Lorentz violation in photons

$$\left| \frac{\delta c}{c} \right| \lesssim 10^{-15}$$



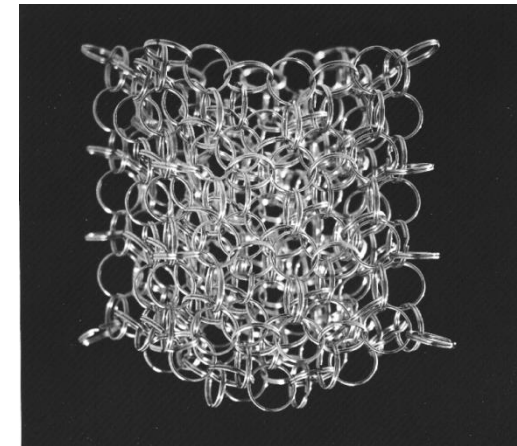
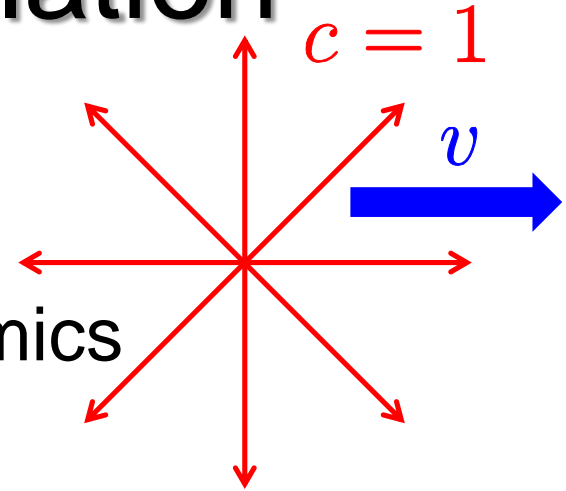
- Y. Michimura+, [Phys. Rev. Lett. \*\*110\*\*, 200401 \(2013\)](#)
- Y. Michimura+, [Phys. Rev. D \*\*88\*\*, 111101\(R\) \(2013\)](#)

# SR and Lorentz violation

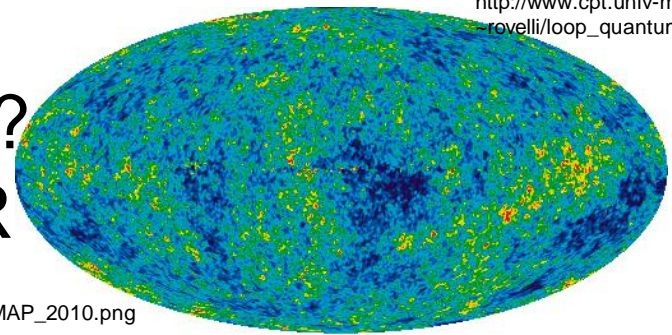
- Special Relativity (1905)  
speed of light is constant
- Lorentz invariance in electrodynamics
- no one could find any violation
- but...
  - quantum gravity suggests violation at some level  
e.g.  $\delta c/c \sim 10^{-17}$

D. Colladay and V. Alan Kostelecký:PRD 58 (1998) 116002

- anisotropy in CMB  
possible preferred frame?  
→ motivation for testing SR



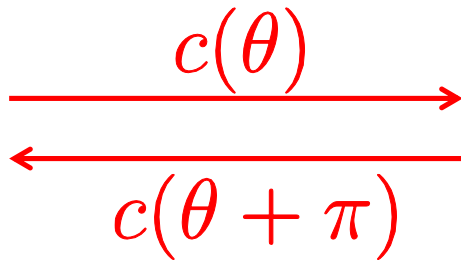
[http://www.cpt.univ-mrs.fr/~rovelli/loop\\_quantum\\_gravity.jpg](http://www.cpt.univ-mrs.fr/~rovelli/loop_quantum_gravity.jpg)



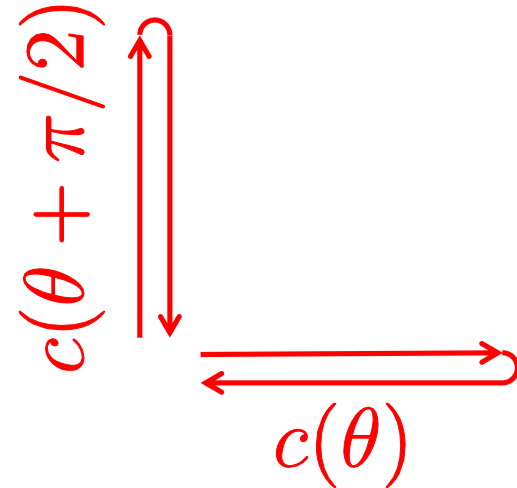
# Test of Special Relativity

- test of constancy of speed of light
- two types of test: even-parity and odd-parity

odd-parity test  
(Ives-Stilwell type test)

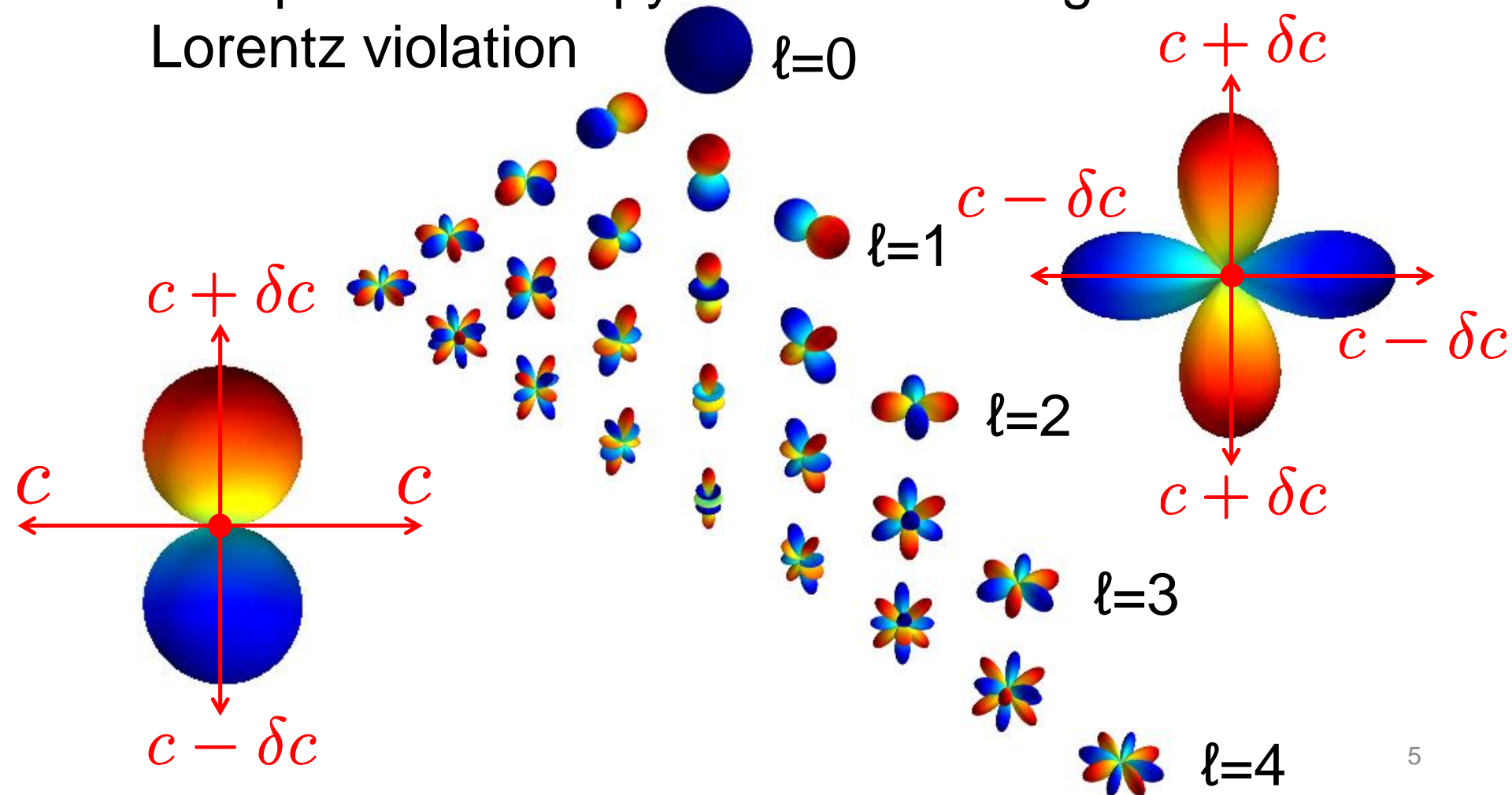


even-parity test  
(Michelson-Morley type test)



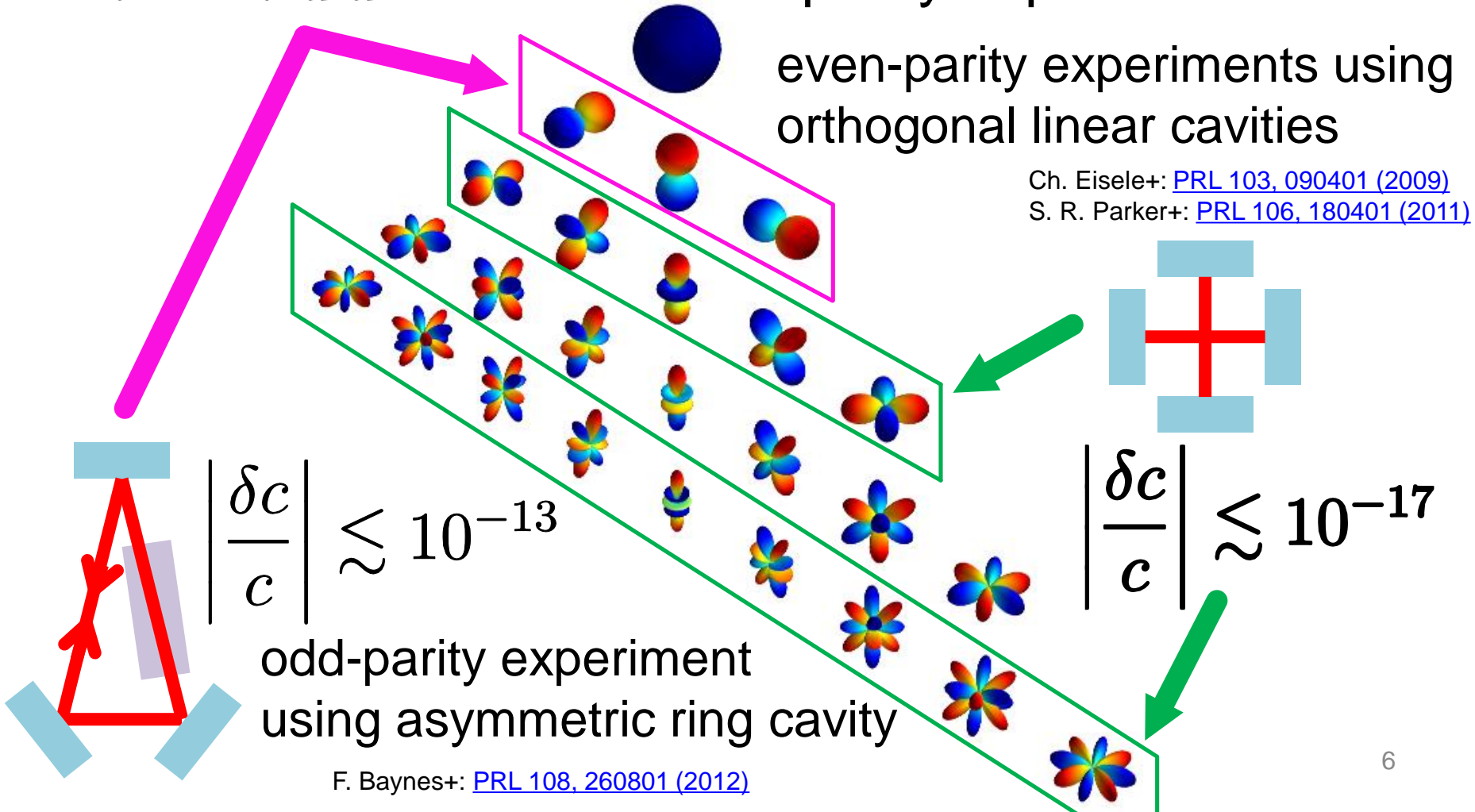
# Anisotropy in the Speed of Light

- can be expanded with spherical harmonics
- multipole anisotropy comes from higher order Lorentz violation



