## Ando Group Seminar

# Masaki Ando's Travels in these Two Weeks Chinese Space GW Mission and VIRGO

# Masaki Ando (Univ. of Tokyo / NAOJ)

# Ando's Travel Schedule

May 20 (Travel) 21  $\Lambda$ KIW3: 3<sup>rd</sup> KAGRA int. workshop (Taipei, Taiwan) 22 AIW2: 2<sup>nd</sup> ASTROD int. workshop (Shinchu, Taiwan)  $\left( \right)$ 23 24 Visit to NSPO (Hsinchu) 25<sup>(Tr</sup>和<sup>el)</sup> <u>ISGW2017</u>: International Symposium on Gravitational Waves (Beijing, China) 26 (Travel) **U-Tokyo Guidance** 27 28 (Travel) 29 VIRGO STAC (Scientific and Technical 30 Advisory Committee) (Pisa, Italy) 31 June (Travel) 2 U-Tokyo Open Public lecture 3

# Chinese Space GW Mission

# **Chinese GW Mission**

• Just after the LIGO's announcement of the first discovery in Feb. 2016, China decided to launch space GW mission.

#### Nature 531, 150 (March 2016)

#### NEWS IN FOCUS

## **Chinese gravitational-wave** hunt hits crunch time

The pressure is on to choose between several proposals for space-based detectors.

#### BY DAVID CYRANOSKI

n the wake of last month's historic detection of gravitational waves by a US-led collaboration, a range of Chinese proposals to take studies of these ripples in space-time to the next level are attracting fresh attention.

The suggestions, from two separate teams, are for space-based observatories that would pick up a wider range of gravitational radiation than ground-based observatories can. The most ambitious plan could give China an edge over the leading European proposal to detect gravitational waves from space, but whether a single country can achieve that on its own is unclear. Also under consideration are a possible collaboration between Chinese researchers and the European effort, and a cheaper Chinese plan. Although an Earth-based detector - the US Advanced Laser Interferometer Gravita-

tional-Wave Observatory (LIGO) - was the first to confirm a prediction made by Albert Einstein a century ago, launching the field of

Chinese researchers have proposed several ways to detect gravitational wayes in space

CHINA'S CHOICES

The most ambitious proposal uses three spacecraft in a triangle that

gravitational waves from a range of objects, like Europe's eLISA

proposal. The spacecraft are farther part than in eLISA, giving Taiji

TianQin spacecraft ~150.000 km apart

150 | NATURE | VOL 531 | 10 MARCH 2016

orbits the Sun and detects

TALJI



can be achieved only in space, where spacecraft equipped with signals

ISA spacecraft

Taiji spacecraft

3 million km apar

gravitational-wave astronomy, such detectors ultimate', is to create a more ambitious version can pick up only limited frequencies. Advanced of the leading proposal for the European pro ject, which is called eLISA (Evolved Laser LIGO compares laser light beamed along two perpendicular detector arms to reveal whether Interferometer Space Antenna). one beam has been compressed or stretched by gravitational waves gle of three spacecraft in orbit around the Each LIGO arm measures 4 kilometres, Sun, which bounce lasers between each other

but picking up the frequencies that are

richest in gravitational waves requires distances of hundreds of thousands of kilometres or more. This

lasers can be positioned at these distances. Space-based detectors also avoid fluctuations in Earth's gravitational field, which can obscure

A cheaper proposal puts three craft in orbit around Earth, and

much closer to each other than in Taiji. This would target the gravitational waves emitted by HM Cancri, a pair of white

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With such considerations in mind, the European Space Agency (ESA) is pursuing a spacebased gravitational-wave detector. One of the Chinese proposals, Taiji, meaning 'supreme

2033, slipping in a year ahead of eLISA's current schedule. "If Taiji produces a Chinese version of eLISA, then it will bring China to the frontier," says Yanbei Chen, a gravitational wave physicist at the California Institute of Technology in Pasadena, who works on LIGO. Gerhard Heinzel, an eLISA physicist also at the Max Planck Institute in Hanover, cautions against a single country going it alone on such

a large project. It "is definitely too big - mainly in terms of cost but also resources in terms of scientists and experts in the presence of competing science projects", he says.

