

# Search for Anisotropy in the One-Way Speed of Light Using an Optical Ring Cavity

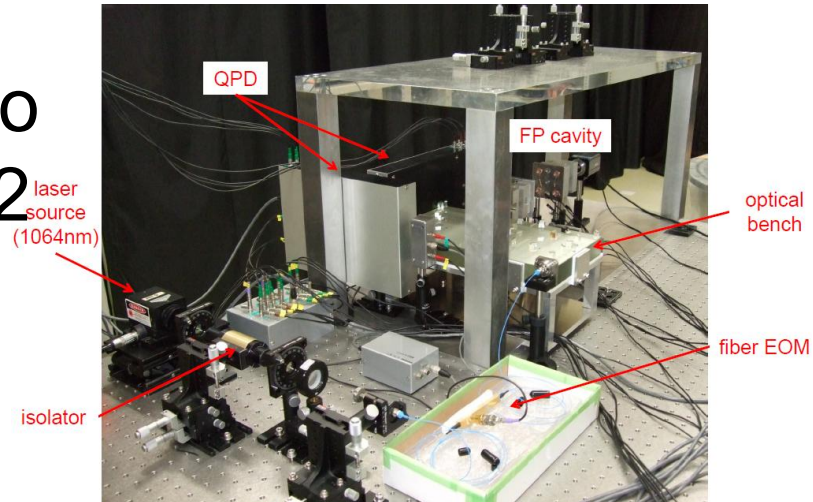
Yuta Michimura

Tsubono Group  
University of Tokyo

# Self-introduction

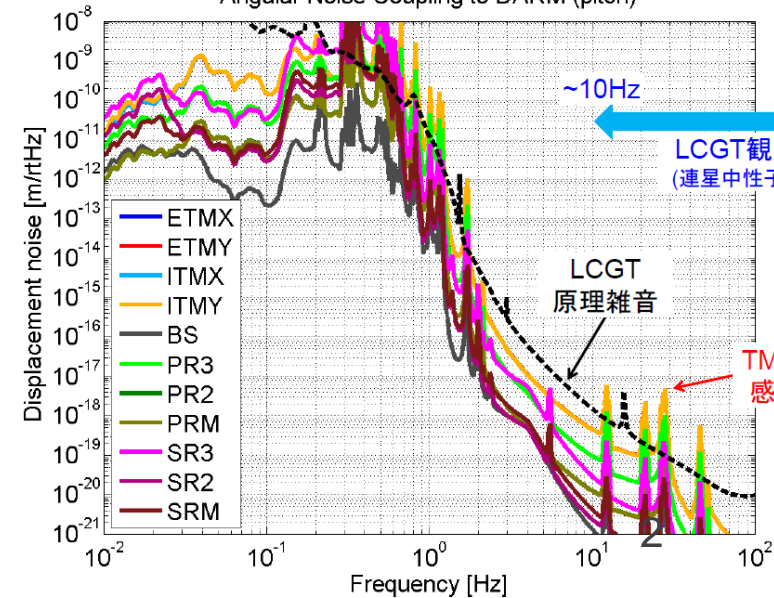
- Tsubono Group,  
Dept. of Physics, U. of Tokyo  
got master's in March 2012  
starting Ph D
- what I have been doing
  - DECIGO Pathfinder  
prototype FP experiment
  - KAGRA (LCGT)  
ASC simulation
  - anisotropy search in the  
speed of light  
(master's thesis)
  - lock 40m IFO

## DPF prototype FP



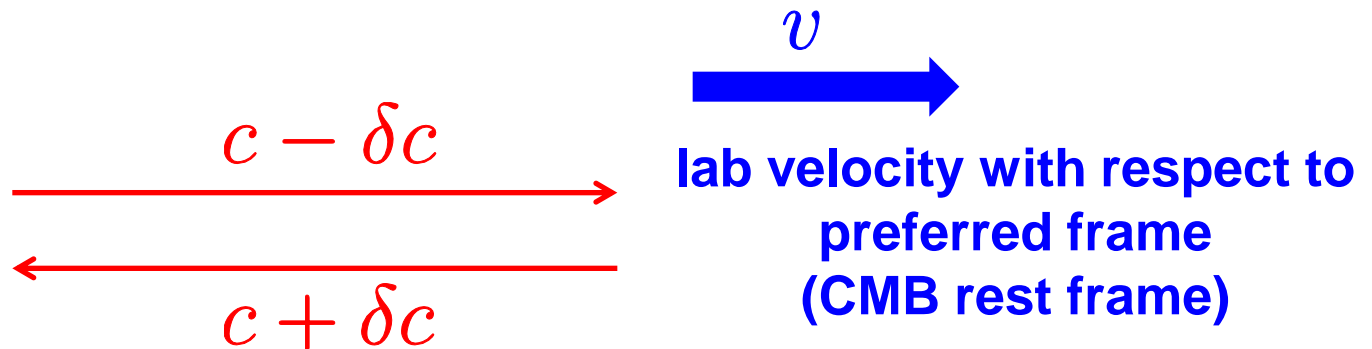
## KAGRA ASC

Angular Noise Coupling to DARM (pitch)



# Abstract

- tested Special Relativity(Lorentz invariance in photons) by testing isotropy in the **one-way** speed of light
- new idea: use asymmetric optical ring cavity
- got the **world's best limit** (more than x2 better)  
 $\hat{\alpha} = (-2.3 \pm 2.6) \times 10^{-10}$   
set upper limit on the anisotropy to a level of  $|\delta c/c| \lesssim 10^{-13}$



# Contents

1. Background
2. Experimental Principle
3. Experimental Setup
4. Data Analysis
5. Current Status and Summary

# 1. Background

# SR and Lorentz violation

- Special Relativity (1905)  
speed of light is constant
- Lorentz invariance in electrodynamics
- no one could find any violation
- but...

- quantum gravity theory suggests violation at some level

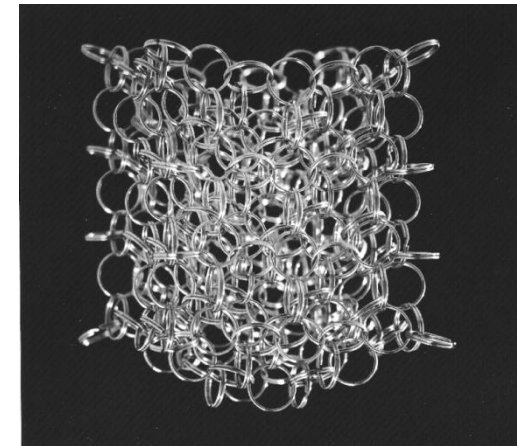
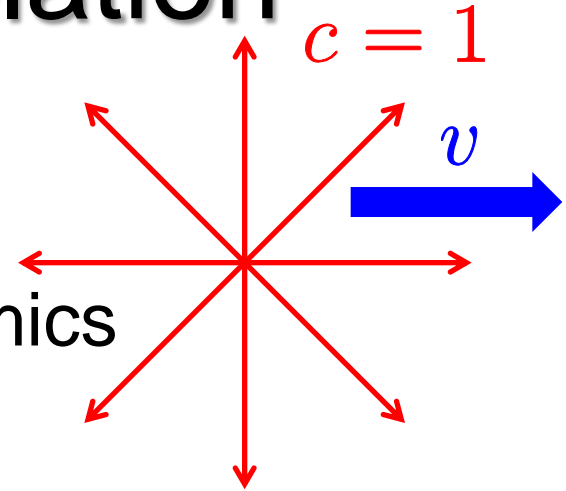
$$\text{e.g. } \delta c/c \sim 10^{-17}$$

D. Colladay and V. Alan Kostelecký: PRD 58 (1998) 116002

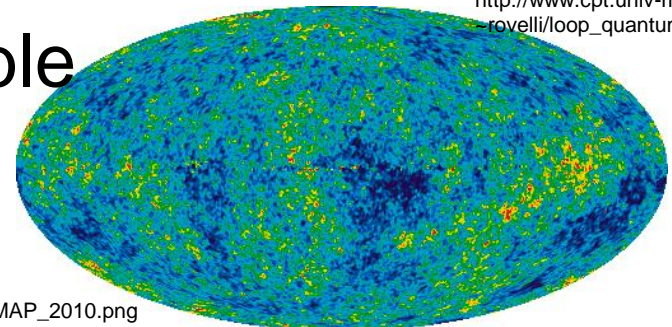
- anisotropy in CMB

CMB rest frame: possible preferred frame?

→ we have to test SR !



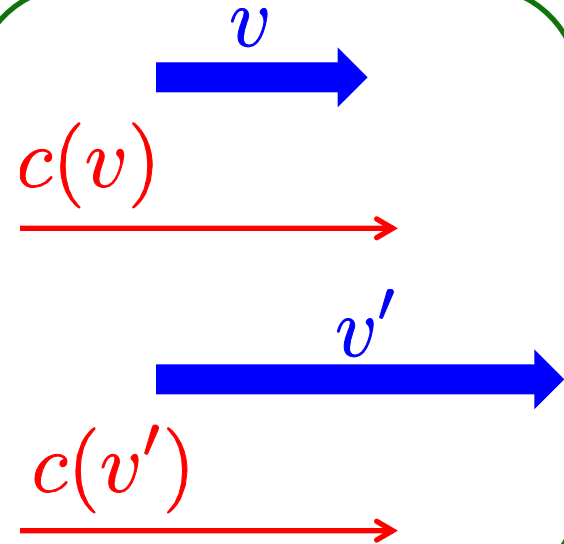
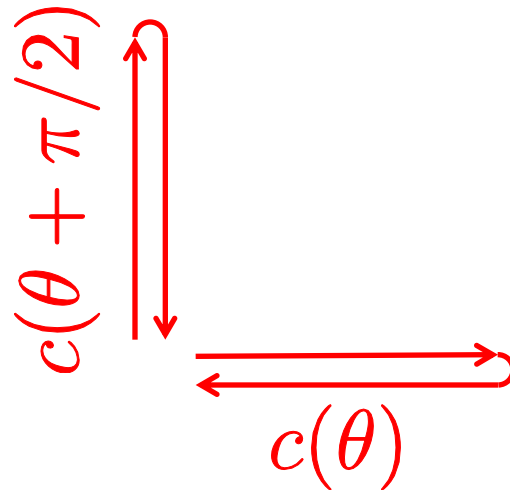
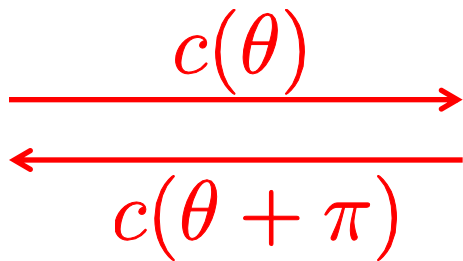
[http://www.cpt.univ-mrs.fr/~rovelli/loop\\_quantum\\_gravity.jpg](http://www.cpt.univ-mrs.fr/~rovelli/loop_quantum_gravity.jpg)



[http://en.wikipedia.org/wiki/File:WMAP\\_2010.png](http://en.wikipedia.org/wiki/File:WMAP_2010.png)

# Testing SR

- most traditional way to test SR
- constancy of the speed of light consists from
  - isotropy in the one-way speed of light
  - isotropy in the two-way speed of light
  - independence of the speed of light from the lab. velocity