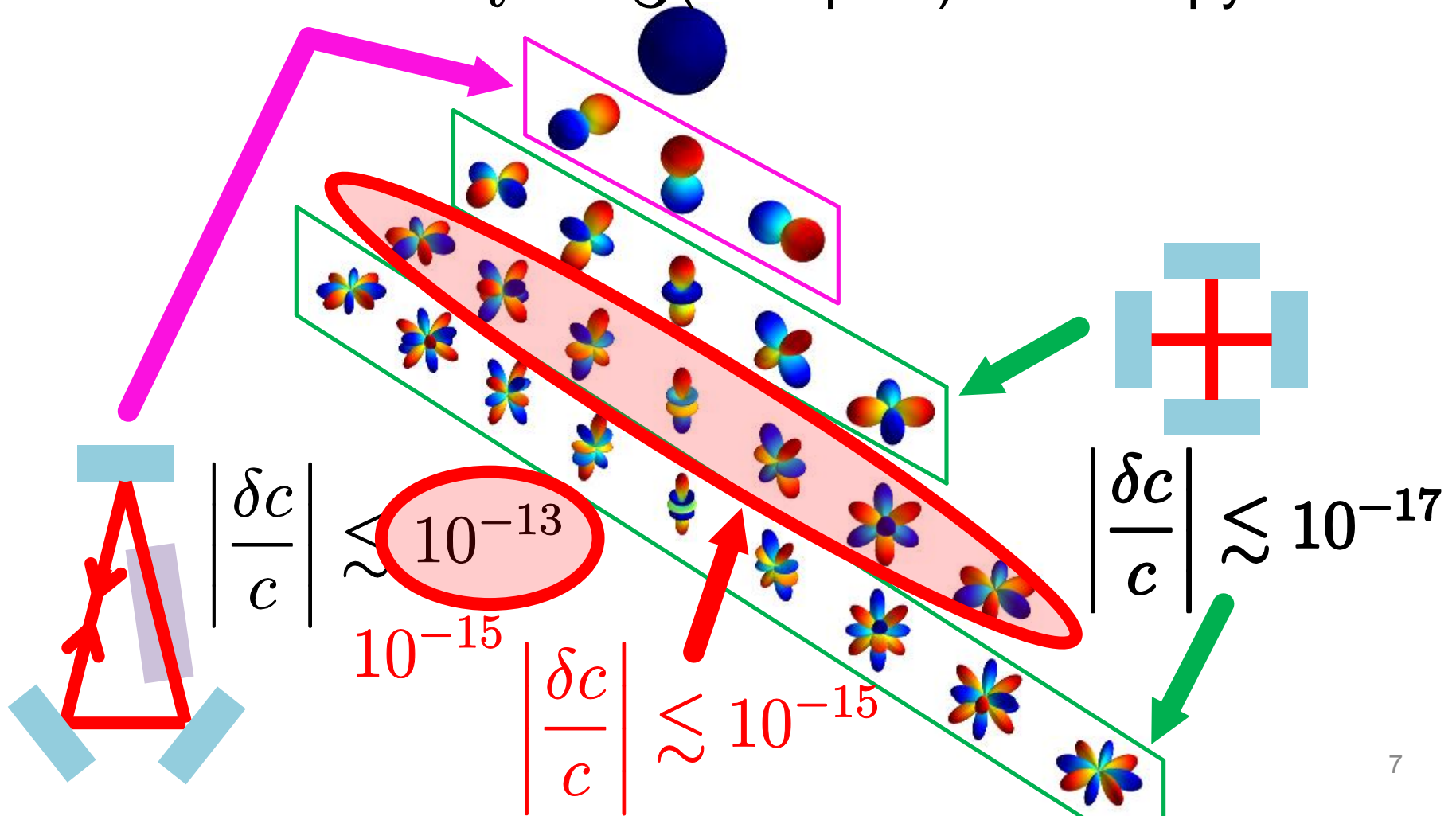
# Previous Limits

- $l = \text{even}$  limits with even-parity experiments
- $l = \text{odd}$  limits with odd-parity experiments



# Our Limits

- improved limits on  $l = 1$  (dipole) anisotropy
- new limits on  $l = 3$  (hexapole) anisotropy



# Optical Ring Cavity

- sensitive to LV when a dielectric is contained

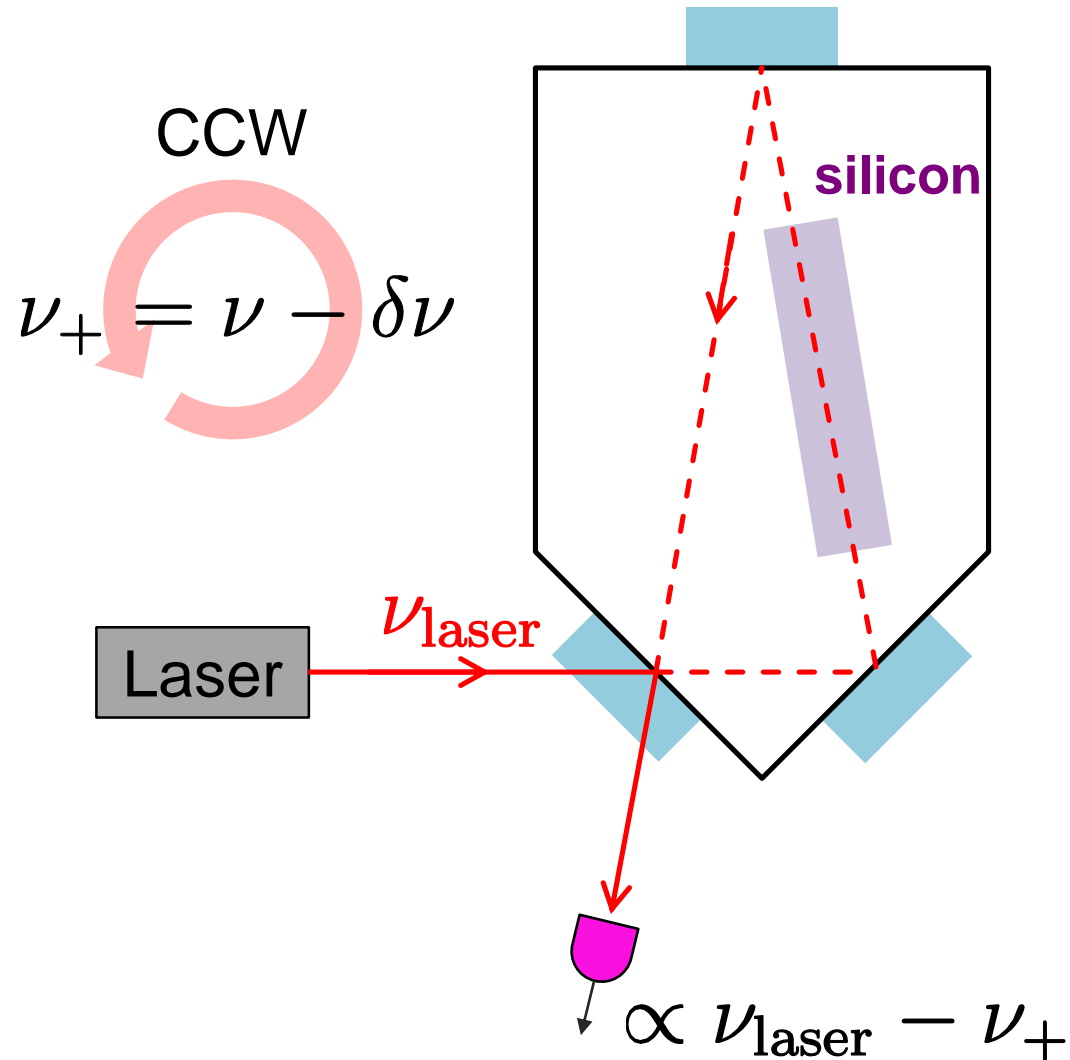
no LV	$\nu_+ = \nu_0$ $\nu_- = \nu_0$	$\nu_+ = \nu$ $\nu_- = \nu$ <div style="border: 1px solid red; padding: 5px; display: inline-block; color: red;">             freq. shift  <math>\propto</math> LV         </div>
LV	$\nu_+ = \nu_0$ $\nu_- = \nu_0$	$\nu_+ = \nu - \delta\nu$ $\nu_- = \nu + \delta\nu$

- $\nu_+ - \nu_-$  gives LV signal (null measurement)