Like eLISA, Taiji would consist of a trian-

(see 'China's choices'). The distance between

eLISA's components is still under discussion.

but current plans suggest it could be 2 million

kilometres, says eLISA member Karsten

Danzmann of the Max Planck Institute for

Gravitational Physics in Hanover, Germany.

Taiji's spacecraft would be separated by 3 mil-

lion kilometres, giving the detector access to

different frequencies. Taiji would launch in

Taiji project leader Wu Yue-Liang, a particle physicist at the Chinese Academy of Sciences' Institute of Theoretical Physics in Beijing, estimates that the project will cost 14 billion yuan (US\$2 billion), roughly twice as much as ESA is budgeting for its gravitational-wave detector.

#### SECOND STRING

A second Chinese proposal, led by Luo Jun, a physicist at the Sun Yat-Sen University campus in Zhuhai, would lower the bar in terms of cost and resources. Called TianOin, a name that refers to the metaphor of nature playing a stringed instrument (a zither) in space, the project has three satellites that orbit Earth at a distance of about 150,000 kilometres from each other. It would cost 2 billion vuan, says Luo.

TianOin would be more limited than Taiji in terms of what it could detect: rather than acting as an observatory for the waves emitted by myriad objects including black holes and neutron stars, it would mainly target a particular pair of orbiting white dwarf stars, called HM Cancri. TianQin's simplicity makes it cheaper and

# **Chinese GW Missions**

- Taiji (太極)
   \* Slightly longer
   than LISA
- \* Heliocentric orbit
- \* Proposed by Chinese Academy of Science

#### CHINA'S CHOICES

Chinese researchers have proposed several ways to detect gravitational waves in space.

Earth

#### TAIJI

The most ambitious proposal uses three spacecraft in a triangle that orbits the Sun and detects gravitational waves from a range of objects, like Europe's eLISA proposal. The spacecraft are farther apart than in eLISA, giving Taiji access to different frequencies.

Sun



・TianQin (天琴)

- \* ~10 times shorter
- \* Geocentric orbit
- \* Proposed by
   Sun Yat-Sen University



#### TIANQIN

eLISA spacecraft

~2 million km apart

A cheaper proposal puts three craft in orbit around Earth, and much closer to each other than in Taiji. This would target the gravitational waves emitted by HM Cancri, a pair of white dwarf stars.

Earth's orbit

# KIW3 and AIW2

# KIW3 and AIW2

ASTROD Int. Workshop at Hsinchu (National Tsing Hua Univ.) \* 1 day, ~20 participants \* LPF/LISA, DECIGO, TianQin, ASTROD \* Visit to NSPO in the next day

#### KAGRA Int. Workshop at Taipei

(NTU: National Taiwan Univ.)

- \* Two days
- \* KAGRA reports, Status reports (LIGO, VIRGO, KAGRA), KAGRA future plans, and space missions (LPF/LISA, DECIGO, TianQin, ASTROD)



by Google Map

# **AIW2:** The 2nd ASTROD Int. Workshop



#### 第二屆雷射天文動力學專題討論會 2nd ASTROD International Workshop (AIW2)

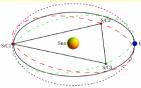
620 Phys. Bldg., National Tsing Hua Univ., Hsinchu • May 23, 2017

**Topic: Gravitational Wave (GW) Detection in Space** 

All the present active space GW proposals - New LISA, DECIGO, TAIJI, TIANQIN and ASTROD-GW will be discussed

Open to all the scientists of various fields







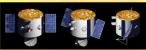
Talks and Lecturers

- Martin Hewitson (Max Planck I.) LISA Pathfinder: Experiment results LISA: A GW Observatory in Space
- Hsien-Chi Yeh (Sun Yat-sen U.) TIANQIN GW mission and key technologies
- Masaki Ando (Tokyo U.) Science and Design of DECIGO and B-DECIGO
- Wei-Tou Ni (NTHU) ASTROD-GW
- An-Ming Wu (NSPO) Deployment for Various Gravitational Wave Missions
- Gang Wang (INFN) Orbit design and TDI simulation for LISA, TAIJI and others

Organizing Committee Ling-Wei Luo (National Tsing Hua Univ.), Wei-Tou Ni (National Tsing Hua Univ.), Sheau-shi Pan (Industrial Technology Research Institute), An-Ming Wu (National Space Organization), Hwei-Jang Yo (National Cheng-Kung Univ.)