# Test theory of SR: MS Theory

- test theory proposed by Mansouri & Sexl (1977)

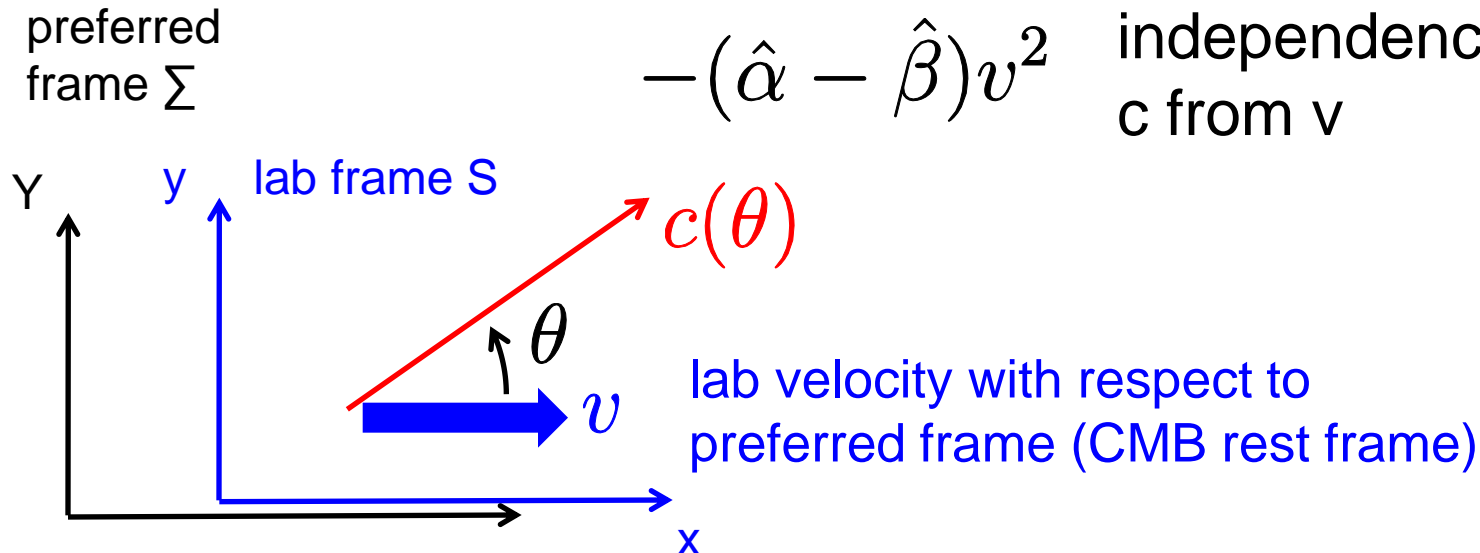
R. Mansouri and R. U. Sexl: Gen. Relativ. Grav. 8 (1977) 497/515/809

- speed of light in MS theory

$$c(\theta) = 1 - 2\hat{\alpha}v \cos \theta \quad \text{one-way anisotropy}$$

$$-(\hat{\beta} - \hat{\delta})v^2 \sin^2 \theta \quad \text{two-way anisotropy}$$

$$-(\hat{\alpha} - \hat{\beta})v^2 \quad \text{independence of } c \text{ from } v$$



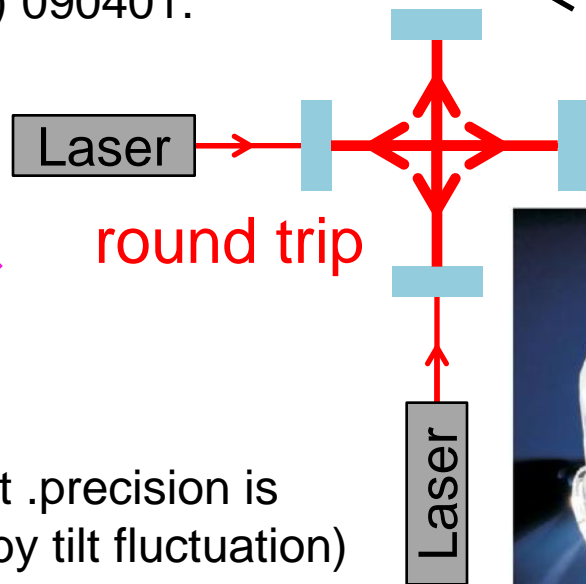
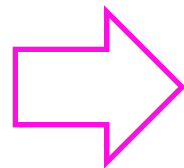
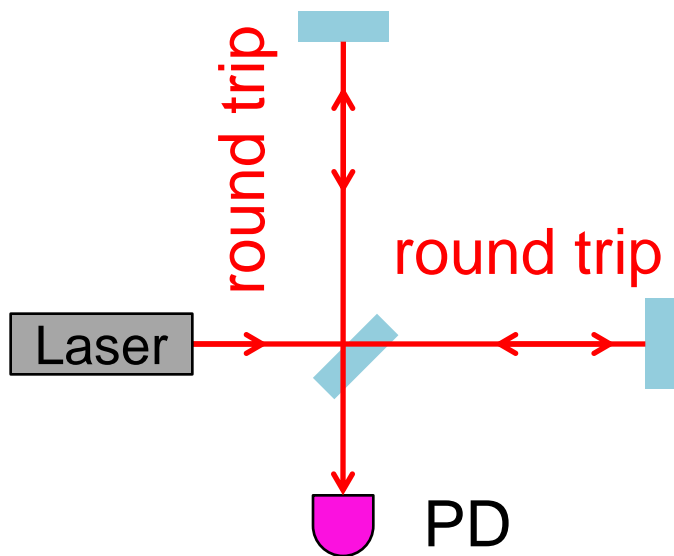


# Previous Test for Two-Way c

- Michelson-Morley experiment (1887)  
Michelson interferometer
- compare the resonant freqs of crossed FP in a single block(2009)

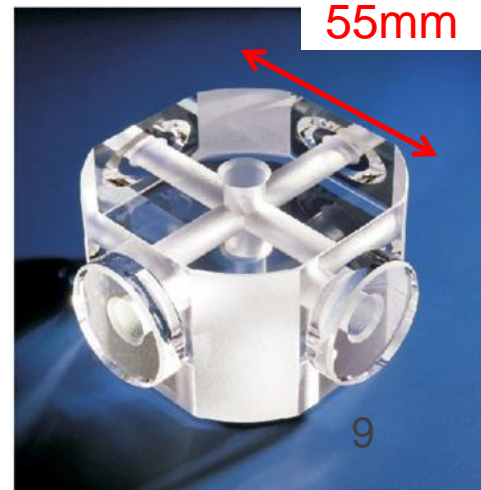
$$\hat{\beta} - \hat{\delta} = (-1.6 \pm 6 \pm 1.2) \times 10^{-12}$$

Ch. Eisele+: PRL **103** (2009) 090401.



$$|\delta c/c| \lesssim 10^{-17}$$

(Current precision is limited by tilt fluctuation)



S. Herrmann+: PRD 80 (2009) 105011.

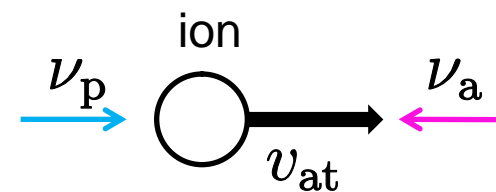
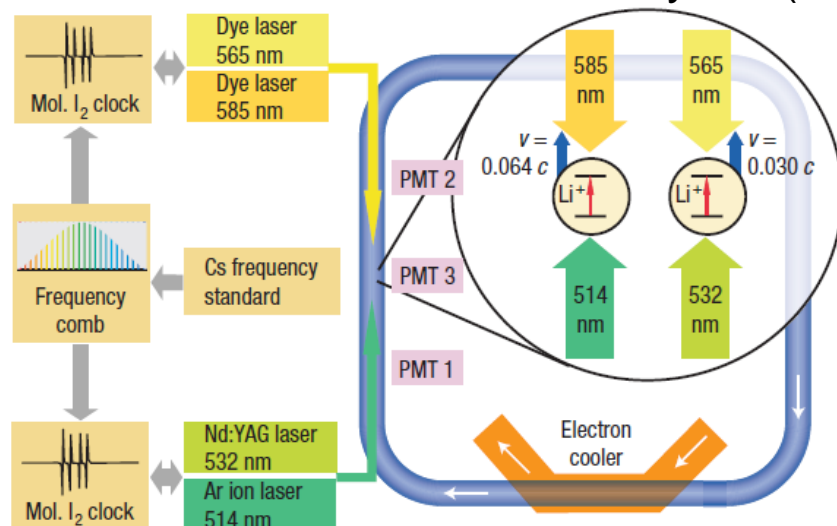
# Previous Test for One-Way c

- Ives-Stilwell experiment (1938)  
measure Doppler shifted resonant freq of ions
- most recent IS-type experiment (2007)

$$\hat{\alpha} = (-4.8 \pm 8.4) \times 10^{-8}$$

S. Reinhardt *et al.*: Nat. Phys. **3** (2007) 861.

$$|\delta c/c| \lesssim 10^{-10}$$



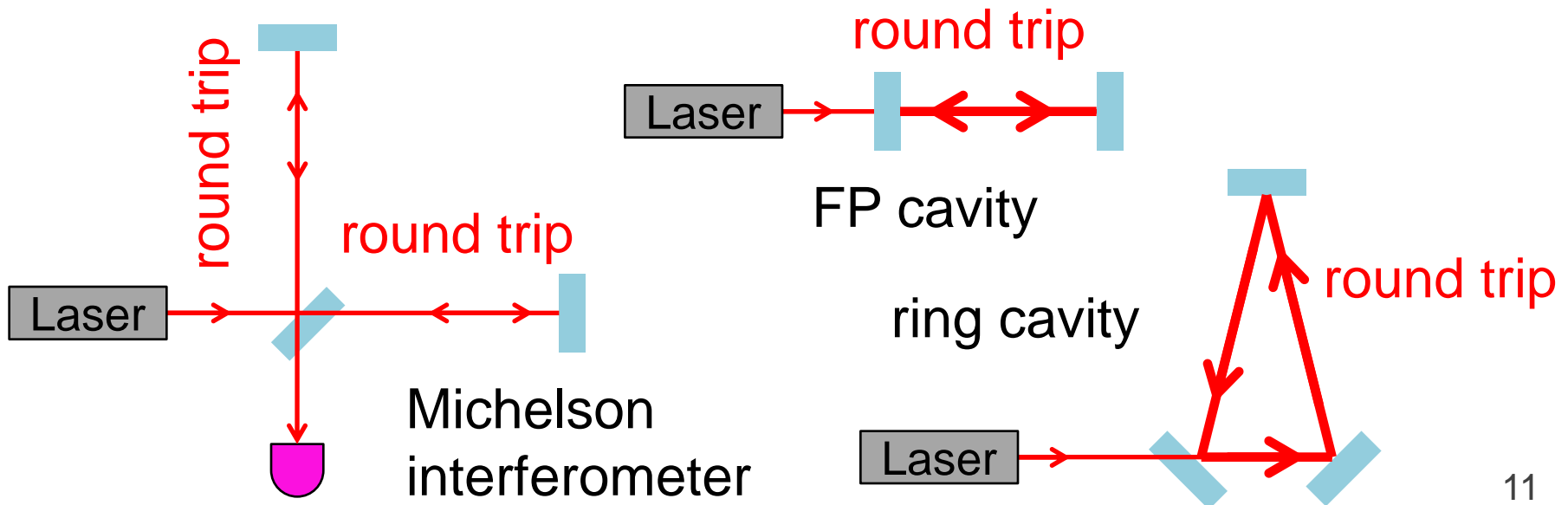
have to measure the absolute value of the resonant frequency

**Figure 1** Schematic diagram of the TSR.  $\text{Li}^+$  ions circulate in the 55-m-circumference ring. In the electron cooler, cold electrons are overlapped with the ions and provide cooling. The measurements at the two different velocities are carried out sequentially. In the experiment, the two lasers are coupled into the ring from the same side and are retro-reflected.