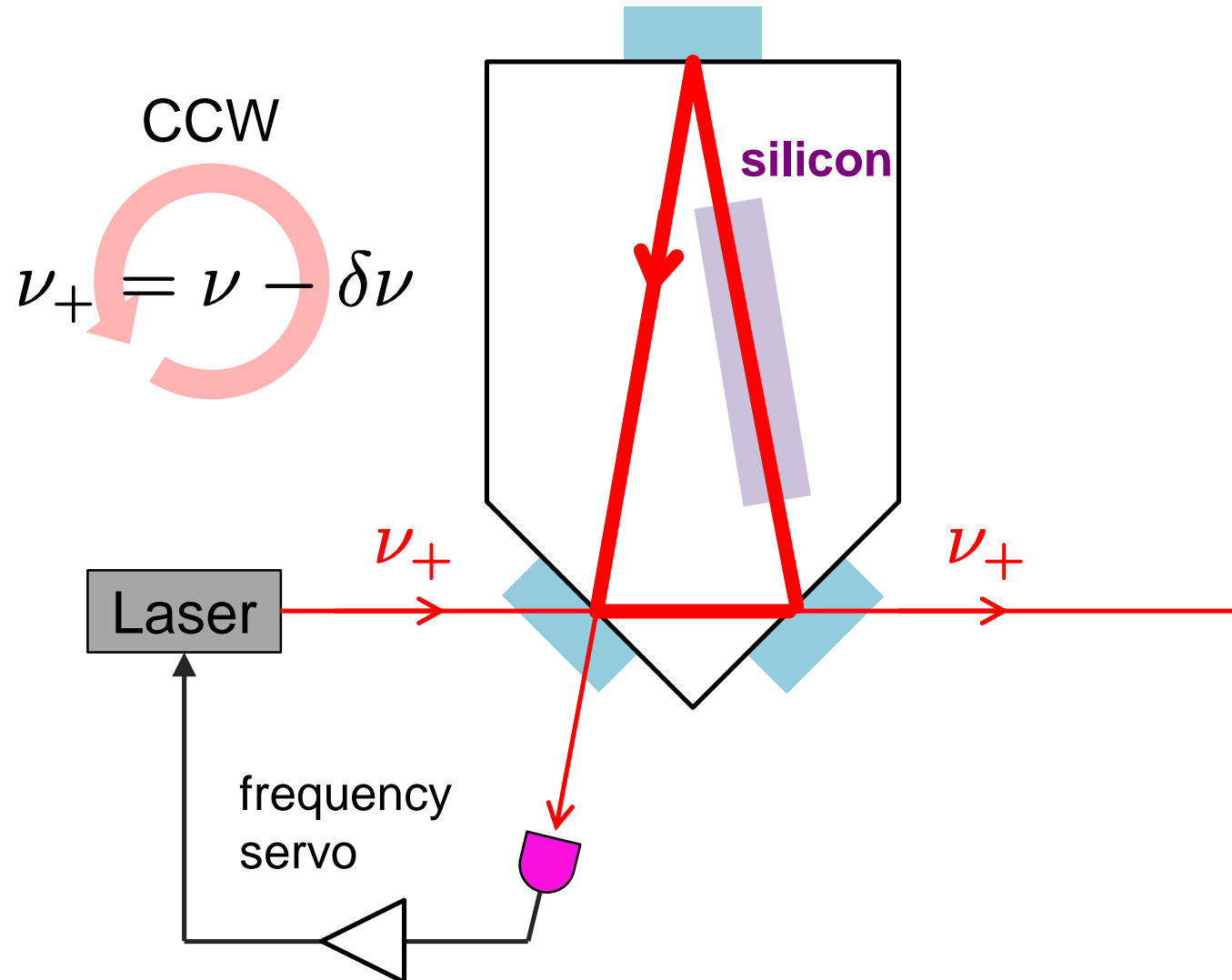
# How Do We Measure 1/4

- inject laser beam in CCW



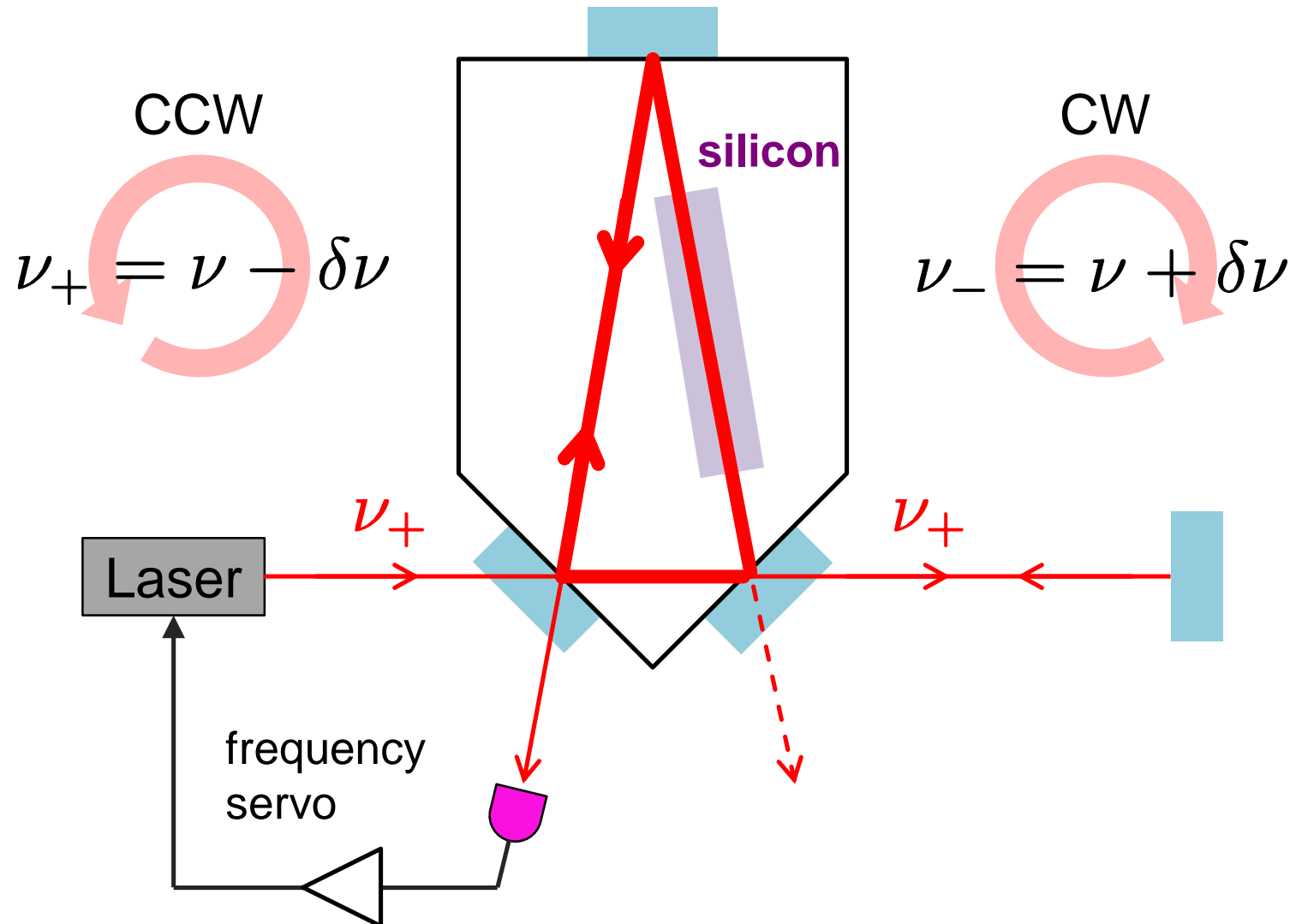
# How Do We Measure 2/4

- lock laser frequency to CCW resonance ( $\nu_+$ )



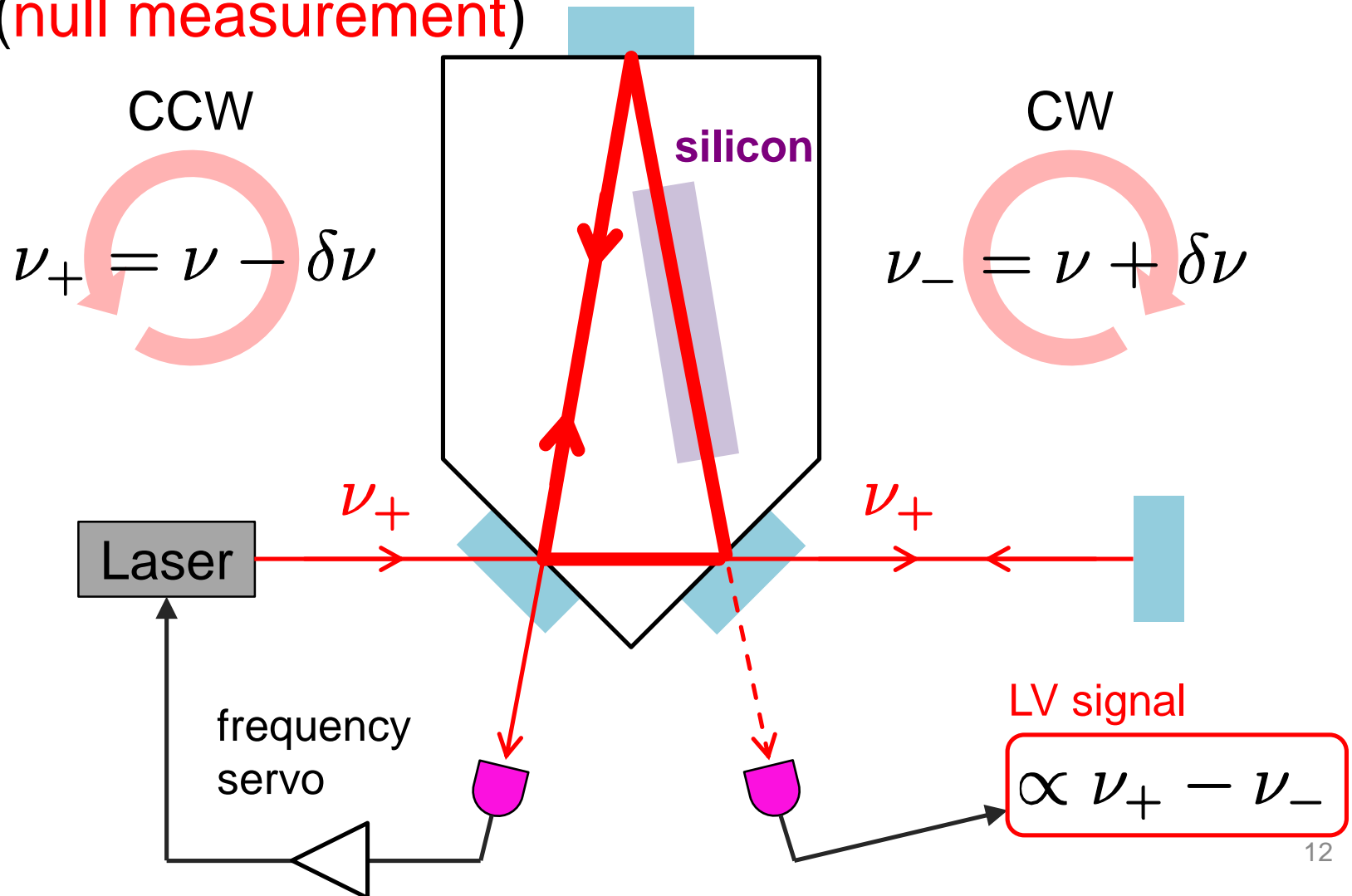
# How Do We Measure 3/4

- reflect the beam back into the cavity in CW



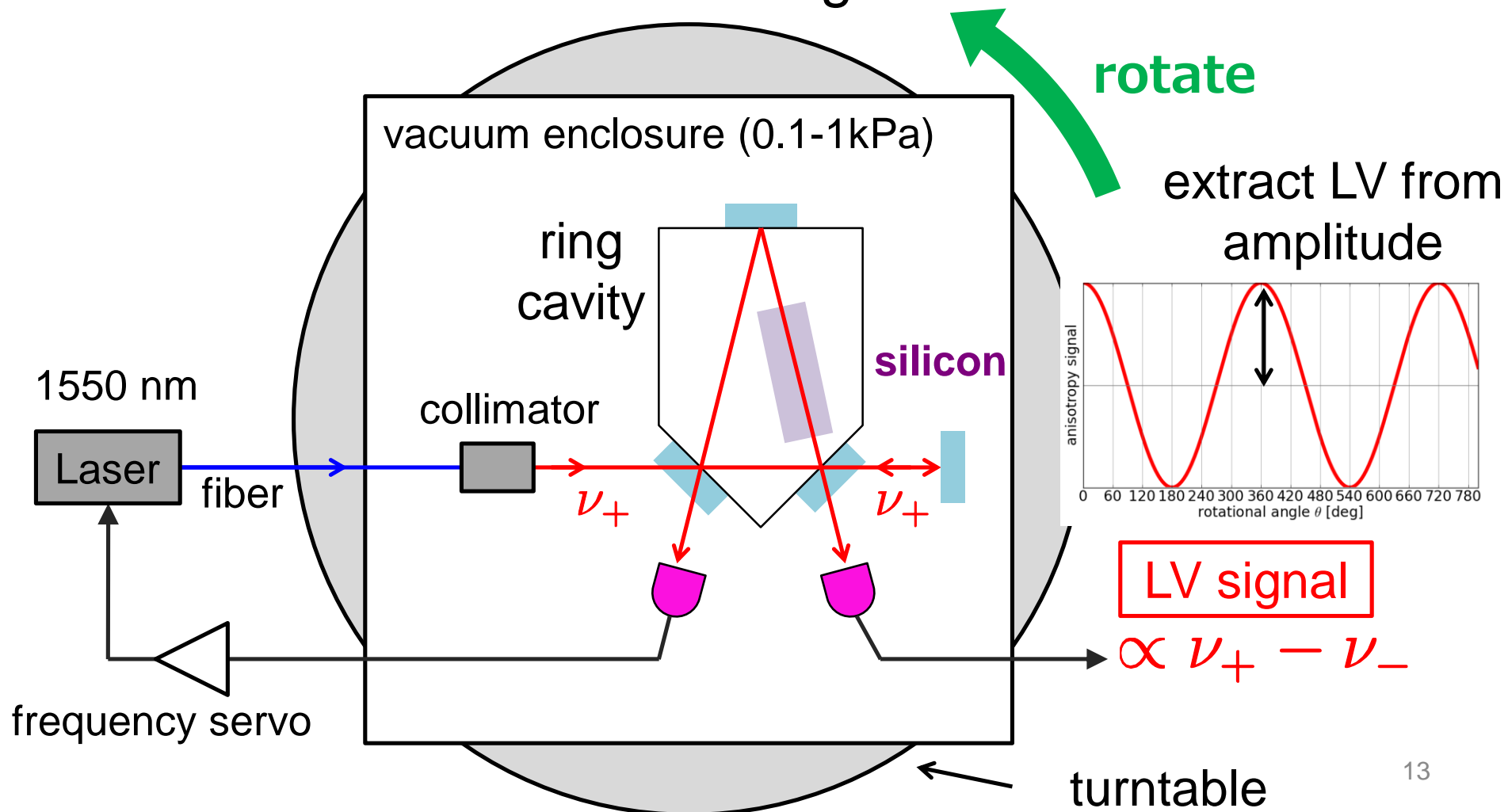
# How Do We Measure 4/4

- LV signal obtained from cavity reflection (null measurement)