- http://www.phys.nthu.edu.tw/~gravity/gws2017/
- Deadline: 10 May 2017 (registration)





Contact: Ling-Wei Luo lwluo@mx.nthu.edu.tw



Sponsors: National Tsing Hua Univ./Physics Department The Gravitational Society of the Republic of China

# Photos at Hsinchu (新竹市)

Physics Building of National Tsing Hua Univ.







# **Photos at Hsinchu**

#### NSPO

(National Space Organization, 国家天空中心) Three floors in a office building (Office, Meeting rooms, Operation rooms), and One dedicated building (Clean building with Satellite assembly and Full-scale tests) in a industrial park.

# <complex-block>

#### Ando Group Seminar (June 8th, 2017, Tokyo)

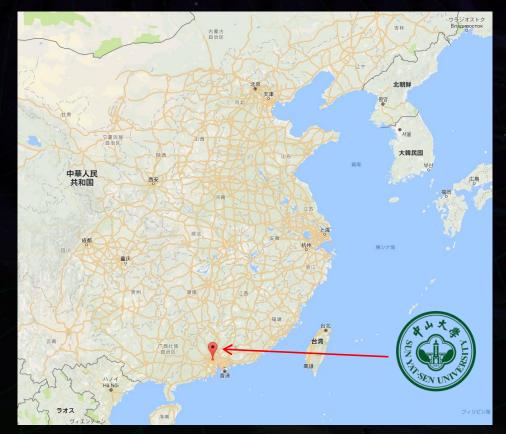
#### Sea food restaurant

# TianQin (天琴) Mission

from Presentations at KIW3 and AIW2 by Prof. Hsien-Chi Yeh (Tianqin Research Center for Gravitational Physics, Sun Yat-Sen Univ.)

KIW3: http://grqc.ncts.ncku.edu.tw/KAGRA2017/program.html AIW2: http://www.phys.nthu.edu.tw/~gravity/gws2017/prog.php

# Sun Yat-Sen Univ (中山大学)



Sun Yat-sen University (孫逸仙大学,中山大学) \* At Guangdong (広東省) \* Founded in 1924

by Google Map

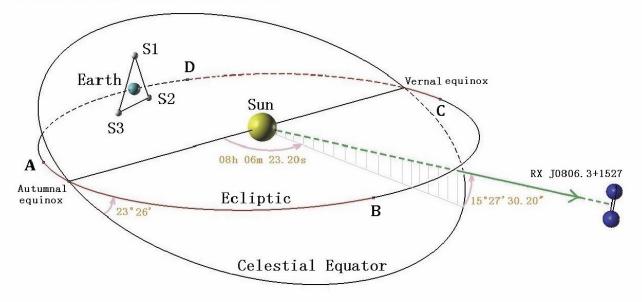
# **TianQin Mission Concept**

## **Guidelines** :

- Geocentric orbit, shorter arm-length, higher feasibility;
- Target a well-known GW source (location and GW frequency) first, as the "calibrated source";

# **TianQin GW Antenna**

- Orbit: geocentric orbit with altitude of 100,000km;
- Configuration: 3-satellite triangular constellation, nearly vertical to the Ecliptic;
- "Calibrated" source: J0806.3+1527, close to the ecliptic;
- Detection time window: 3 months;



**Sensitivity goal** 

G.H.A.Roelofs et al, ApJ, 711, L138 (2010)

T.E.Strohmayer, ApJ, 627,920(2005)

Simbad data base

## Gravitational wave from RX J0806.3+1527

- Masses (0.5, 0.27) Msun
- Period 321.5s (distance between stars 66000km)
- Distance (0.05 ~ 5) kpc
- Strain

$$h_0 \sim h_+ \sim h_\times \sim \frac{2G_N^2 M_1 M_2}{r_0 a} \\ \approx 6.4 \times 10^{-23} \left(\frac{M_1}{0.55 M_\odot}\right) \left(\frac{M_2}{0.27 M_\odot}\right) \left(\frac{5kpc}{r_0}\right) \left(\frac{66000 km}{a}\right)$$