# Starting Point

- one-way test is 7-orders of magnitude less precise than two-way test!
- can't test one-way  $c$  using ordinary interferometers
- one-way anisotropy term cancels in a closed loop
$$c(\theta) = 1 - 2\hat{a}v \cos \theta + \mathcal{O}(v^2)$$

→ how can we deal with it?

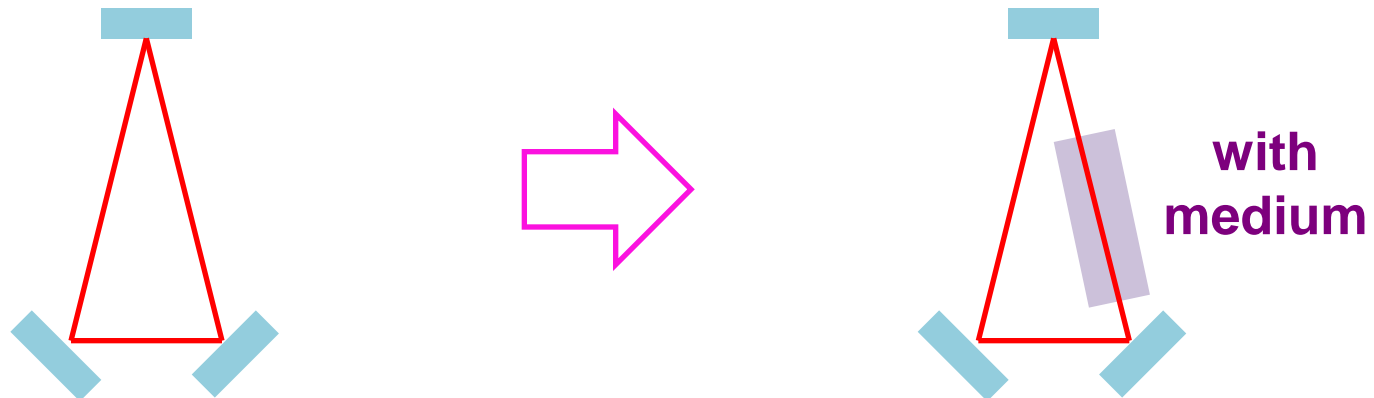


## 2. Experimental Principle

# Asymmetric Ring Cavity

- putting a medium in the optical path makes an asymmetry
  - ring cavity will be sensitive to the one-way anisotropy
- asymmetric Sagnac experiment was first done by Trimmer+ (1973) W. S. N. Trimmer+: PRD 8 (1973) 3321
- cavity type proposed by Exirifard (2010)

Q. Exirifard: arXiv:1010.2057.



# Resonant Frequencies

- one-way term remains because of asymmetry

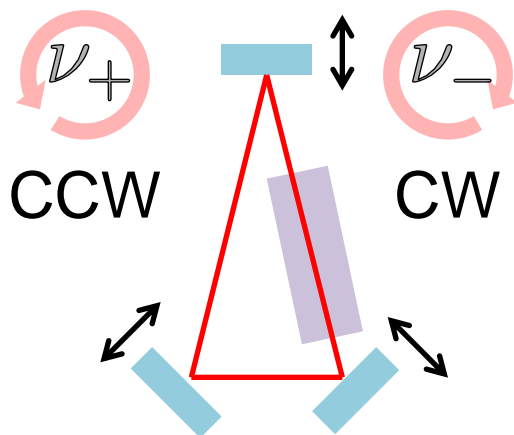
$$c(\theta) = 1 - 2\hat{\alpha}v \cos \theta + \mathcal{O}(v^2)$$

no anisotropy	$\nu_+ = \nu_0$ $\nu_- = \nu_0$	$\nu_+ = \nu$ $\nu_- = \nu$ <div style="border: 1px solid red; padding: 5px; display: inline-block; margin-top: 10px;">             freq. shift  <math>\propto \hat{\alpha}</math> </div>
anisotropy	$\nu_+ = \nu_0$ $\nu_- = \nu_0$	$\nu_+ = \nu - \delta\nu$ $\nu_- = \nu + \delta\nu$

# Counter Propagating Modes

- comparing resonant frequencies of counter propagating modes
  - **high CMRR** to cavity length change
  - no need for high vacuum
  - seismic isolation
  - temperature control (or cryogenic)
- first experiment done by Baynes+ (Oct 2011)

F. Baynes+: PRD 84 (Oct 2011) 0811021.

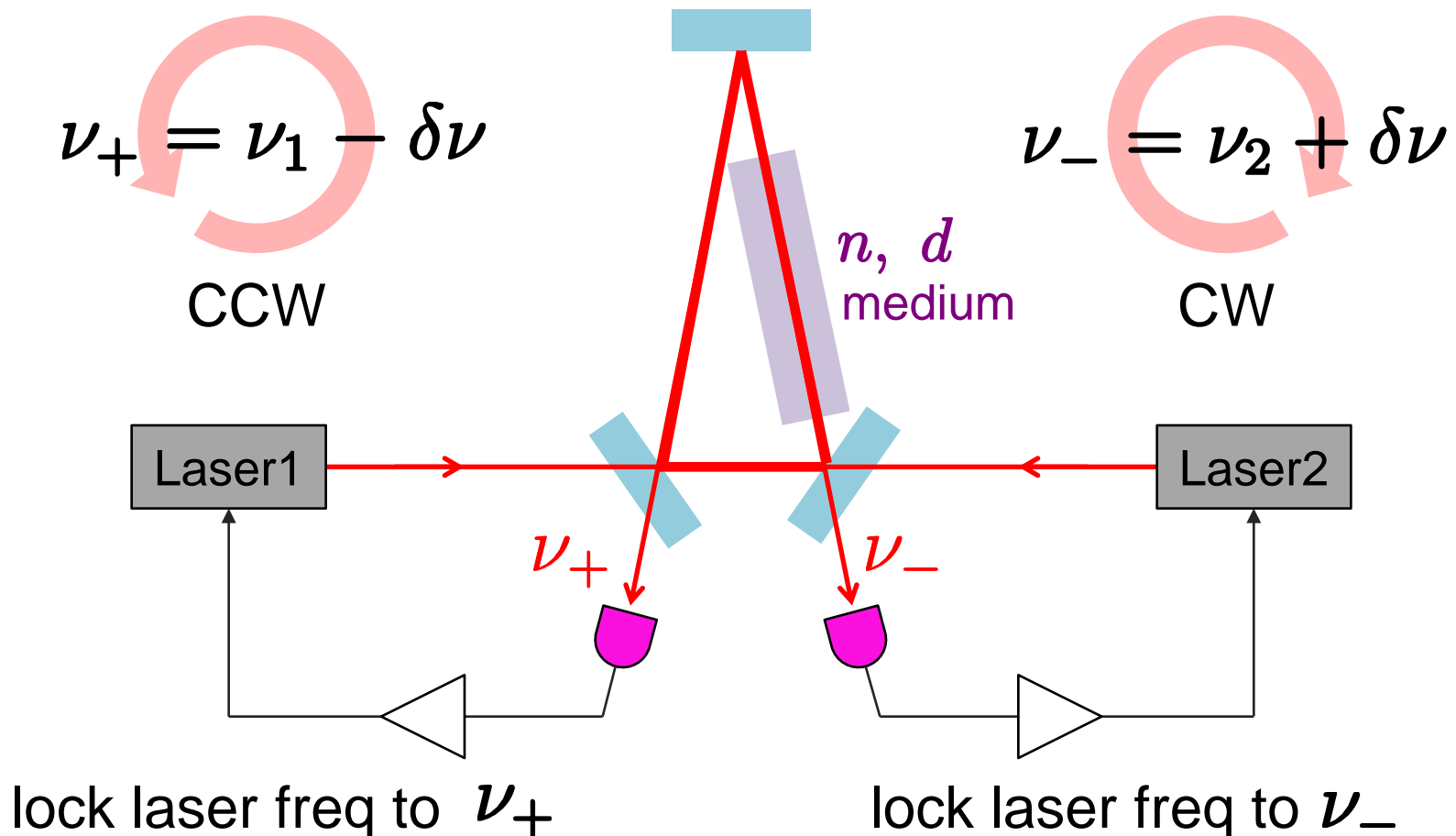


$$\nu_+ = \nu - \delta\nu$$

$$\nu_- = \nu + \delta\nu$$

# Optical Setup of Baynes+(2011)

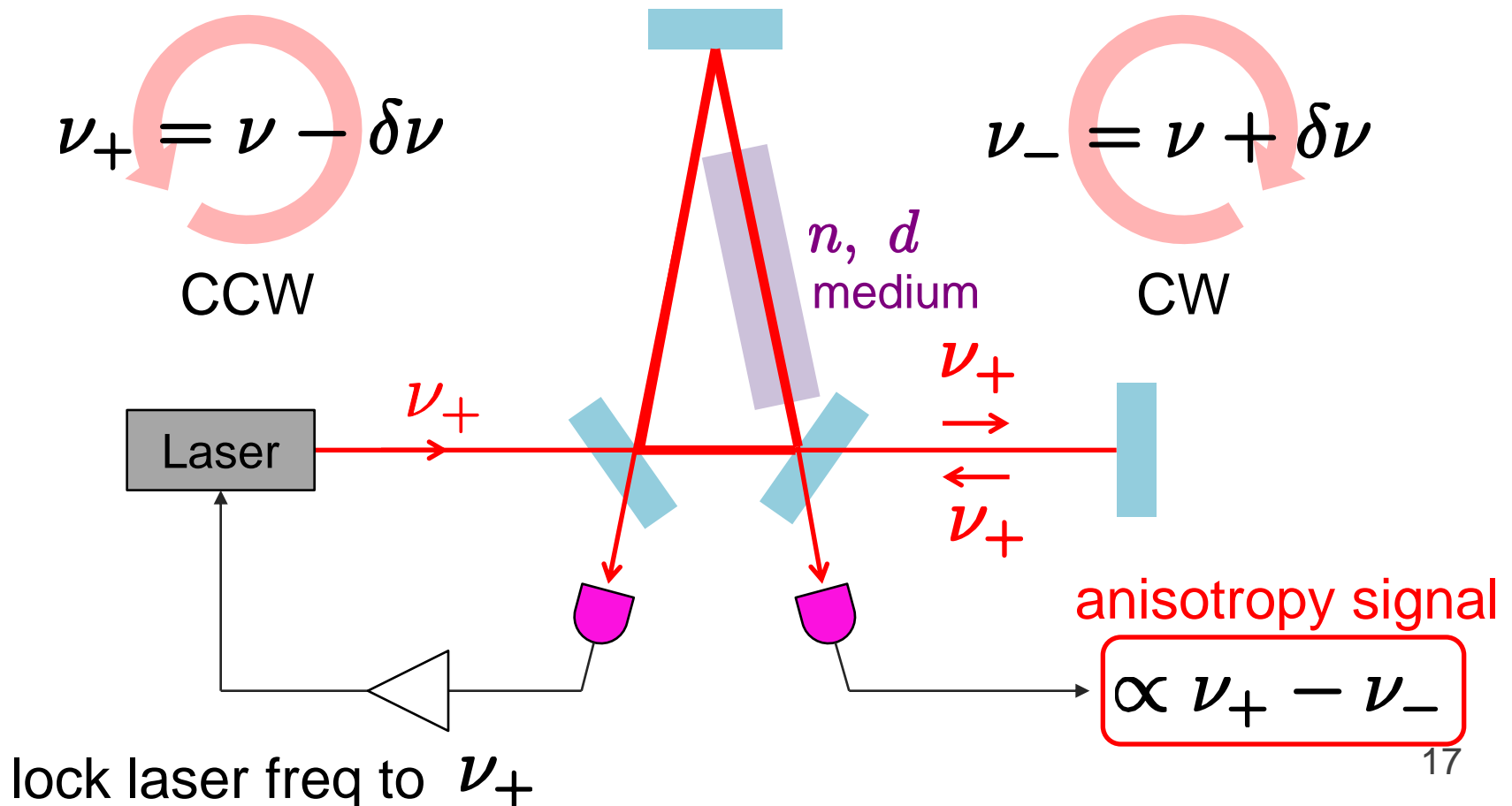
- lock freqs of two lasers to  $\nu_+$ ,  $\nu_-$
- have to shift two laser freqs to avoid the lock-in problem (not a null experiment)