# Experimental Setup

- frequency comparison using double-pass setup
- rotate and modulate LV signal



# Photo of the Optics

Inside vacuum enclosure  
(30cm × 30cm × 17cm)

ring  
cavity

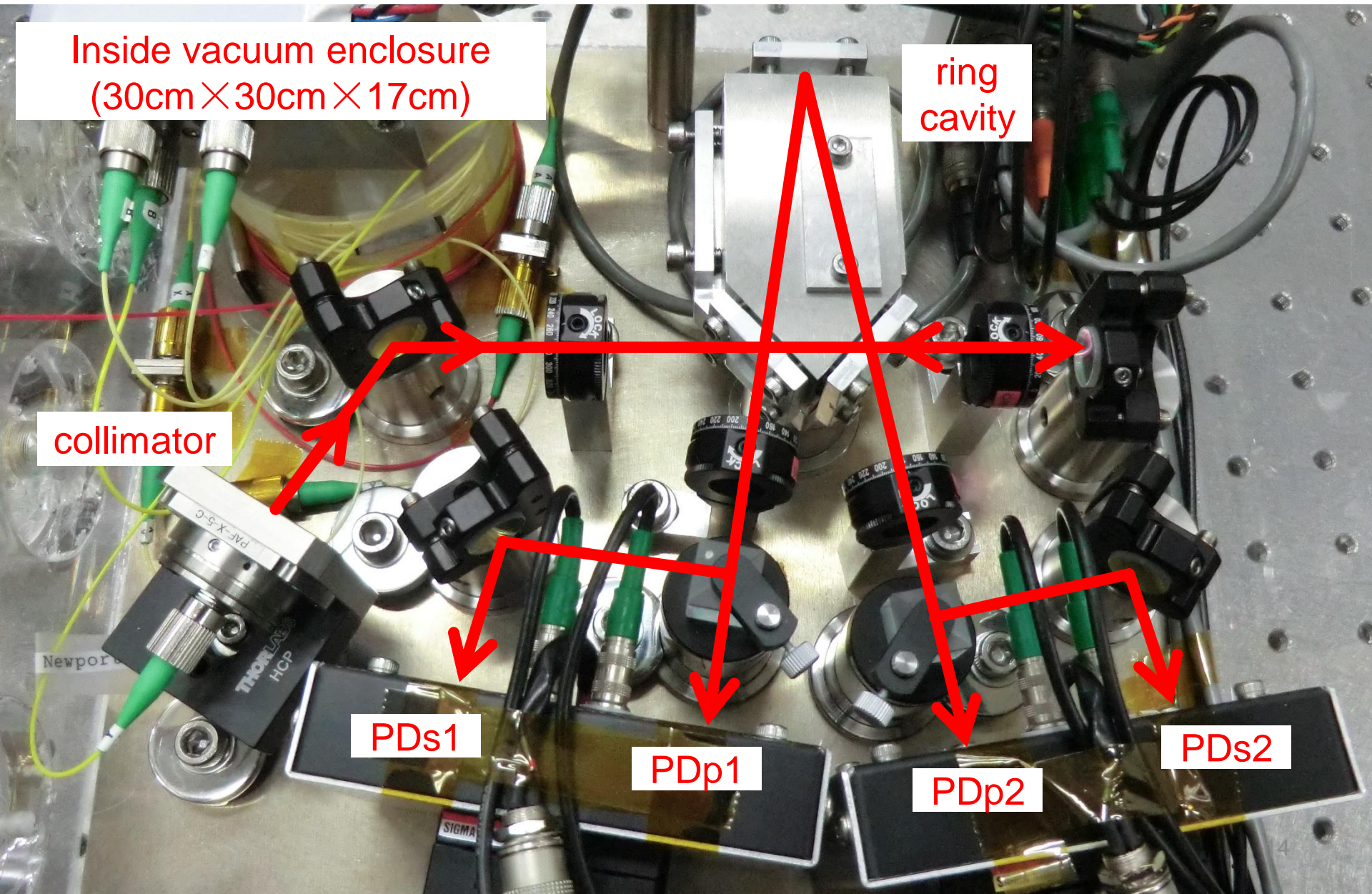
collimator

PDs1

PDp1

PDp2

PDs2



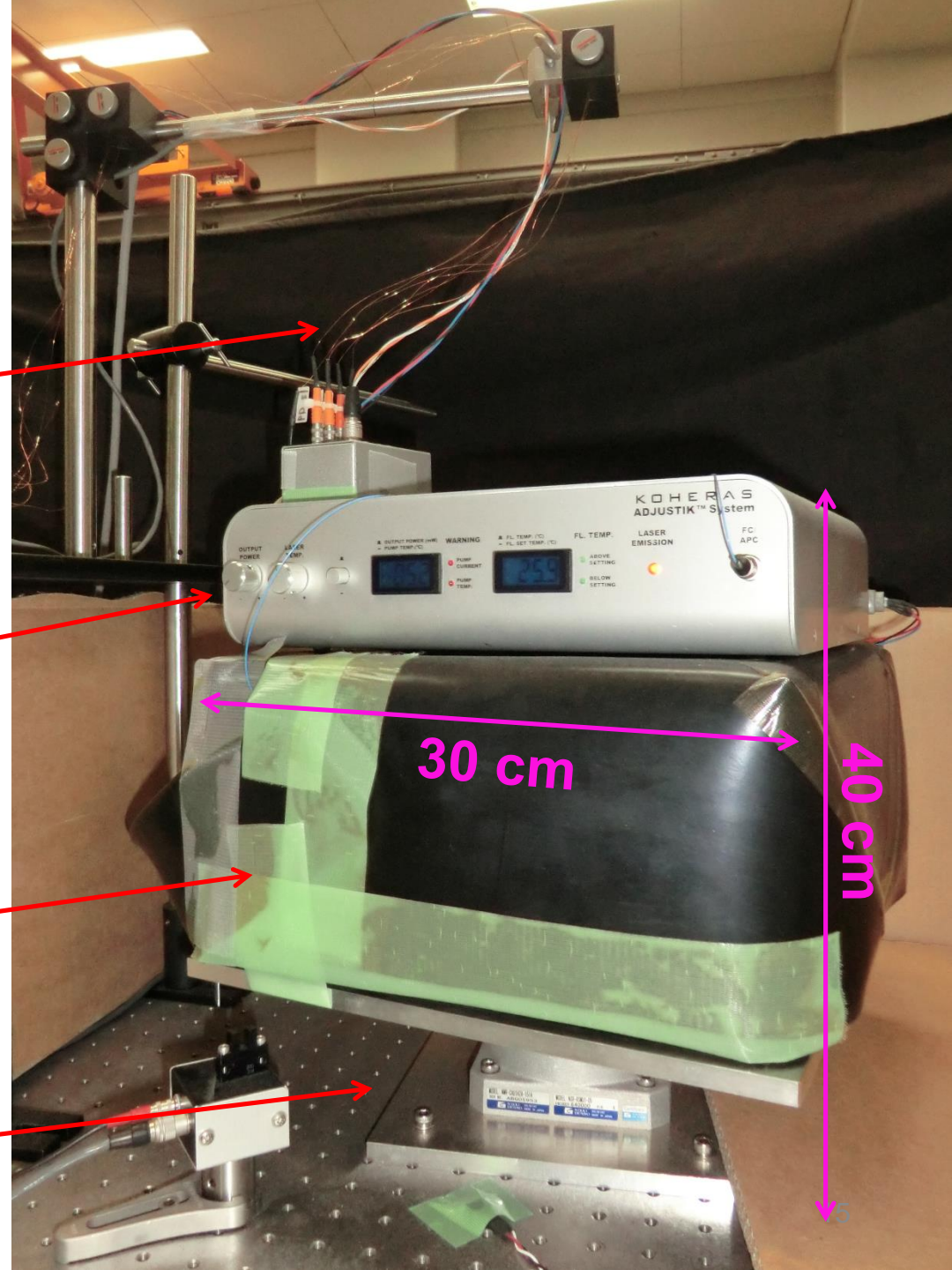
# Photo of the Whole Setup

electrical cables

laser source

vacuum enclosure  
+ shielding  
(optics inside)