• Integrated strength (90days)

$$h_f = h_0 \sqrt{90 \text{days}} \approx 1.8 \times 10^{-19} / \text{Hz}^{1/2} \left(\frac{M_1}{0.55 M_{\odot}}\right) \left(\frac{M_2}{0.27 M_{\odot}}\right) \left(\frac{5 kpc}{r_0}\right) \left(\frac{66000 km}{a}\right)$$

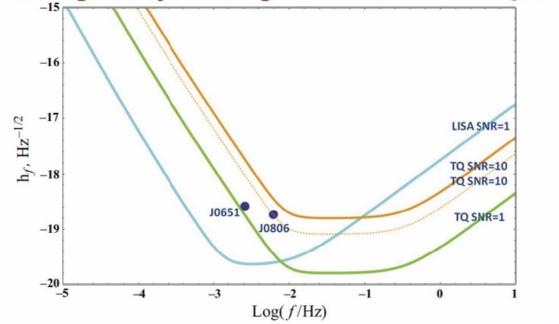
• Relation to noise (SNR=10)

 $\frac{h_f}{10} \ge \frac{2}{\sqrt{R_0}} \Big[ \frac{S_x}{L_0^2} + \frac{S_a}{(2\pi f)^4 L_0^2} \Big( 1 + \frac{10^{-4} \text{Hz}}{f} \Big) \Big]^{1/2} , \quad R_0 \approx 2.0 \quad \text{: Transfer function}$ 

S\_x Noise in distance measurement; S\_a Noise in acceleration

# **Sensitivity Curve of TianQin**

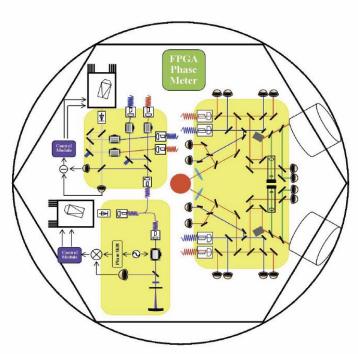
Assuming 90 days of integration time for TIANQIN



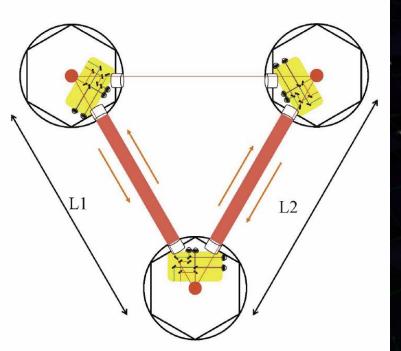
Para.	eLISA	TianQin		
Arm Len.	10 <sup>6</sup> km	1.7*10 <sup>5</sup> km		
Sa <sup>1/2</sup>	7*10 <sup>-15</sup> m/s <sup>2</sup> /Hz <sup>1/2</sup>	3*10 <sup>-15</sup> m/s <sup>2</sup> /Hz <sup>1/2</sup>		
<b>Sx</b> <sup>1/2</sup>	<b>10 pm/Hz</b> <sup>1/2</sup>	1 pm/Hz <sup>1/2</sup>		

# **Configuration of Space GW Antenna**

## **Single Satellite**



## **Triangular constellation**



# Requirements

Key Technologies		Specifications		
Inertial sensing & Drag-free control	Proof mass	magnetic susceptibility 10 <sup>-5</sup> Residual charge 1.7*10 <sup>-13</sup> C Contact potential 100uV/Hz <sup>1/2</sup> @ 10mV		
	Cap. Sensor	$1.7*10^{-6} pF/Hz^{1/2}$ (3nm/Hz <sup>1/2</sup> ) @ 5mm		
	Temp. stability	5uK/Hz <sup>1/2</sup>		
$10^{-15} \text{ m/s}^2/\text{Hz}^{1/2}$	Residual magnetic field	2*10 <sup>-7</sup> T/Hz <sup>1/2</sup> Satellite remanence 1Am <sup>2</sup> @0.8m		
	uN-thruster	100 uN (max); 0.1 uN/Hz <sup>1/2</sup>		
Space Interferometry	Nd:YAG Laser	Power 4 W, Freq. noise 0.1 mHz/Hz <sup>1/2</sup>		
	Telescope	Diameter 20 cm		
1pm/Hz <sup>1/2</sup>	Phasemeter	Resolution 10 <sup>-6</sup> rad		
	Pointing control	Offset & jitter 10 <sup>-8</sup> rad/Hz <sup>1/2</sup>		
	Wavefront distortion	$\lambda/10$		
	thermal drift of OB	5nm/K		