# Our New Idea: Double-Pass

- double-pass makes **null measurement**
- only one beam; no need to care about lock-in



# Anisotropy Signal

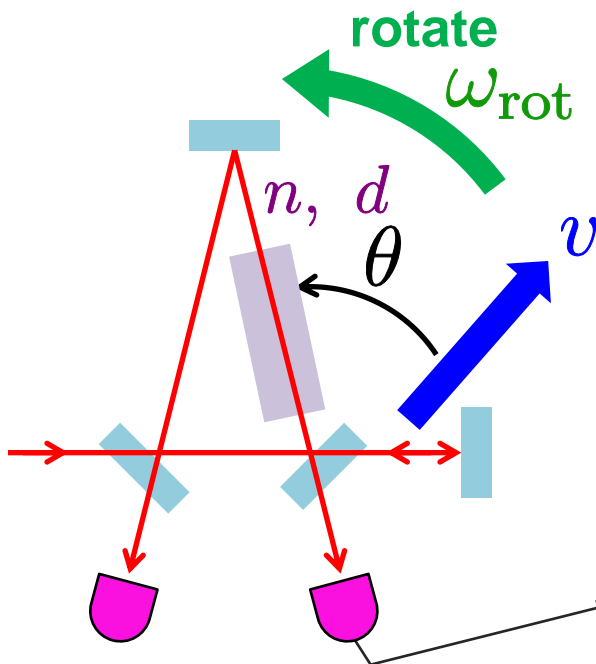
- $\delta\nu \equiv \nu_+ - \nu_-$

lab speed with respect to CMB  
 $v \simeq 10^{-3}$

$$\frac{\delta\nu}{\nu} = \frac{4(n-1)d}{L + (n-1)d} \hat{\alpha} v \cos \theta$$

round trip length  $\rightarrow$   $L + (n-1)d$

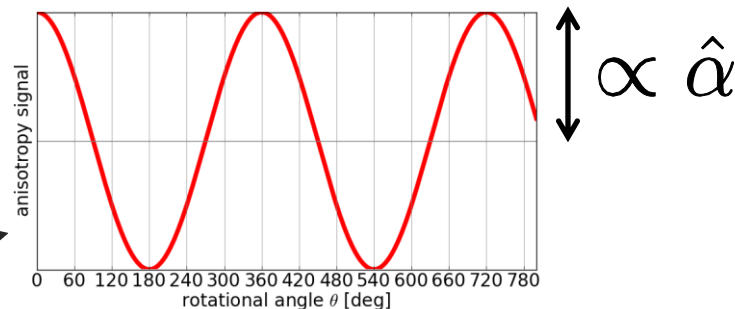
$\hat{\alpha}$   $\rightarrow$  rotate cavity to modulate



putting a medium is essential

larger n, bigger signal

$\rightarrow$  let's use silicon with 1550nm  
 (n=3.69)



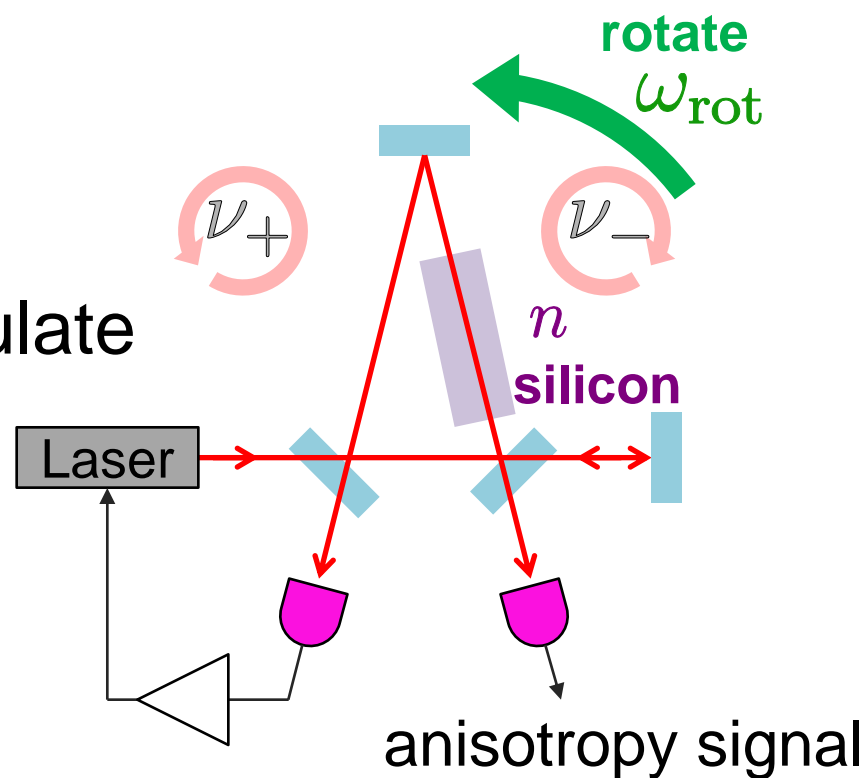
# Summary (first half)

- measure anisotropy in one-way speed of light using a ring cavity
  - silicon inside
  - compare counter-propagating resonant freqs