turntable

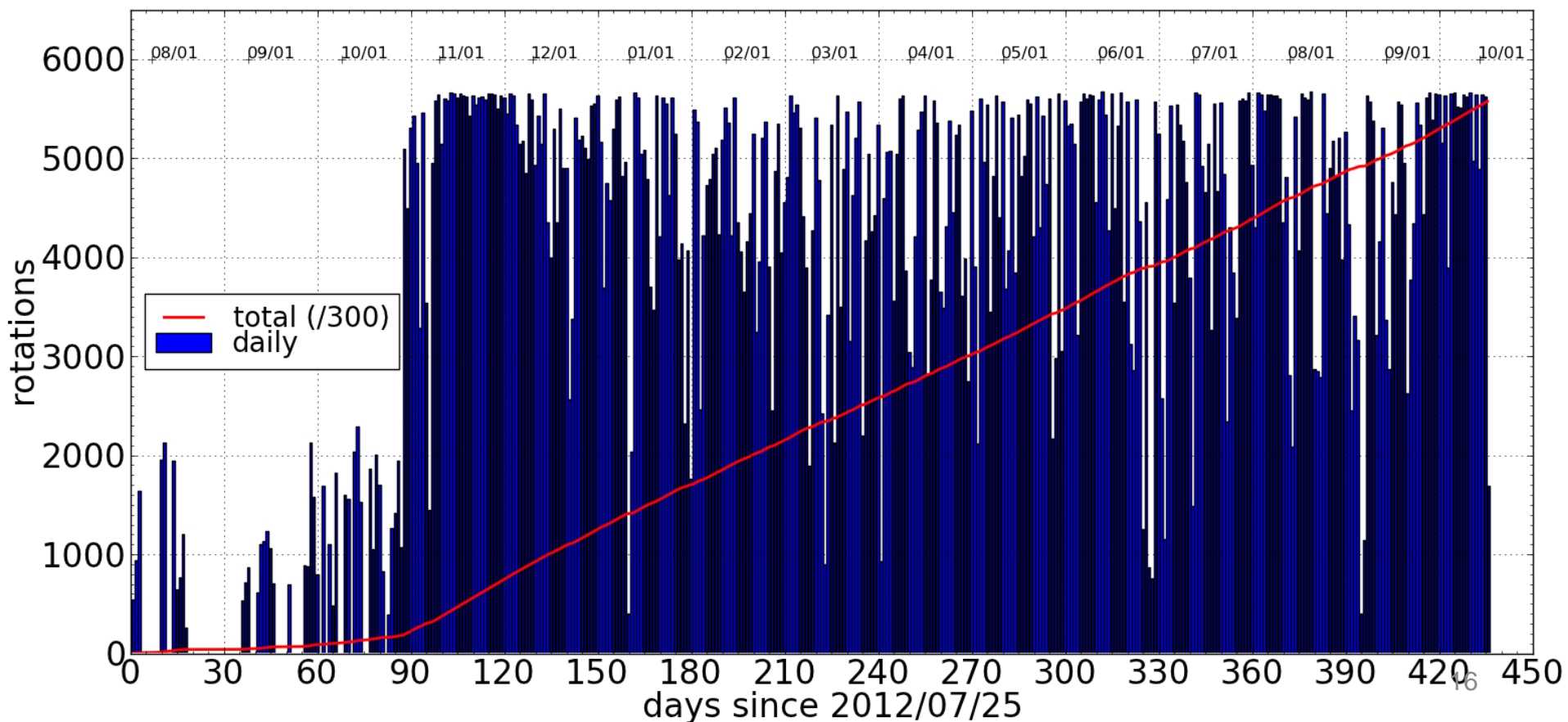


30 cm

40 cm

# Observation Data

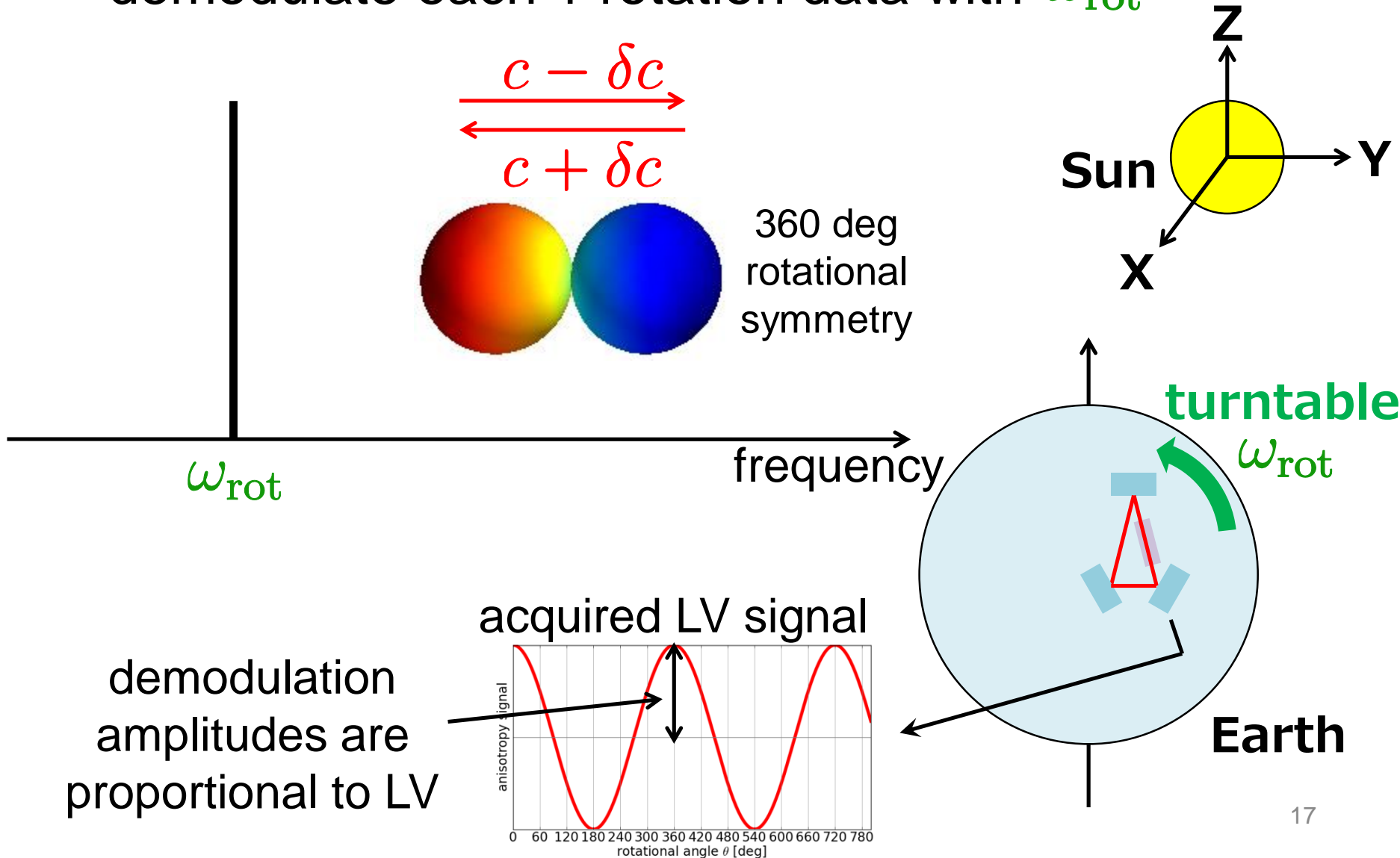
- from July 2012 to October 2013
- 393 days, 1.67 million rotations
- duty cycle: 53% (64% after Oct 2012)





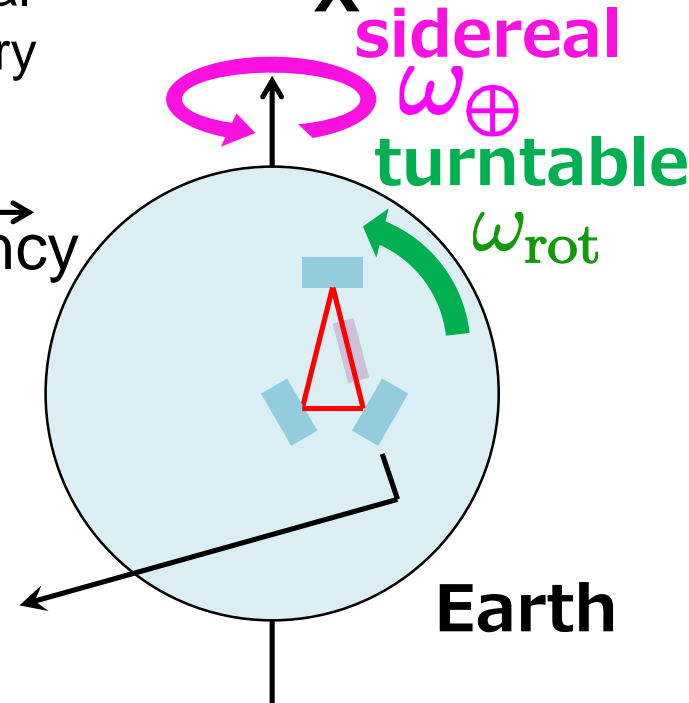
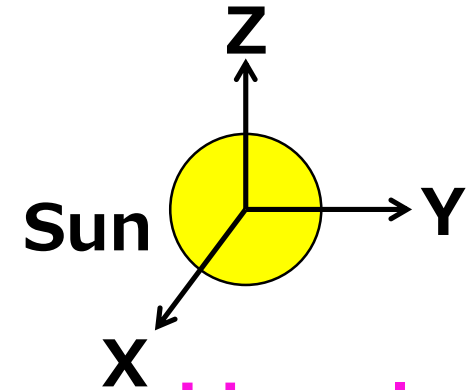
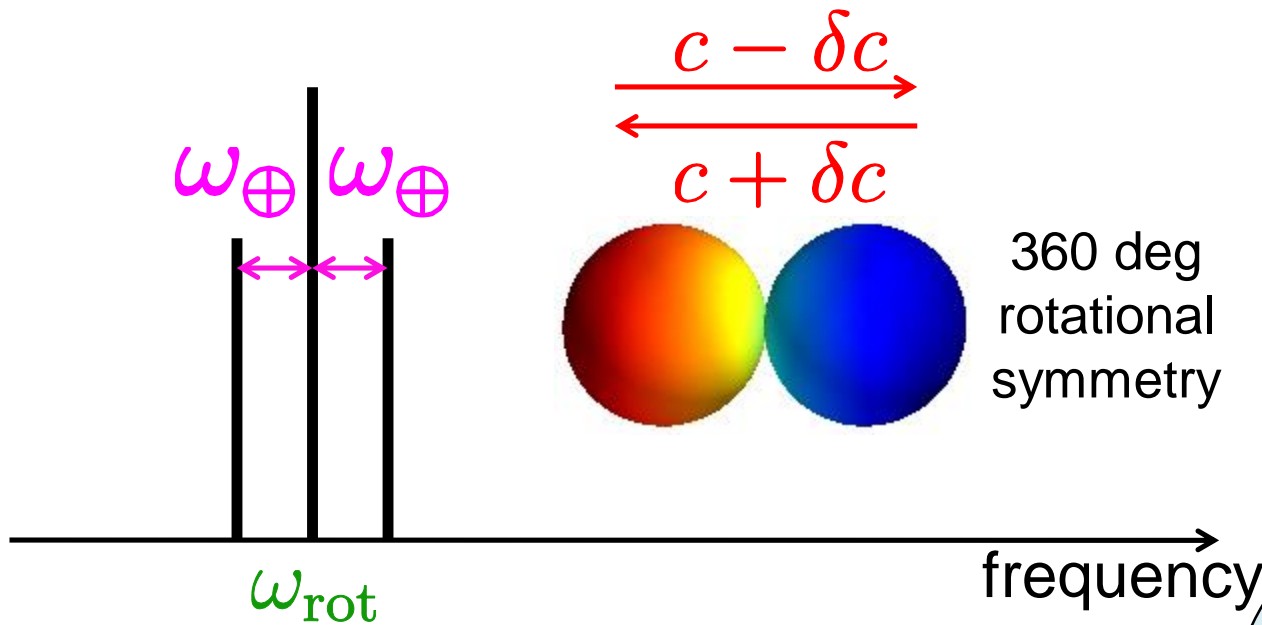
# Data Analysis 1/3