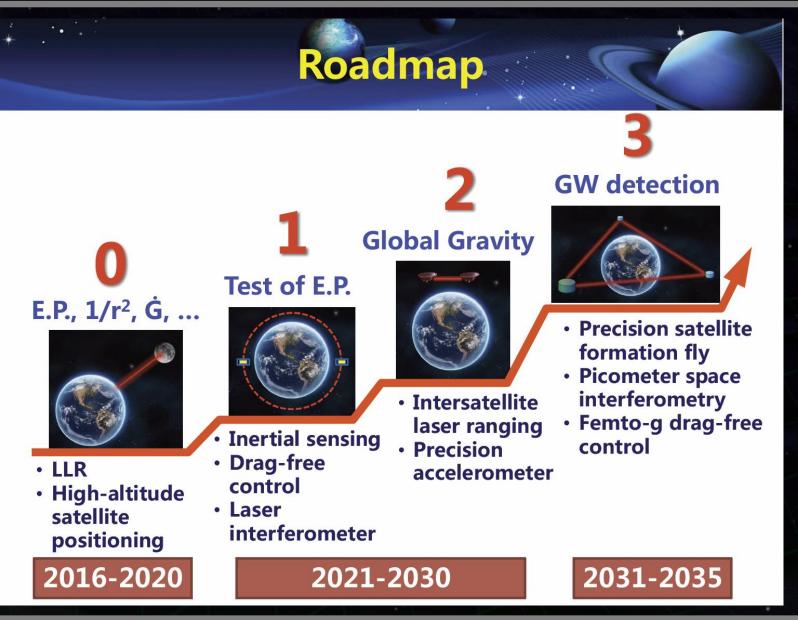
# Key Technologies

## Femto-g Drag-free control:

- > Ultraprecision inertial sensing: ACC, proof mass
- > uN-thruster: continuously adjustable, 5-year lifetime
- > Charge management (UV discharge)

## Picometer laser interferometry:

- Laser freq. stab.: PDH scheme + TDI
- Ultra-stable OB: thermal drift 1nm/K
- Phase meas. & weal-light OPLL: 10<sup>-6</sup>rad , 1nW
- Pointing control: 10<sup>-8</sup>rad@10<sup>6</sup>km
- Ultrastable satellite platform:
  - > Stable constellation: min. velocity and breathing angle
  - Environment control: temperature, magnetic field, gravity and gravity gradient
  - Satellite orbiting: position(100m), velocity(0.1mm/s)
     (VLBI+SLR)



# Four Steps to GWD

## Step-3: TianQin 2016-2035

## **Science objectives**

- General Relativity
- GW astronomy

Class. Quantum Grav. 33, 035010 (2016)

**Technology** 

 $^{13}m/s^{2}$ 

objectives

 $10^{-15}$  m/s<sup>2</sup>

Dragfree 10<sup>-</sup>

1pm@10<sup>7</sup>m

µN-thruster

**Inertial sensor** 

## Precision Inertial Sensing

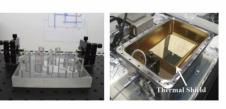
1996-2000: develop flexure-type ACC 2001-2005: space test of flexure-type ACC — launched in 2006 2006-2010: develop electrostatic ACC 2011-2015: space test of electrostatic ACC — launched in 2013



## Space Laser Interferometry

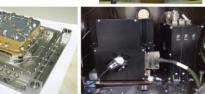
2006-2010: (10m) nm laser interferometer 2011-2015: (200km) inter-satellite laser ranging system

- Picometer laser interferometer
- nW weak light OPLL
- nrad pointing angle measurement
- 10Hz space-qualified laser freq. stab.