**high CMMR**

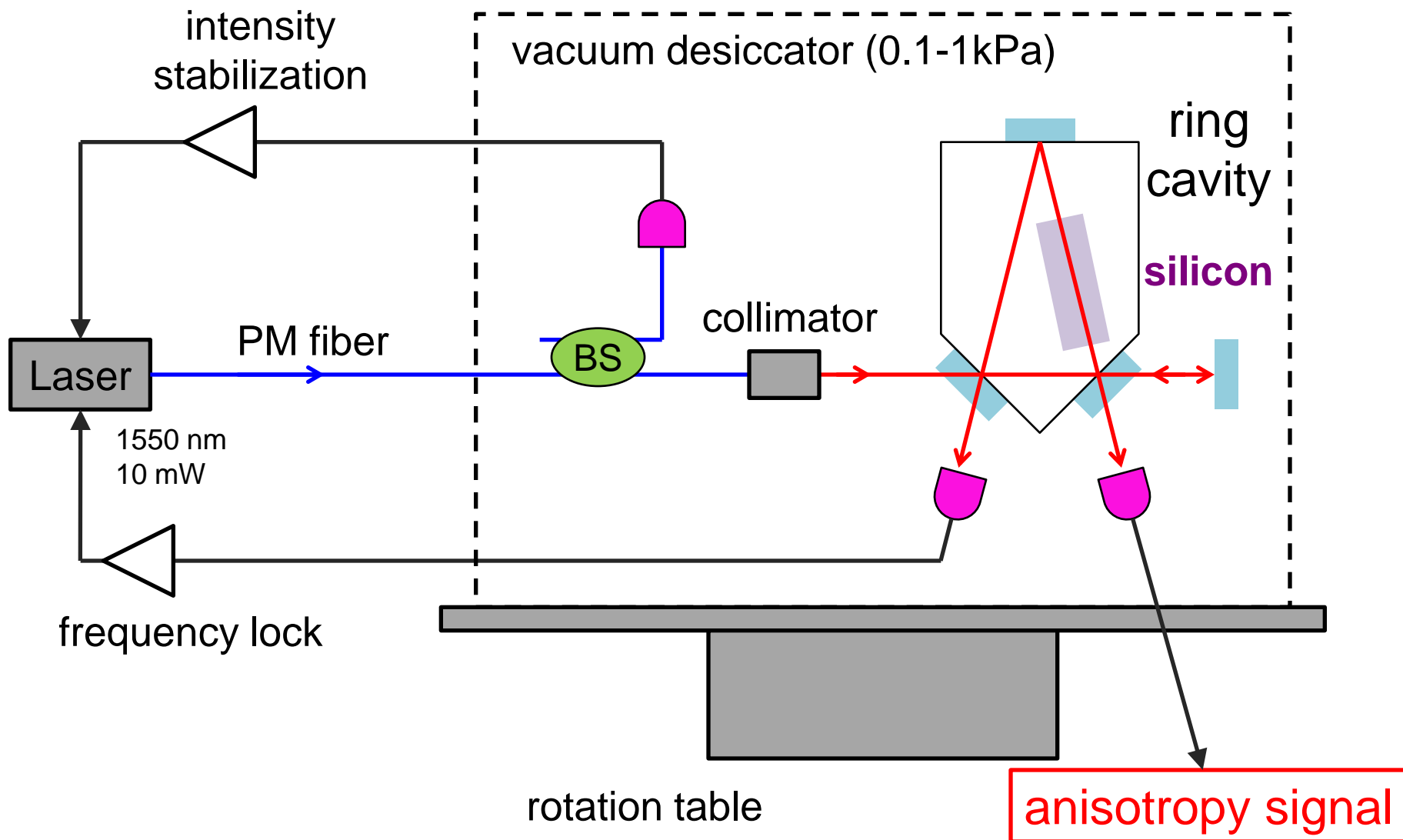
  - double pass

**null measurement**
- rotate the cavity to modulate anisotropy signal

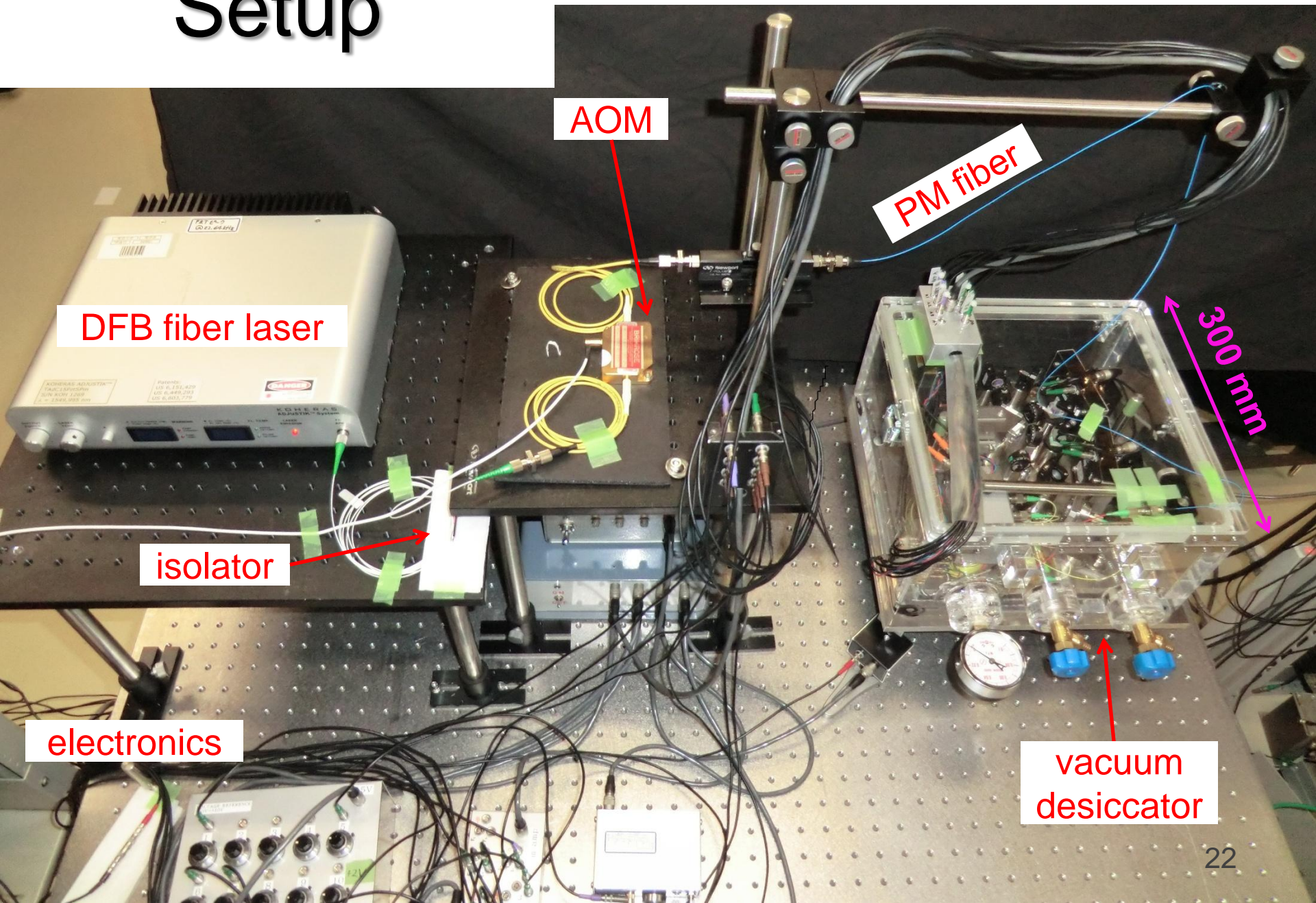


# 3. Experimental Setup

# Whole Setup



# Setup



DFB fiber laser

AOM

PM fiber

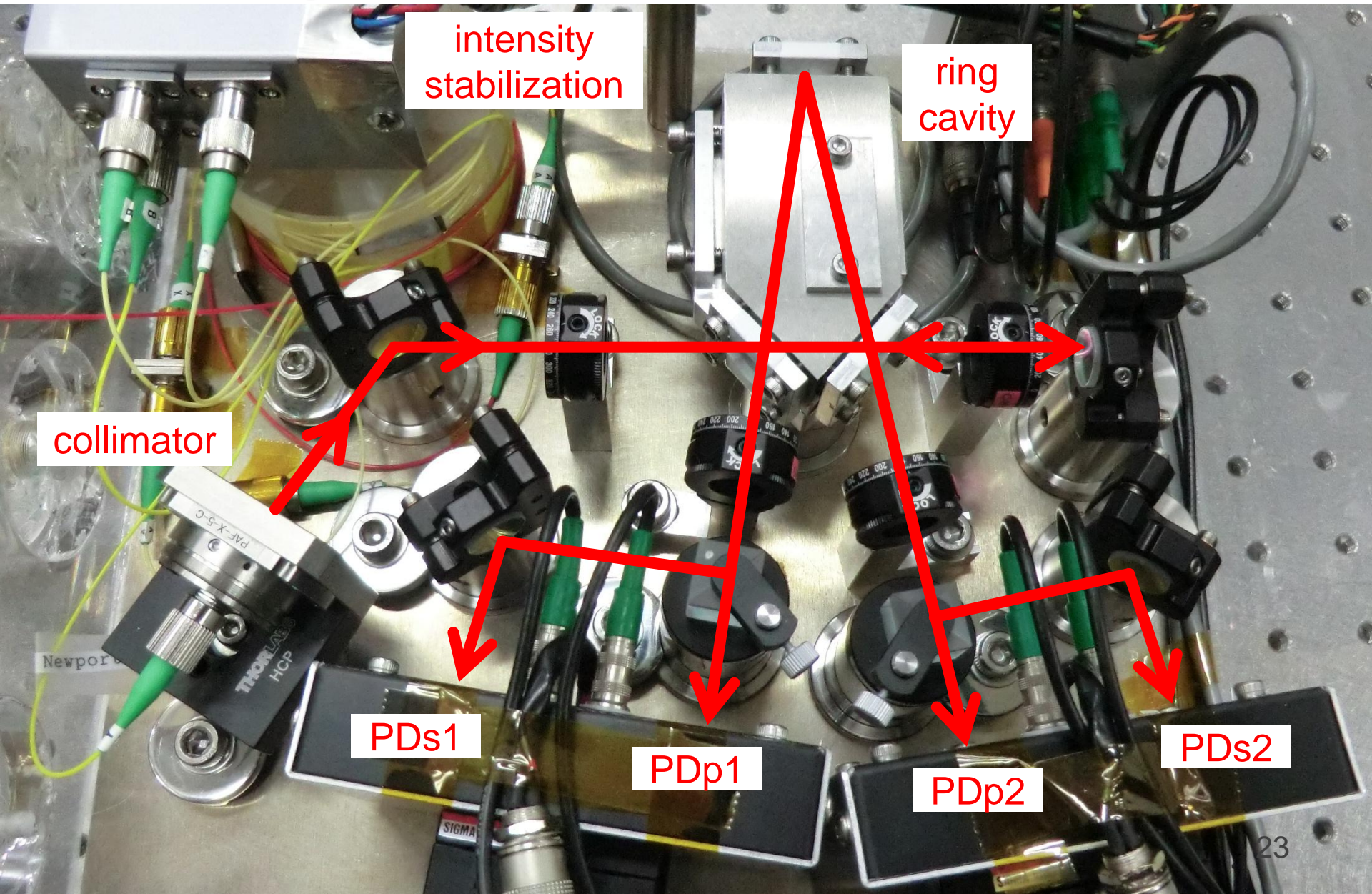
isolator

300 mm

electronics

vacuum desiccator

# Optics Inside Desiccator



intensity  
stabilization

ring  
cavity

collimator

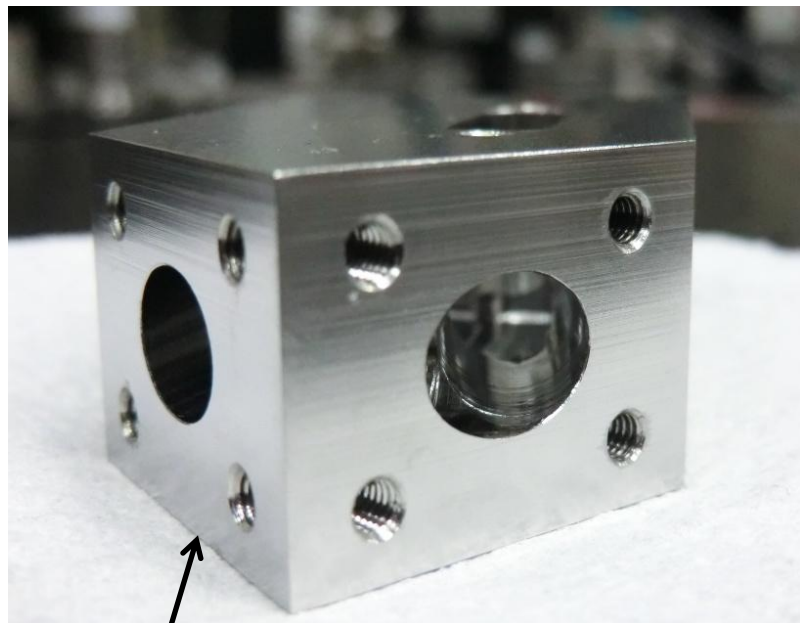
PDs1

PDp1

PDp2

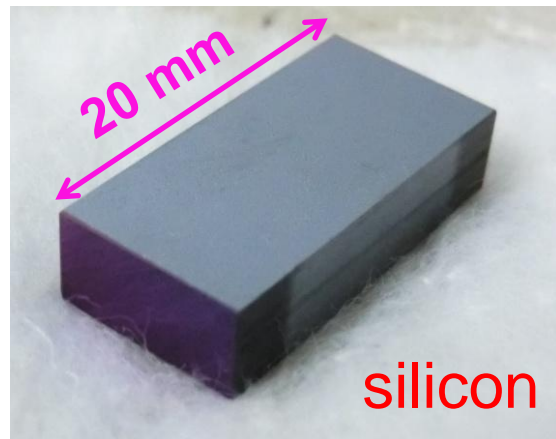
PDs2

# Ring Cavity

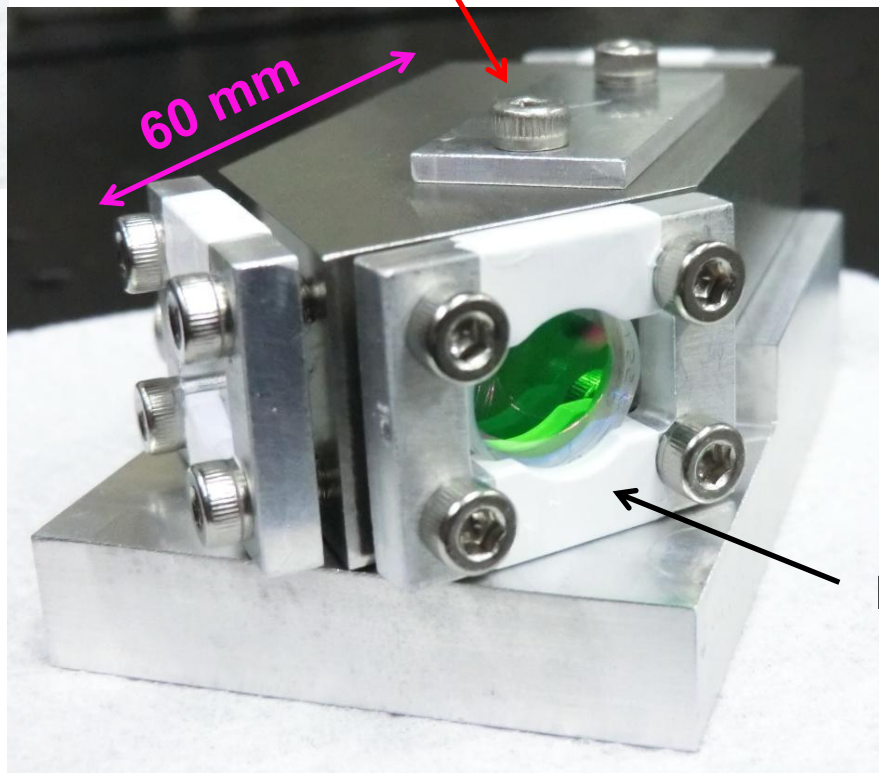


spacer made of Super Invar

ring cavity spec  
incident power:  $\sim 1$  mW  
finesse:  $\sim 125$   
round-trip length: 140 mm  
silicon length: 20 mm  
end mirror RoC: 200 mm