- demodulate each 1 rotation data with  $\omega_{rot}$

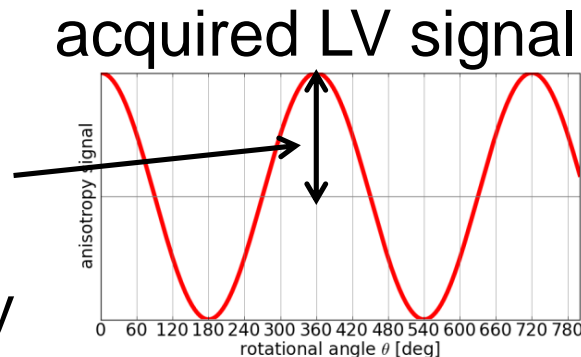


# Data Analysis 2/3

- next, demodulate 1 day data with  $\omega_{\oplus}$

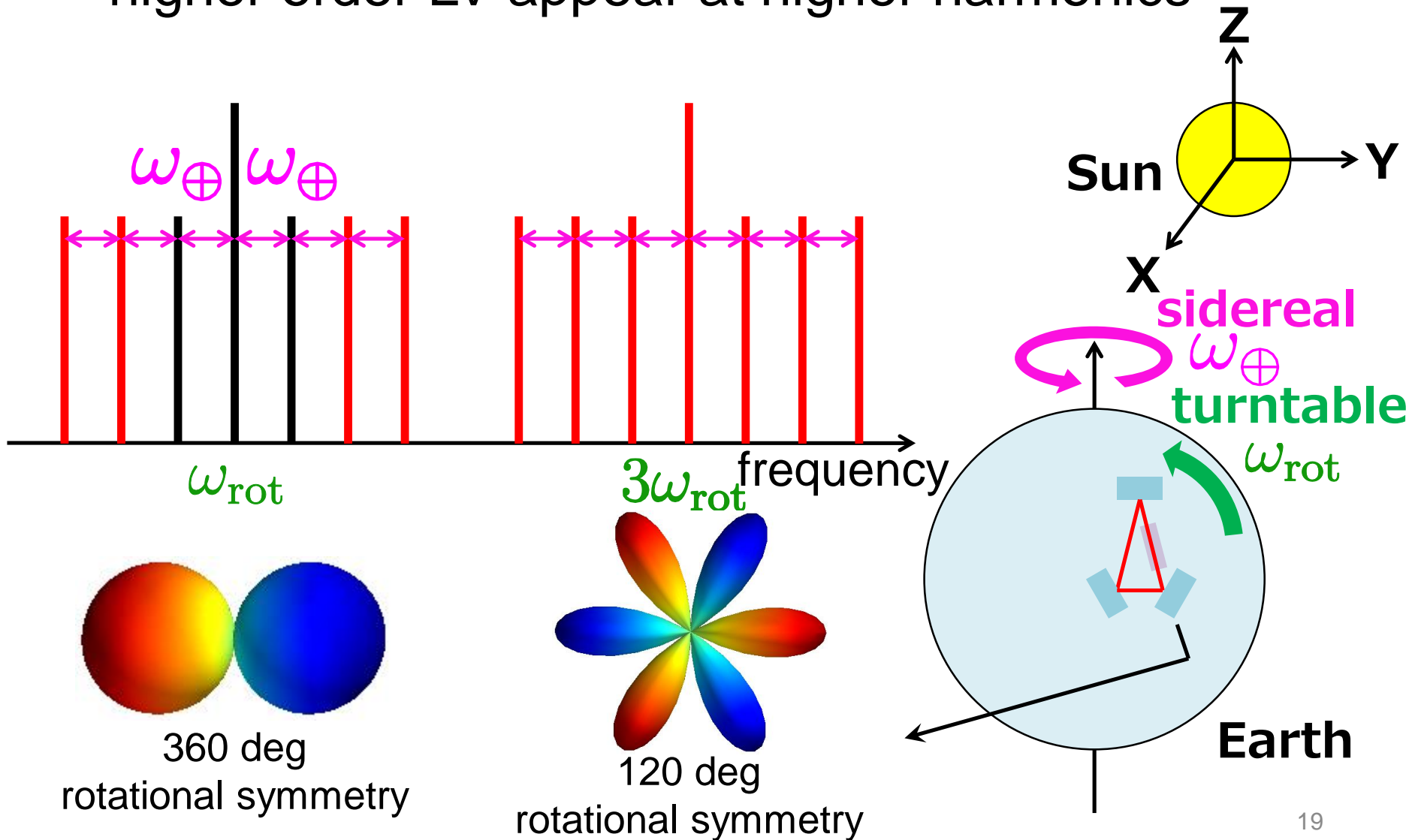


demodulation amplitudes are modulated by sidereal frequency

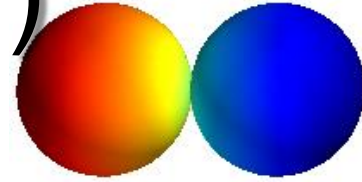


# Data Analysis 3/3

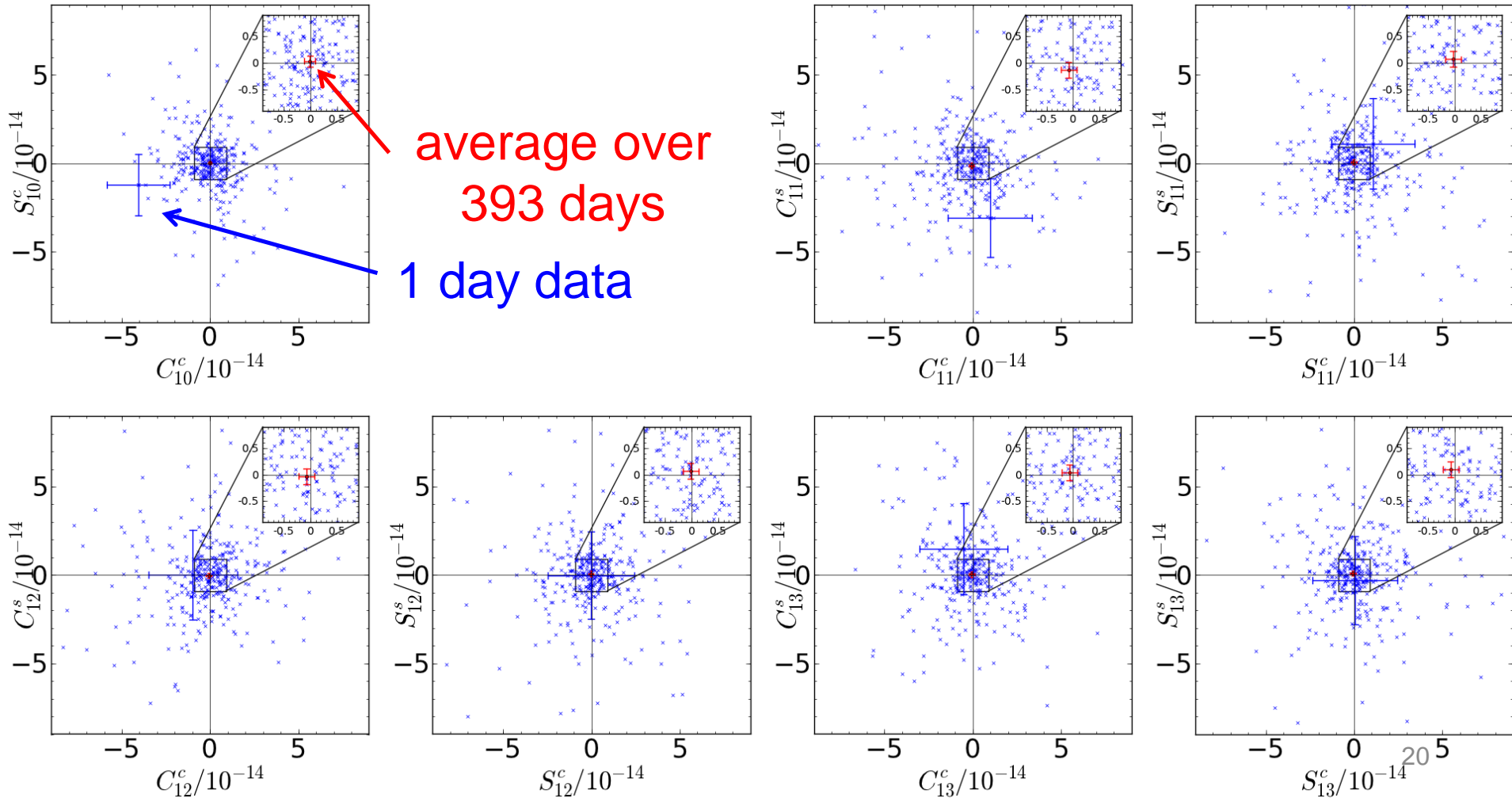
- higher order LV appear at higher harmonics



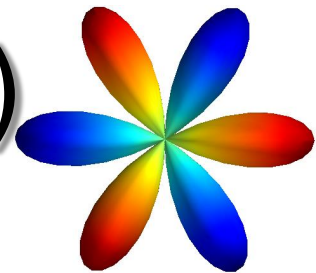
# Demodulation Amps( $\omega_{\text{rot}}$ )



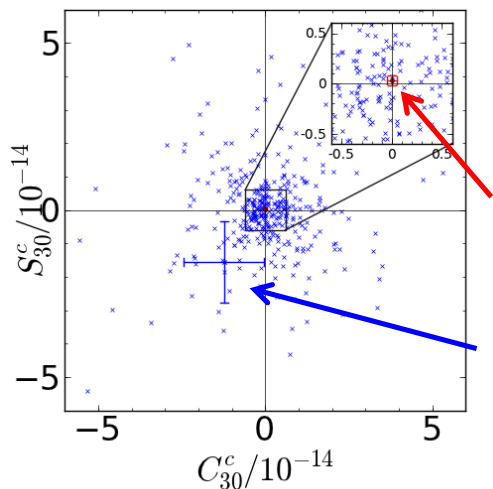
- zero consistent at  $2\sigma$   
→ no significant LV can be claimed



# Demodulation Amps( $3\omega_{\text{rot}}$ )

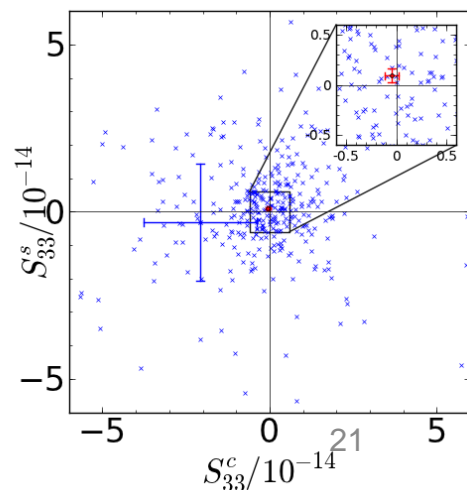
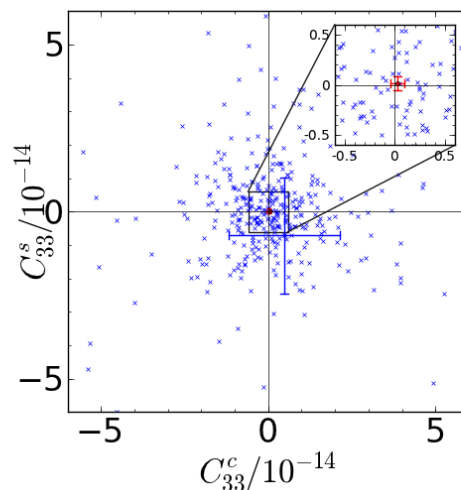
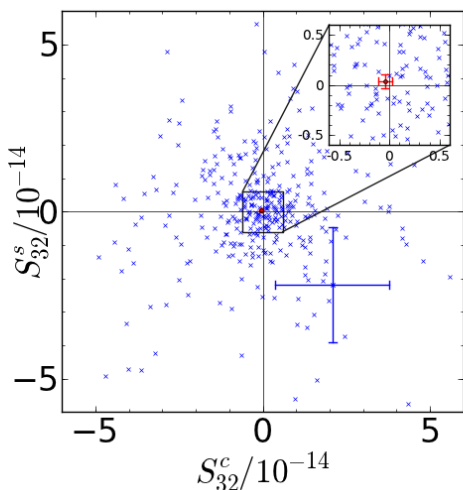
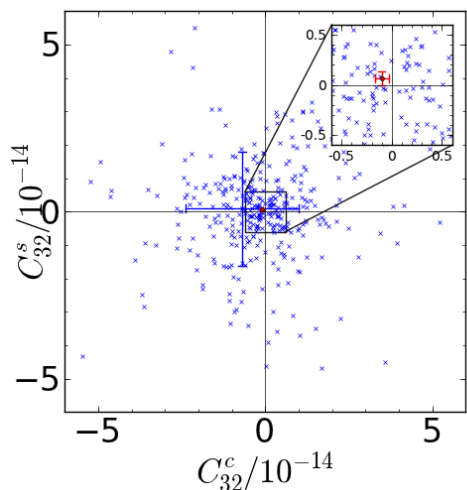
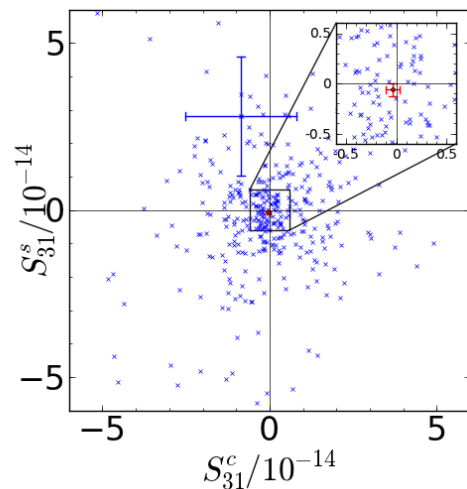
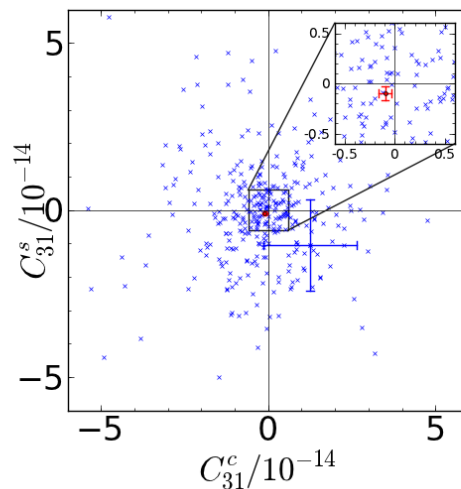