## Large-aperture CCR & SLR

Laser Ranging for CE 4 relay satellite

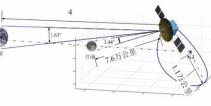
- Manufacturing next-generation laser ranging CCR
- Upgrading ground stations

#### Large-aperture hollow CCR





Yunnan station







- 1. Tianqin will develop all key technologies required for space-based GW detection step by step in the following 15 years.
- 2. Aiming at frequency range of 1mHz-1Hz, Tianqin can provide joint observations with LIGO, KAGRA and LISA.
- 3. Collaboration with DESIGO should be considered seriously, including studying science cases and developing key technologies required for both missions.

# ISGW2017

# **University of Chinese Academy of Science**



by Google Map

UCAS: University of Chinese Academy of Science (中国科学院大学) \* Several campuses at Beijing \* Founded in 1978 \* World's #1 university in Nature Publishing Index (NPI): Ranking of number of papers published in Nature and related scientific magazines (2016).

# **ISGW2017**

- \* Held at International Conference Center (ICC) in the Yanqi campus of the University of Chinese Academy of Sciences (UCAS), Beijing, China.
- \* 3-day Scientific Workshop (1<sup>st</sup> day was for forum)
- \* 12 invited speakers

## ISGW2017 International Symposium on Gravitational Waves May 25-29, 2017, University of Chinese Academy of Sciences, Beijing, China

#### Topics

#### Gravitational Wave Physics

Missions, Strategies and Plans of Gravitational Wave Detection Frontiers of Science and Technology in Gravitational Wave Detection International Collaboration in Gravitational Wave Detection

#### International Advisory Committee (IAC)

Chun-Li Bai (CAS), Peter Bender (CU-Boulder), Karsten Danzmann (AEI), Wen-Rui Hu (IMECH), Takaaki Kajita (Univ. Tokyo), Misao Sasaki (Univ. Kyoto), Li-Bin Xiang (CAS), Wei Yang (NSFC), He-Jun Yin (MOST), Wen-Long Zhan (CAS)

#### **Invited Speakers**

Masaki Ando (University of Tokyo) David Blair (Australian International Gravitational Research Centre) Rong-Gen Cai (Institute of Theoretical Physics, CAS) Yanbei Chen (California Institute of Technology) Stefan Danilishin (Institut für Theoretische Physik) Karsten Danzmann (Albert-Einstein-Institut) Jinn-Ouk Gong (Asia Pacific Center for Theoretical Physics) Gerhard Heinzel (Albert-Einstein-Institut) Gang Jin (Institute of Mechanics, CAS) Shane L, Larson (Northwestern University) Run-Qiu Liu (Institute of Applied Maths, CAS) Misao Sasaki (Kyoto University) Bangalore Sathyaprakash (Penn State University) Bernard F. Schutz (Cardif University) Daniel Shaddock (The Australian National University) Gary Shiu (University of Wisconsin / HKUST) Shinji Tsujikawa (Tokyo University of Science) Stefano Vitale (Università di Trento) Suwen Wang (Stanford University) Yue-Liang Wu (UCAS / Institute of Theoretical Physics, CAS) William Joseph Weber (Università di Trento) Bing Zhang (University of Nevada / Peking University)



# Venue

\* Yanqi campus of UCAS
50km North from Beijing city area (~1hour drive).
\* The conference center has nice accommodations.

\* APEC (Asia-Pacific Economic Cooperation, アジア太平洋経済協力) was held at this area in 2014.



# Photos

#### International Conference Center



## UCAS School Visit (I could not join)



#### Accommodation



### Tour to the Great wall (I could not join)



# **Group Photo**



# Group Photo (Zoom Up)

\*Somewhere: Yanbei Chen \*Not arrived yet : Stefano Vitale, William Joseph Weber, Misao Sasaki





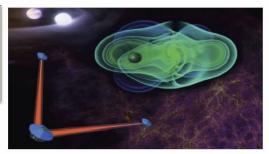
# Taiji Mission (空間太極計画)