silicon inside

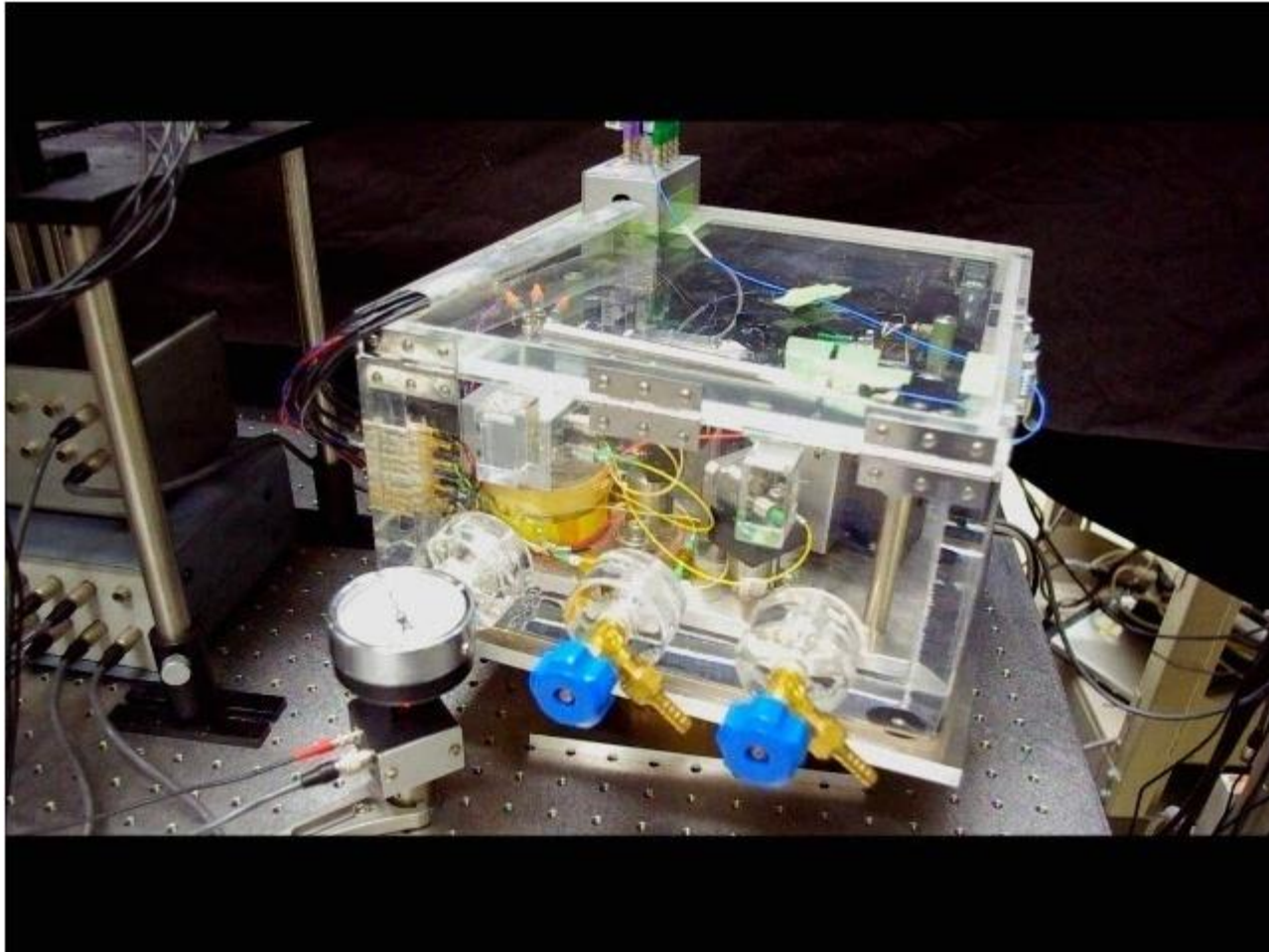


mirrors



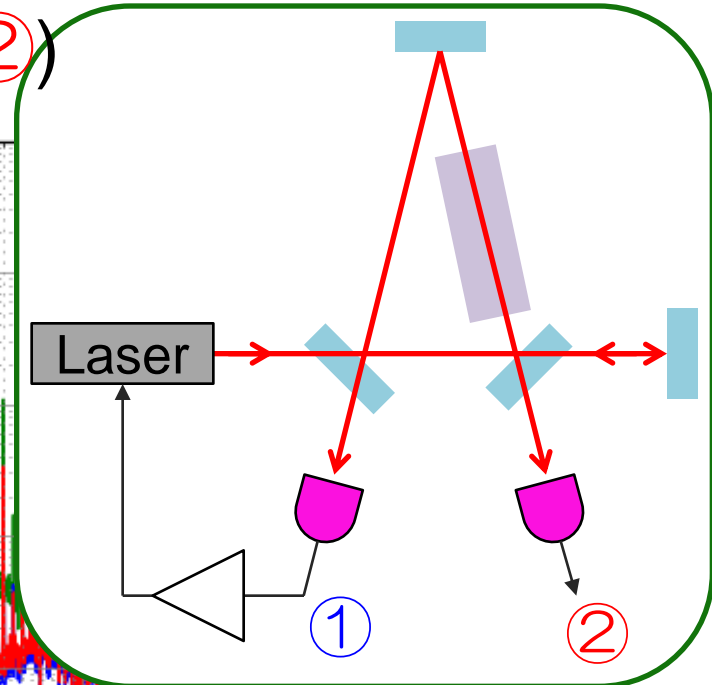
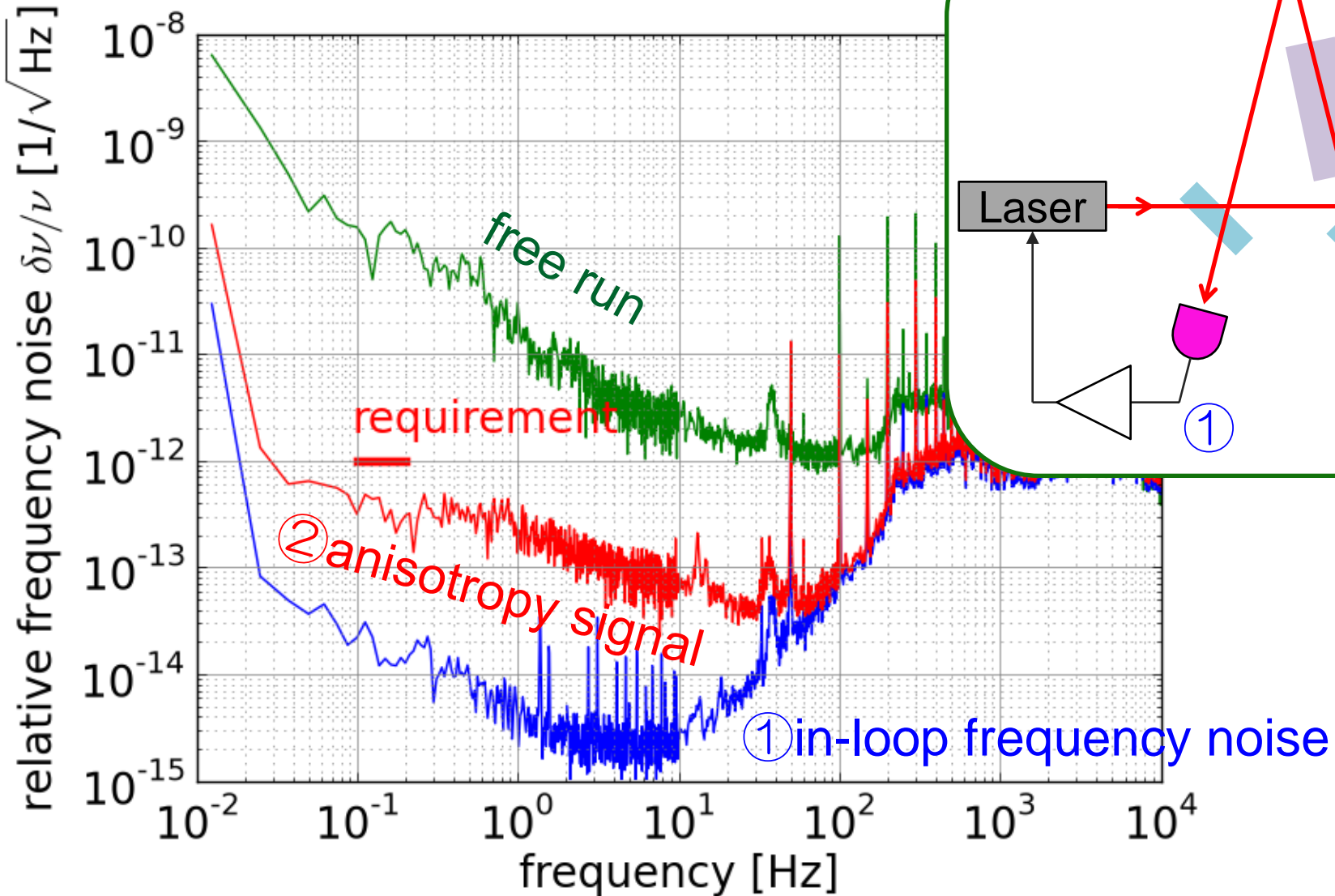
# It's Rotating