- zero consistent at  $2\sigma$   
→ no significant LV can be claimed



average over  
393 days

1 day data



# Our Limits on Anisotropy

- each demodulation amplitude is related to each anisotropy component

- limits three dipole ( $l = 1$ ) components

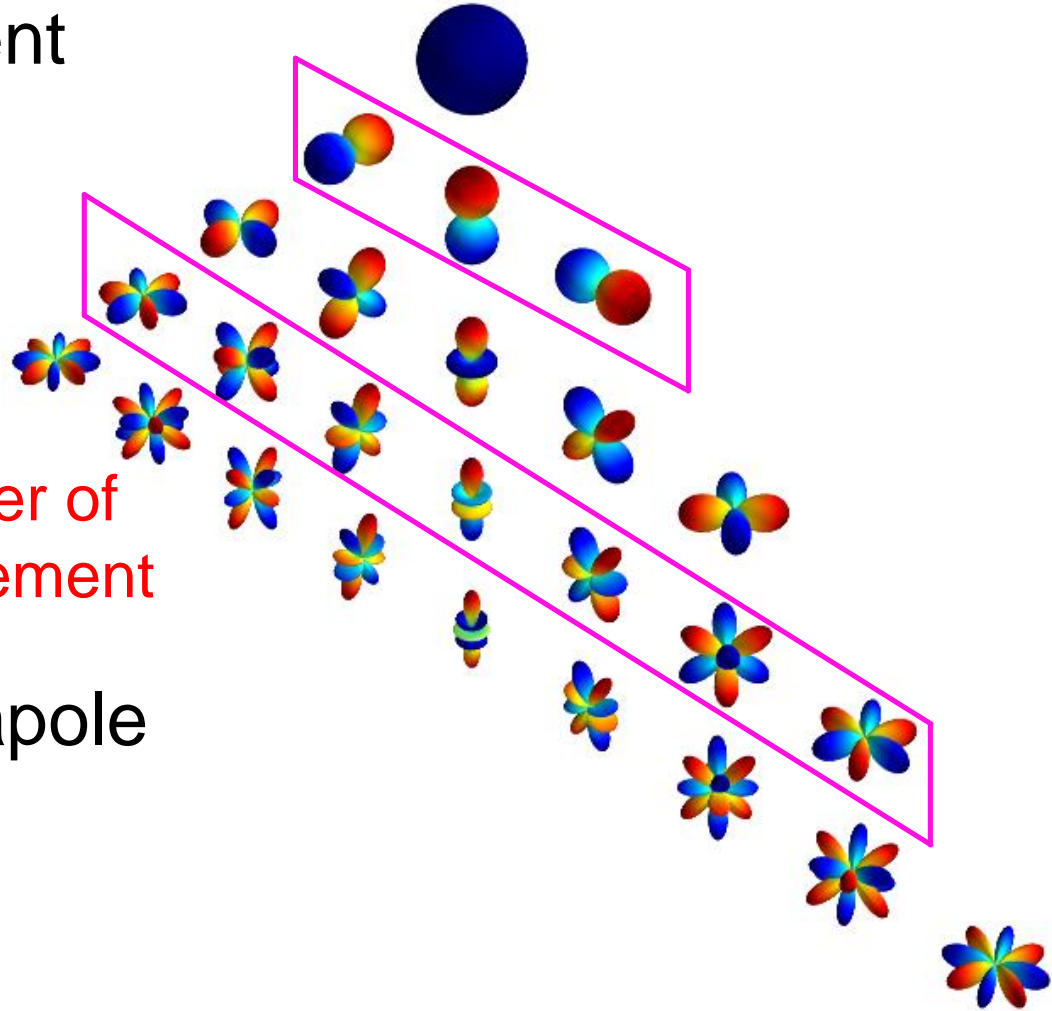
$$\left| \frac{\delta c}{c} \right| \lesssim 6 \times 10^{-15}$$

more than an order of magnitude improvement

- limits on seven hexapole ( $l = 3$ ) components

$$\left| \frac{\delta c}{c} \right| \lesssim 2 \times 10^{-15}$$

new limit



# Our Limits on SME Coefficients

- Standard Model Extension (SME)
  - [ D. Colladay and V. Alan Kostelecký: [PRD 58, 116002 \(1998\)](#) ]
- test theory with all realistic Lorentz violation
- our result put **new limits** on “camouflage coefficients” of LV in photon sector

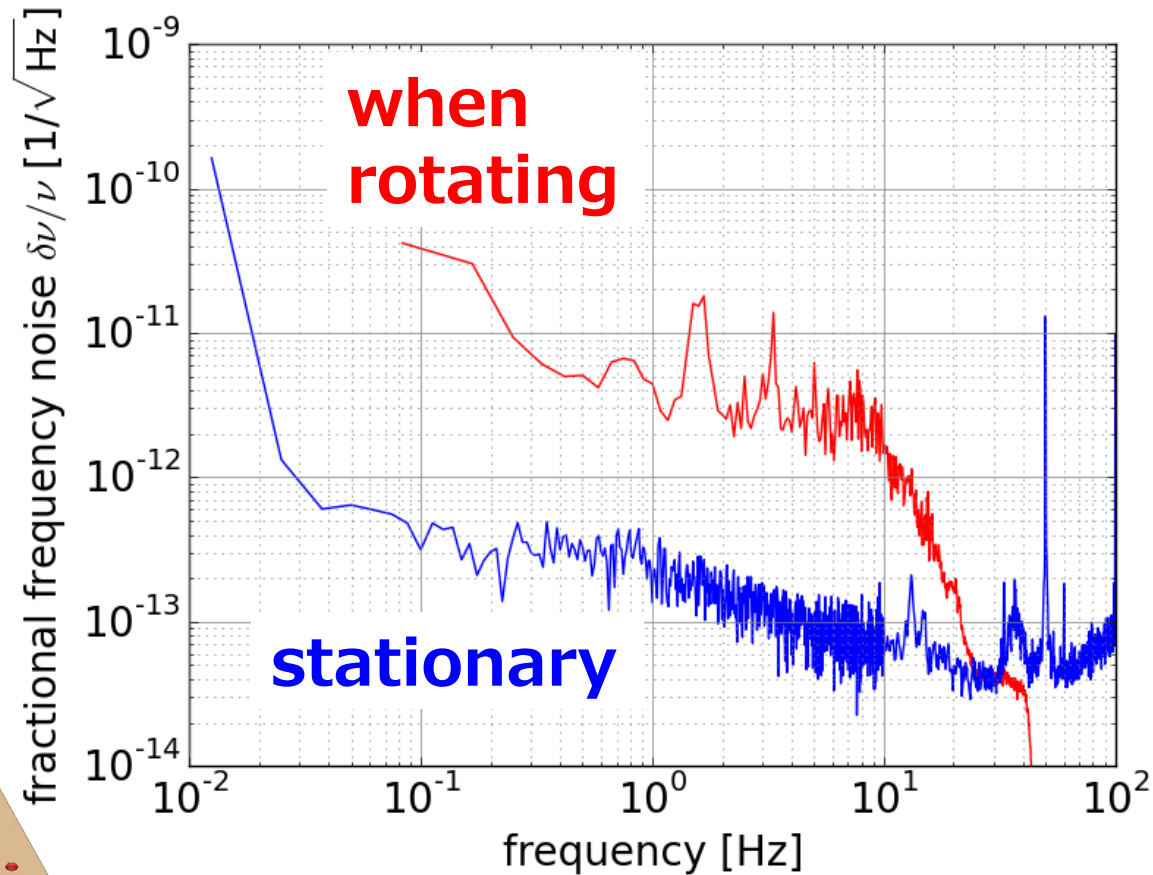
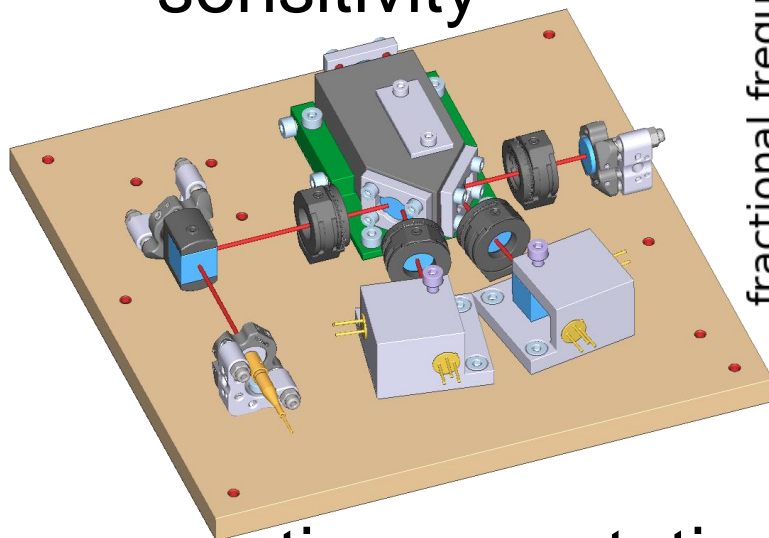
Dimension	Coefficient	Measurement
$d = 6$	$(\bar{c}_F^{(6)})_{110}^{(0E)}$	$(-0.1 \pm 1.5) \times 10^3 \text{ GeV}^{-2}$
	$\text{Re}[(\bar{c}_F^{(6)})_{111}^{(0E)}]$	$(-0.8 \pm 1.1) \times 10^3 \text{ GeV}^{-2}$
	$\text{Im}[(\bar{c}_F^{(6)})_{111}^{(0E)}]$	$(-0.6 \pm 1.0) \times 10^3 \text{ GeV}^{-2}$
$d = 8$	$-0.020(\bar{c}_F^{(8)})_{110}^{(0E)} + (\bar{c}_F^{(8)})_{310}^{(0E)}$	$(-0.2 \pm 1.9) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Re}[-0.020(\bar{c}_F^{(8)})_{111}^{(0E)} + (\bar{c}_F^{(8)})_{311}^{(0E)}]$	$(1.4 \pm 1.3) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Re}[-0.020(\bar{c}_F^{(8)})_{111}^{(0E)} + (\bar{c}_F^{(8)})_{311}^{(0E)}]$	$(0.1 \pm 1.3) \times 10^{19} \text{ GeV}^{-4}$
	$(\bar{c}_F^{(8)})_{330}^{(0E)}$	$(-0.8 \pm 3.3) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Re}[(\bar{c}_F^{(8)})_{331}^{(0E)}]$	$(-0.3 \pm 1.9) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Im}[(\bar{c}_F^{(8)})_{331}^{(0E)}]$	$(-2.8 \pm 1.9) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Re}[(\bar{c}_F^{(8)})_{332}^{(0E)}]$	$(2.2 \pm 1.3) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Im}[(\bar{c}_F^{(8)})_{332}^{(0E)}]$	$(0.2 \pm 1.3) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Re}[(\bar{c}_F^{(8)})_{333}^{(0E)}]$	$(-0.1 \pm 1.6) \times 10^{19} \text{ GeV}^{-4}$
	$\text{Im}[(\bar{c}_F^{(8)})_{333}^{(0E)}]$	$(-0.1 \pm 1.6) \times 10^{19} \text{ GeV}^{-4}$

limits on LV of  
dimension 6  
 $10^3 \text{ GeV}^{-2}$

limits on LV of  
dimension 8  
 $10^{19} \text{ GeV}^{-4}$

# Upgrade of the Apparatus

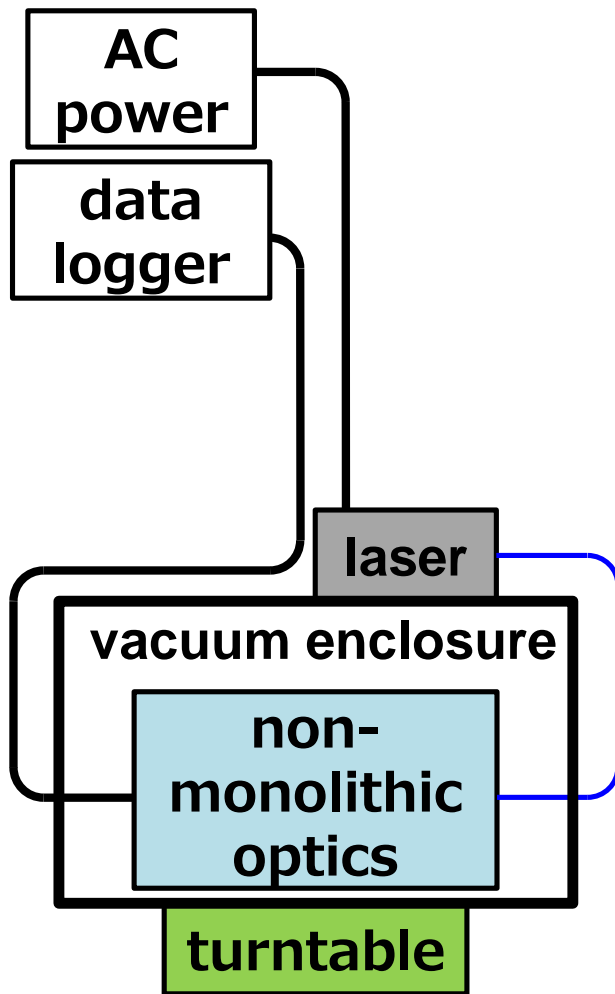
- current noise level is limited by vibration noise from rotation
- semi-monolithic optical bench to reduce vibration sensitivity