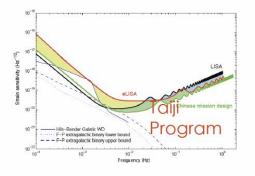
from Presentations at ISGW2017 by Prof. Yue-Liang Wu (UCAS : University of Chinese Academy of Science) ISGW2017: http://isgw2017.csp.escience.cn/dct/page/15

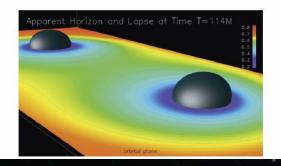


# Taiji Program in Space

- Taiji Program is proposed to detect GW with frequency covering over the range of eLISA (0.1mHz-1.0Hz).
- Focus on the intermediate BH binaries (10^2~10^4 M\_sun)
   With more sensitivity around (0.01-1Hz) (in comparison eLISA)
- How did the intermediate mass seed BH formed in early universe
- Whether DM could form BH
- How the seed BH grows into large or extreme-large BH
- Probe the polarization of GW and understand the nature of gravity

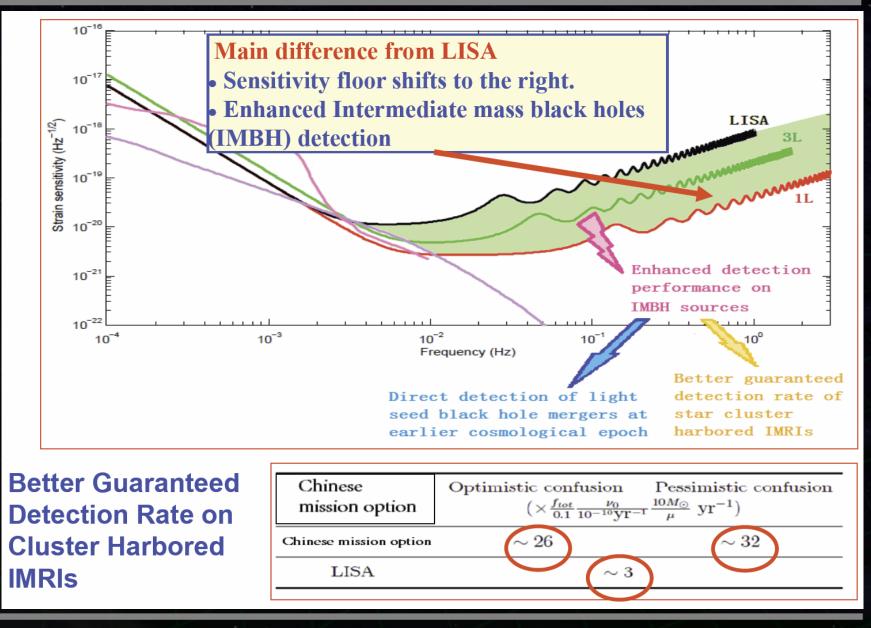






## Taiji Program Baseline Design Parameters (preliminary mission proposal)

	Taiji Program		LISA		eLISA	
	preliminary mission	proposal				
Arm length	3×10 <sup>9</sup> m	5×10 <sup>9</sup> m		1×10 <sup>9</sup> m		
1-way position		_1		_1		
noise budget	5~10 pm Hz	$5\sim10$ pm Hz <sup>-1</sup> / <sub>2</sub>		$Hz^{-2}$	$11 \text{ pm Hz}^{-2}$	
Laser power	2W	2W		2W		
Telescope diameter	~50cm		40cm		20cm	
Acceleration noise budget	3× 10 <sup>-15</sup> ms <sup>-2</sup> Hz <sup>-1/2</sup>	3× 10 <sup>-15</sup> ms <sup>-2</sup> Hz <sup>-1/2</sup>		10-1	3× 10 <sup>-15</sup> ms <sup>-2</sup> Hz <sup>-1/2</sup>	



# Road Map of Taiji Program in Space

# Phase I: 2016-2020 Pre-study on EP. & TH.

Concept & Design

## Taiji concept

- ✓ Design concept
- Measurement scheme
- ✓ Data Analysis
   Mission Design
- ✓ Spacecraft design
- ✓ Mission Analysis