- movie



# Sensitivity

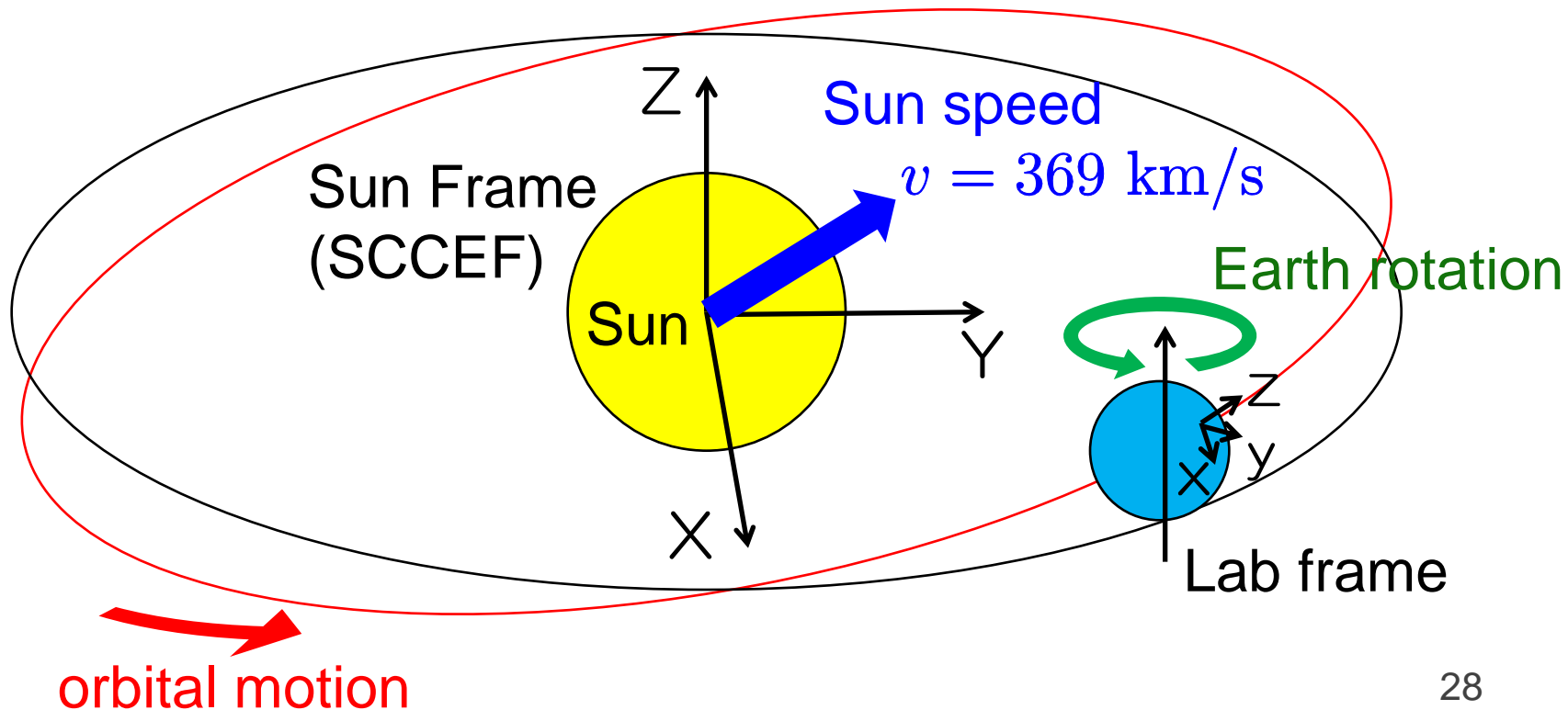
- below requirement (but ①  $\neq$  ②)



# 4. Data Analysis

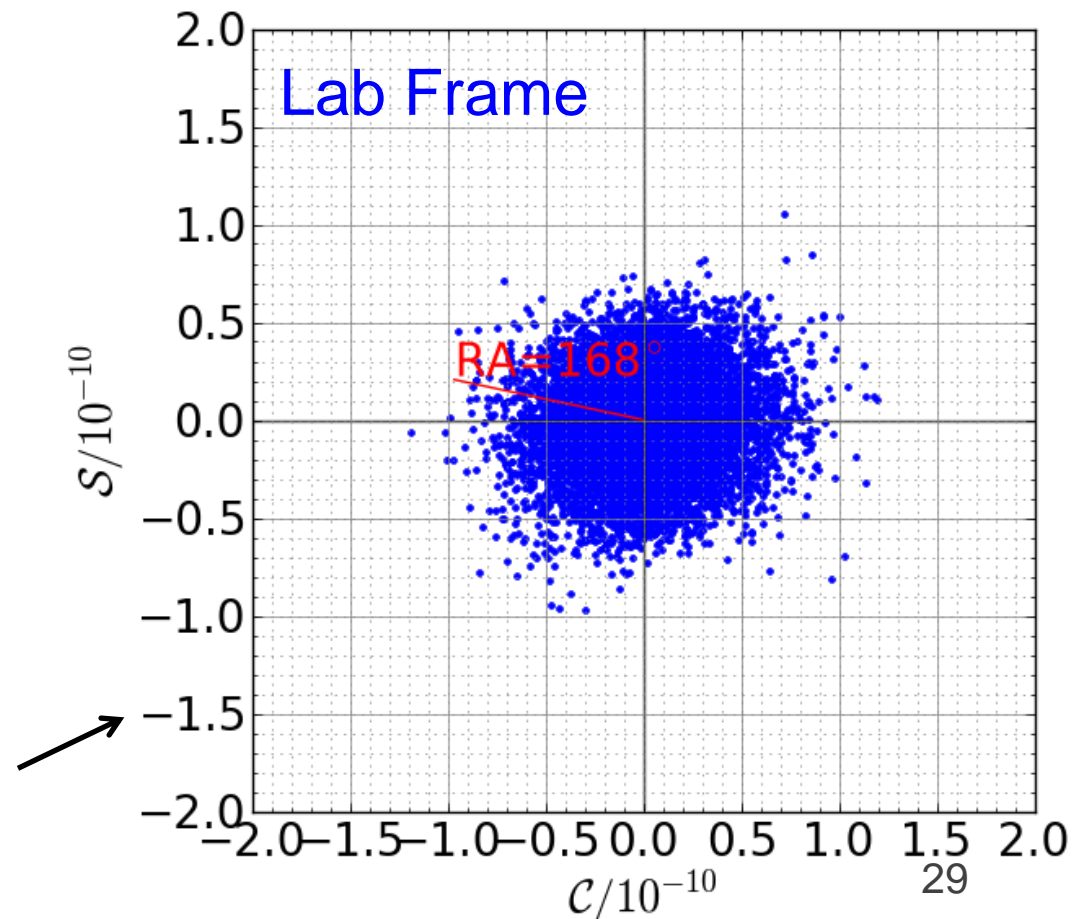
# Data Analysis Flow

- FFT the signal in rotation frequency (0.125 Hz)
- eliminate the effect of Earth rotation  
(convert Fourier amplitudes from Lab to Sun Frame)
- derive  $\hat{\alpha}$  for each cavity rotation



# Result of the Analysis

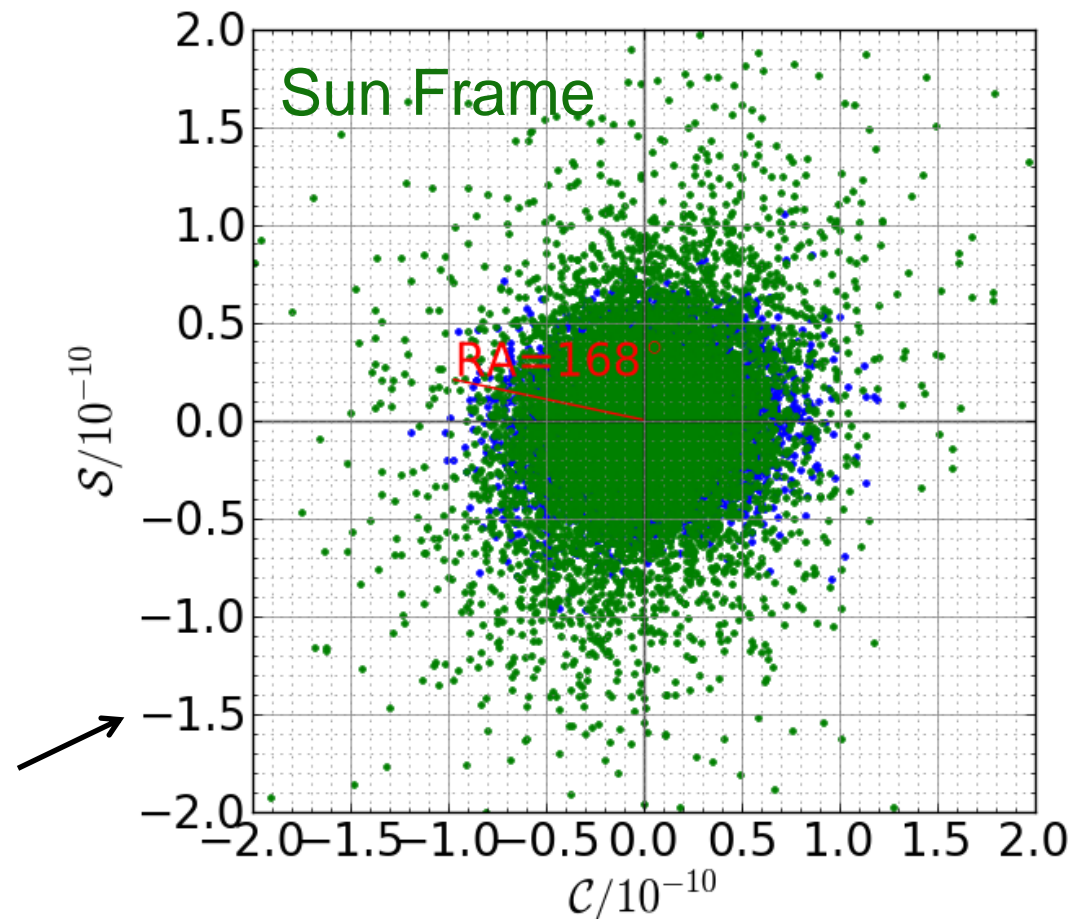
- ~26,000 rotation for 2 weeks in Nov 2011
- used quiet ~10,000 rotation for data analysis



10,000 Fourier complex  
amplitudes in Lab Frame

# Result of the Analysis

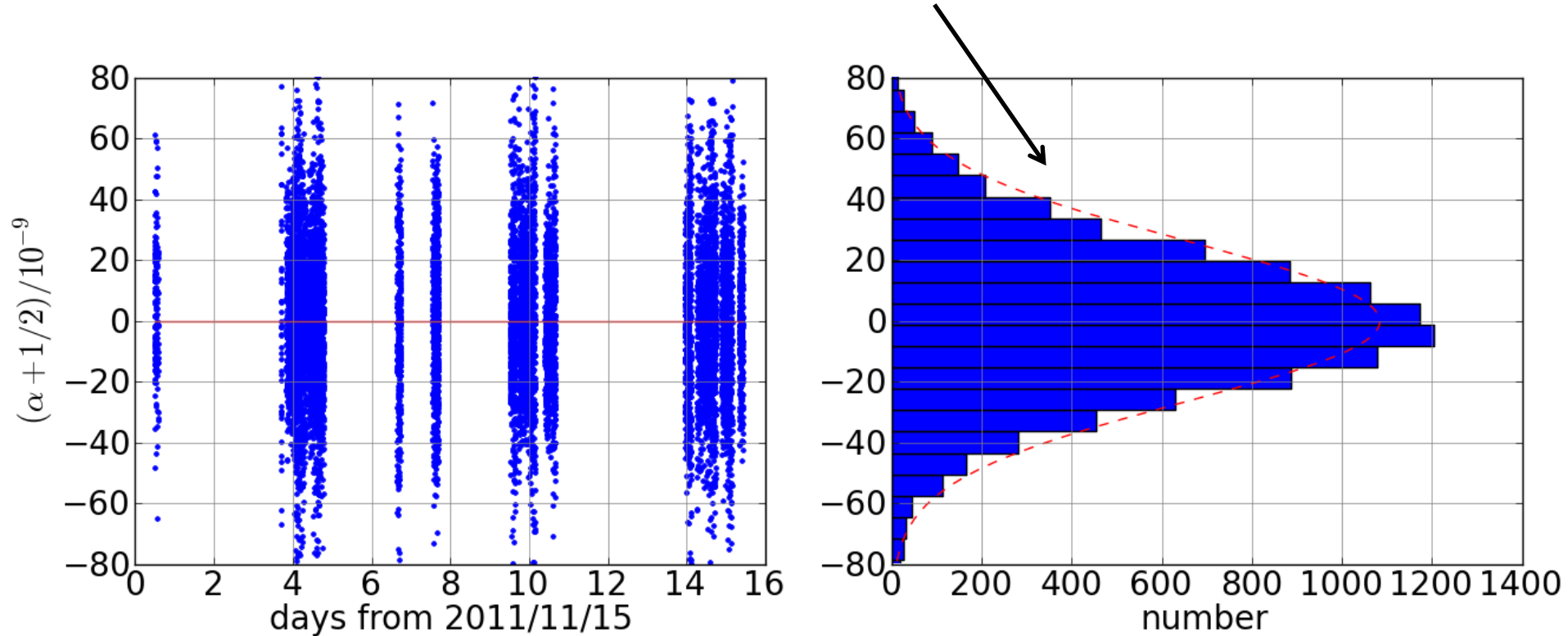
- ~26,000 rotation for 2 weeks in Nov 2011
- used quiet ~10,000 rotation for data analysis