- continuous rotation for more stable operation

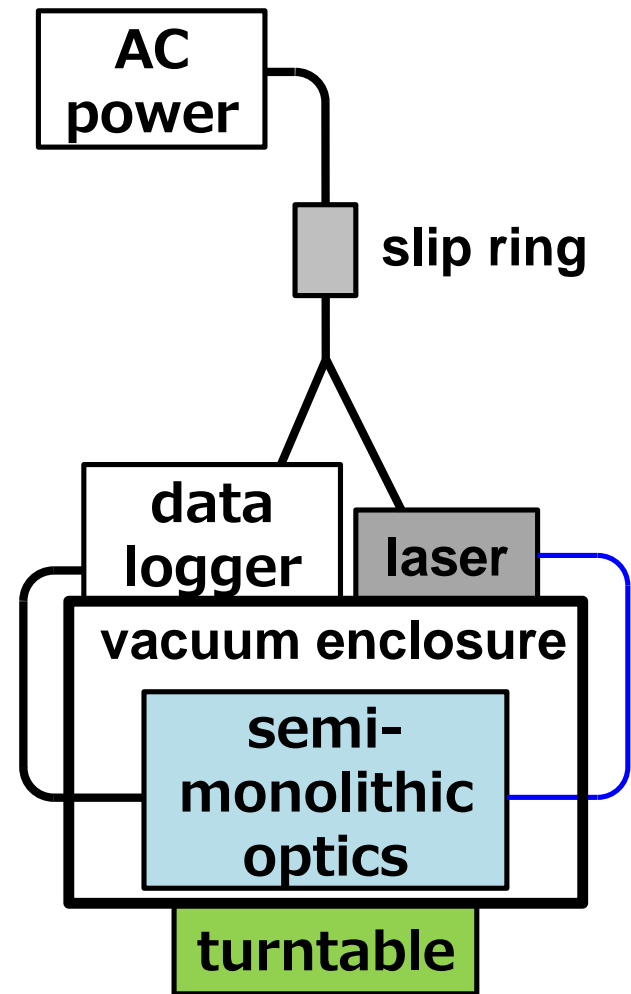


# Apparatus Comparison



2012 Model

- non-monolithic optics
- alternative rotation



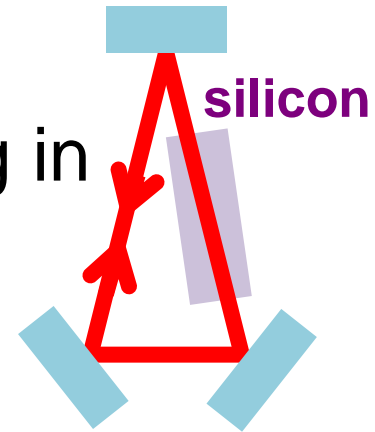
New Model

- semi-monolithic optics
- continuous rotation

# Summary and Outlook

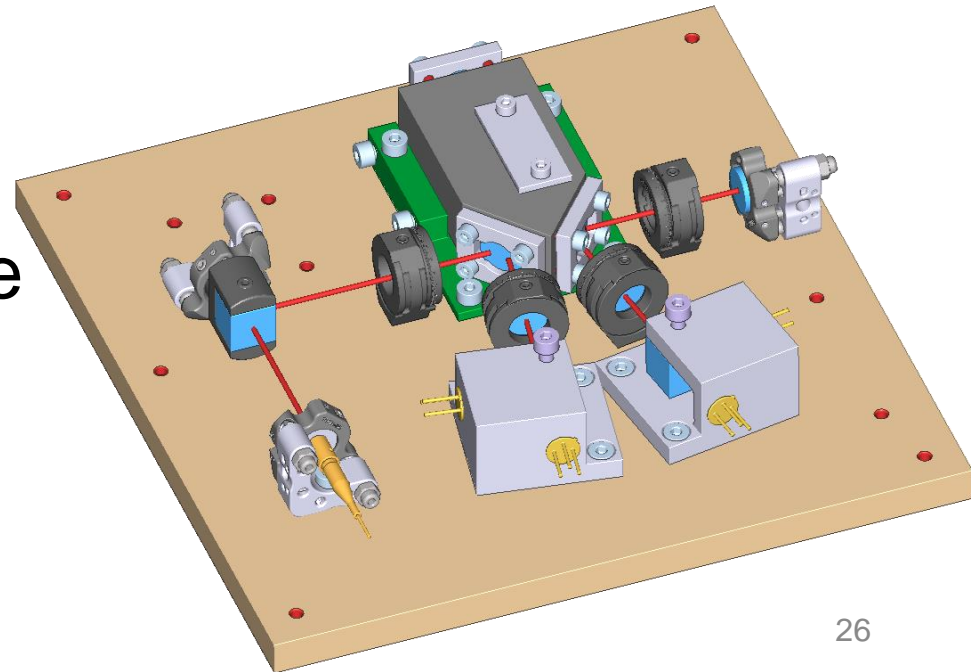
## Summary

- compared the speed of light propagating in opposite directions
- using a double-pass optical ring cavity
- put new limits on higher order LV in photons



## Outlook

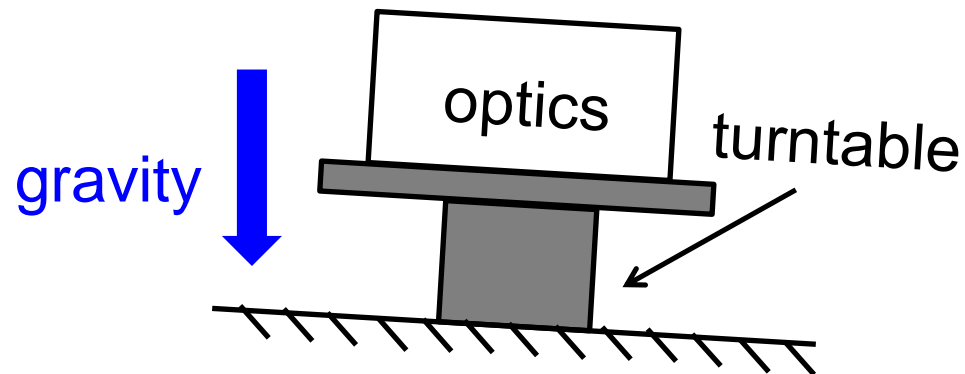
- currently upgrading the apparatus
- semi-monolithic optics
- continuous rotation



# Additional Slides

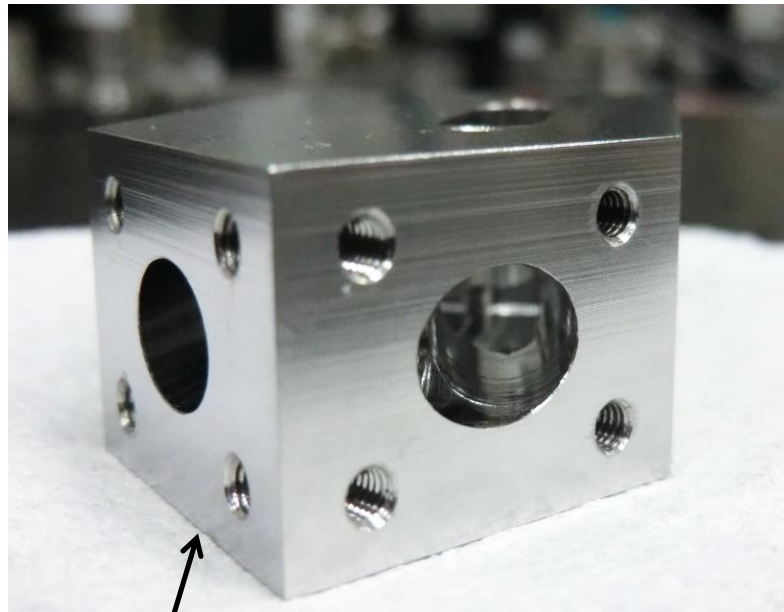
# Systematic Errors

- 10% of statistical error at maximum

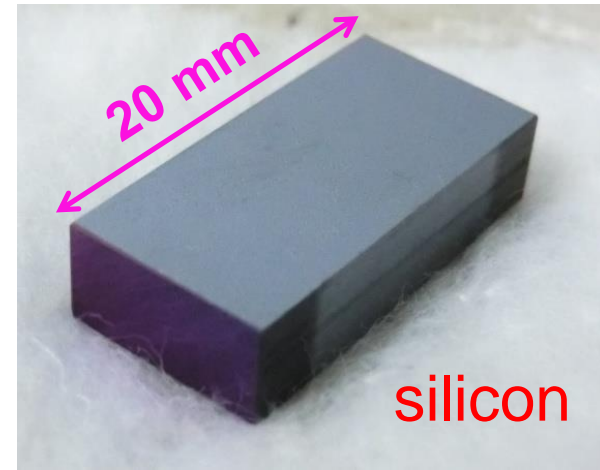


Cause	Amount	Ratio	
Sagnac effect	< 1mrad/sec	<2%	} offset
turntable tilt	< 0.2 mrad	<10%	
detuning	-	3%	} calibration
TF meas.	-	3%	
laser frequency actuation meas.	$12.9 \pm 0.6$ MHz/V	5%	
refractive index	$3.69 \pm 0.01$	0.4%	
cavity length	$192 \pm 1$ mm	0.5%	

# Some Photos

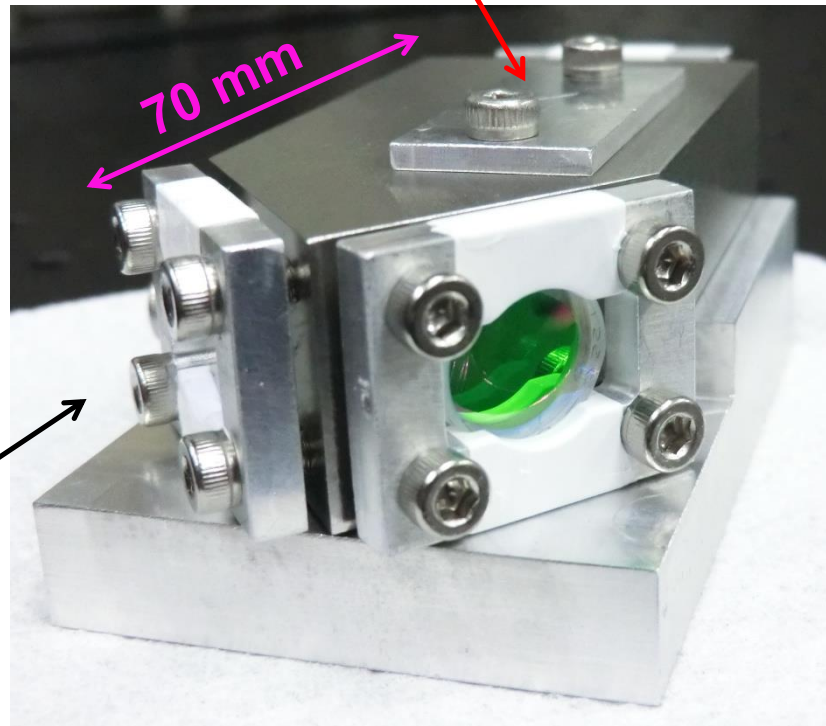


spacer made of  
Super Invar



silicon inside

silicon



cavity mirrors

# Cheat Sheet

- rotation frequency  $f_{\text{rot}} = 0.083$  Hz  
( $T_{\text{rot}} = 12$  sec)
- wavelength  $\lambda = 1550$  nm
- laser frequency  $\nu = 1.9e14$  Hz
- input power  $P_0 = 1$  mW
- finesse  $F = 120$
- cavity length  $L = 140$  mm
- silicon length  $d = 20$  mm
- silicon refractive index  $n = 3.69$
- silicon  $dn/dT = 2e-4$  /K
- silicon thermal expansion =  $3e-6$  /K
- Super Invar thermal exp. =  $\sim 1e-7$  /K
- silicon AR loss  $I < 0.5$  % / surface
- incident angle  $\theta = 9.5$  deg
- FSR = 1.5 GHz
- FWHM = 12 MHz
- current sensitivity  $\sim 6e-13$  /rtHz  
( $\sim 4e-11$  /rtHz when rotated)
- shot noise  $\sim 6e-16$  /rtHz
- thermal noise  $\sim 8e-16$  /rtHz  
(all @ 0.1 Hz)
- Sun speed in CMBR = 369 km/s
- orbital speed of Earth = 30 km/s
- rotational speed of Earth = 0.4 km/s
- History
  - Jul 2011: idea
  - Nov 2011: first run (10hour)
  - Jul 2012: data taking started
  - Oct 2012: continuous data taking
  - Oct 2013: shut down
- cost  $< \sim 200$ 万円