Scientific Research

## Gravitational waves

- ✓ Astrophysics BH
- ✓ Ultra-Compact Binaries
- ✓ Fundamental laws
- Extreme mass ratio inspirals
- Astrophysics of dense stellar sys.
- Test GR & Nature of gravity
- ✓ Cosmology

## Key technologies & Payload

- ✓ Laser system
- $\checkmark$  Optical Sys.
- ✓ Phase
  - measurement
- ✓ Telescope
- Micropropulsi on design

# Road Map of Taiji Program in Space

Phase II: 2020-2025 Taiji Pathfinder mission

Launch Taiji-pathfinder with two satellites Test crucial technologies

Study on the EP. Prototype of GW

# Phase III: 2025-2035 Taiji GW detection

2025-2029: Develop Engineering prototype

2029-2034: Flight load development ~2035: Launch GW spacecraft

More than 10 institutes in China, most of them from the Chinese Academy of Sciences (CAS) have jointly studied the space-based GWD, it dates back to 2008 pioneered by Hu et.al.

The institutions of working groups include:

- ♦ Institute of Mechanics,
- University of Chinese Academy of Sciences (UCAS),
- Institute of Theoretical Physics,
- Academy of Mathematics and Systems Science,
- ♦ Institute of Physics,
- ♦ Institute of high Energy Physics,
- Anjing Institute of Astronomy and Optics,
- National Astronomical Observatory,
- Wuhan Institute of Physics and Mathematics international efforts
- Changchun Institute of Optics,
- Fine Mechanics and Physics, CAS,
- Institute of Geodesy and Geophysics, Wuhan,
- Huazhong University of Science and Technology in Wuhan

GWD covers physics, photonics, astronomy, cosmology, precision measurement, navigation technology and space engineering, etc. We shall work all together with our international colleagues to explore the unknown aspects.

We are going to organize the Taiji Alliance to make both national & international efforts on GW studies.

# Ali Project

## Ali: Micro-wave telescope at Tibet for CMB Polarization Obs.



Probing the origin of our universe through primordial gravitational waves by Ali CMB project

#### CAI Yi-Fu<sup>1</sup> and ZHANG Xinmin<sup>2</sup>

<sup>1</sup>CAS Key Laboratory for Researches in Galaxies and Cosmology, Department of Astronomy, University of Science and Technology of China, Chinese Academy of Sciences, Hefei, Anhui 230026, China and <sup>2</sup>Theoretical Physics Division, Institute of High Energy Physics, Chinese Academy of Sciences, P.O.Box 918-4, Beijing 100049, P.R.China

This is a research highlight invited by SCIENCE CHINA Physics, Mechanics & Astronomy.

Gravitational waves (GW), which were predicted by Einstein in 1916 based on the classical theory of General Relativity (GR), were recently detected by LIGO [I]. This breakthrough is expected to initiate a novel probe of cosmology, the nature of gravity as well as fundamental physics. In general, signals of GWs can be classified into two categories, which are waves from astro-physical and cosmological sources respectively. Accordingly, a number of astronomical and cosmological experiments are under design across the world [2]. In particular, China is playing a very important role in this field by strengthening a series of fundamental scientific subjects, such as cosmic evolution, structure of matter, the origin of life, cognition science, and so on, in the 13th National Five-Year Plan<sup>1</sup>. The Ali project, which aims at measuring the polarization patterns of the cosmic microwave background (CMB) radiation, was put forward in 2014 under the leadership field responsible for yielding inflation gives rise to density fluctuations of quantum origin, of which the wavelengths were initially inside the Hubble radius but were stretched to super-Hubble scales by the exponential expansion of space. These primordial modes become classical and then can provide the seeds for the formation of the large-scale structure (LSS) and the CMB anisotropies [S].

In addition to primordial density fluctuations, inflation also produces primordial tensor perturbations, i.e., primordial GWs [9]. These fluctuations can be described by a traceless and transverse tensor of metric perturbation  $h_{ij}$  governed by a generalized Klein-Gordon equation. In Fourier space, each mode  $h_k$  denoted by a fixed co-moving wave number k obeys the following equation of motion:

 $h_k'' + 2 \frac{a'(\tau)}{a(\tau)} h_k' + k^2 h_k = 0$ ,

#### arXiv:1605.01840