10,000 Fourier complex  
amplitudes in Sun Frame

# Upper Limit on the Anisotropy

- histogram of  $\hat{\alpha}$  from our data



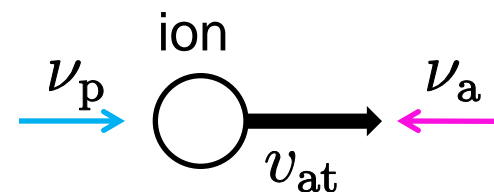
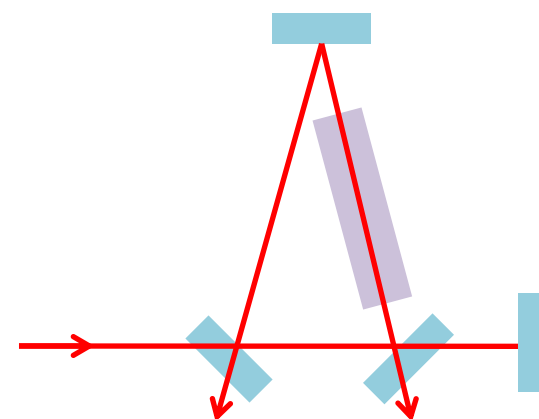
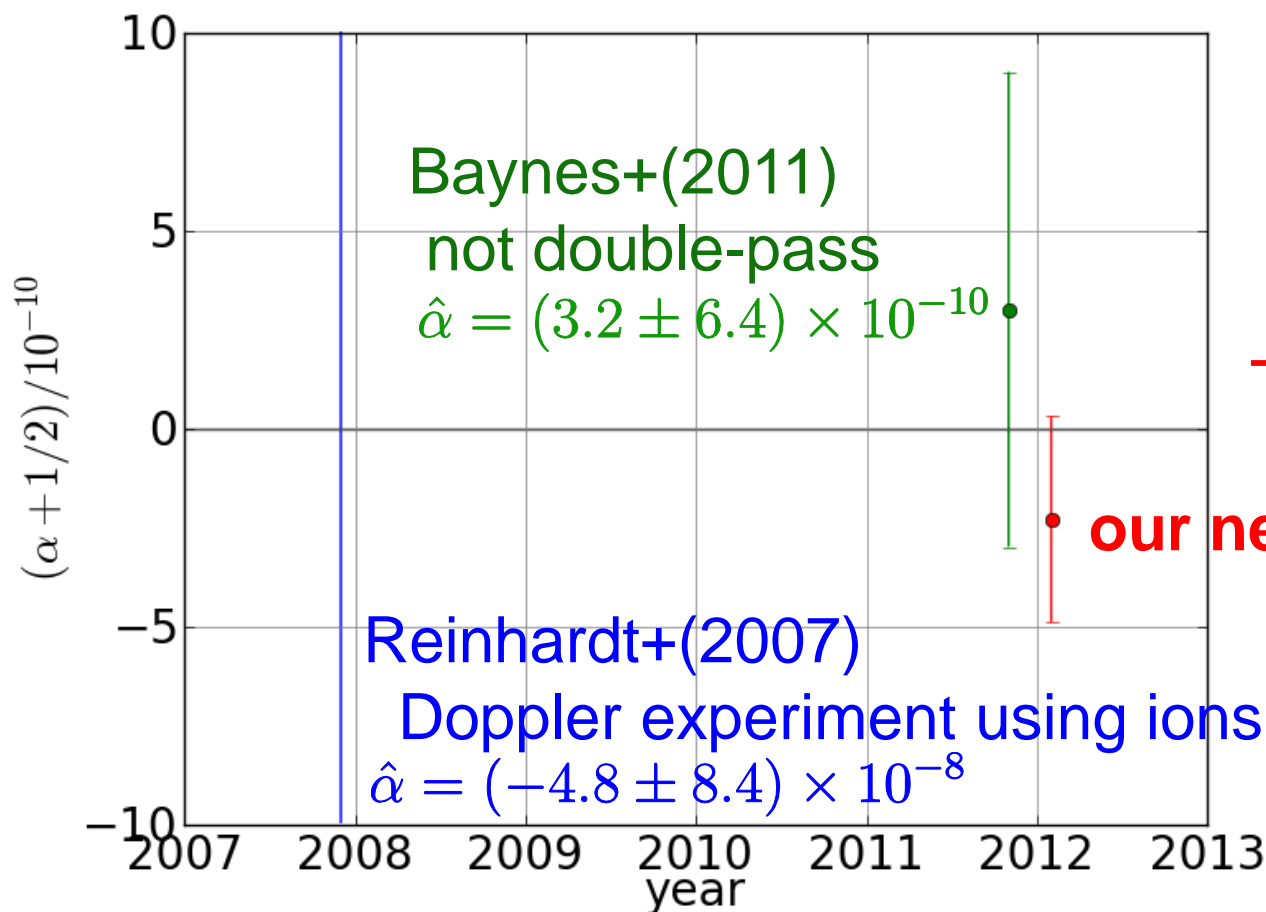
$$\rightarrow \hat{\alpha} = (-2.3 \pm 2.6) \times 10^{-10}$$

statistical error ( $1\sigma$ )

# Comparison with Previous Exp.

- more than factor of 2 better

$$\hat{\alpha} = (-2.3 \pm 2.6) \times 10^{-10}$$

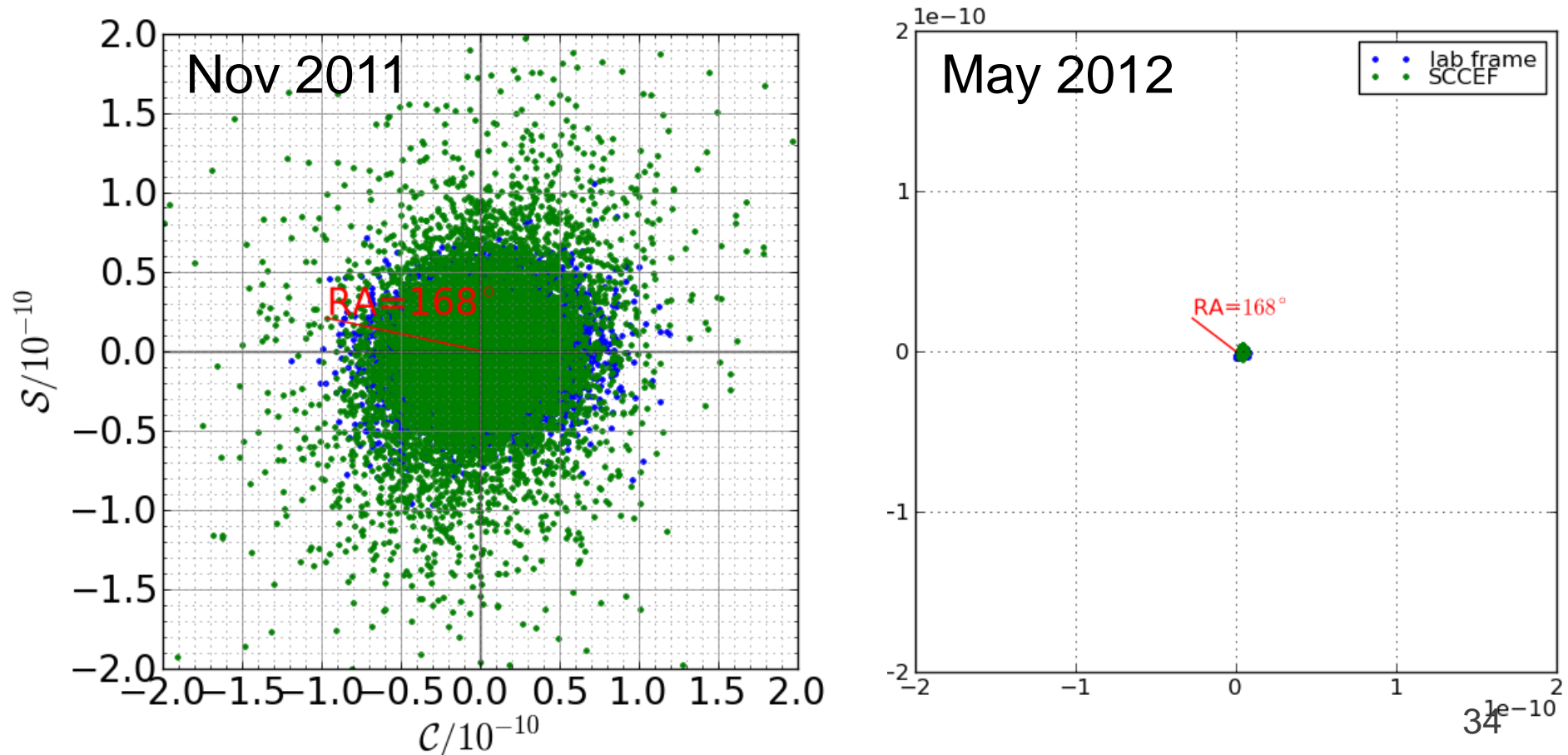




# 5. Current Status and Summary

# Current Status

- reduced noise! (ADC noise was the limiting source...)
- now we have systematic errors > statistic error  
lab light, polarization, **tilt of optical table**



# Summary

- tested SR (Lorentz invariance in photons) by testing isotropy of one-way speed of light
- developed new setup for the anisotropy search
  - silicon inside ring cavity
  - double-pass configuration
- took anisotropy signal data for  $\sim 10,000$  rotations (1.2 days)
- analyzed data, and got the world's best limit
$$\hat{\alpha} = (-2.3 \pm 2.6) \times 10^{-10}$$
- already reduced noise by an order of magnitude
- working on making it insensitive to tilt